

$$\binom{52}{2}$$

$$0.245$$

$$\binom{52}{2}$$

$$0.012066$$

$$E(XY) = E(X)E(Y)$$

D 8. Suppose you play one hand, and $X = 1$ if you are dealt two red cards and $X = 0$ otherwise. $Y = 1$ if you are dealt AK and $Y = 0$ otherwise. What is $\text{cov}(X, Y)$?
 a. -0.00128%. b. -0.00179%. c. 0.00107%. d. 0.00591%. e. None of the above.

C 9. If (X, Y) are bivariate normal with $E(X) = 20$, $\text{var}(X) = 25$, $E(Y) = 16$, $\text{var}(Y) = 9$, and $\rho = 0.5$, what is the distribution of Y given $X = 30$?
 a. $N(22.3, 3.52^2)$. b. $N(22.3, 4.52^2)$. c. $N(19.0, 2.60^2)$. d. $N(19.0, 3.52^2)$. e. None of the above.

For the next three problems, suppose a face card is a jack, queen or king. Let A = the event your two hole cards are both face cards, and B = the event your two hole cards are both diamonds.

A 10. What is $P(A \text{ or } B)$?
 a. 10.6%. b. 11.3%. c. 12.9%. d. 14.1%. e. None of the above.

$$\binom{12}{2} + \binom{13}{2} - \binom{3}{2}$$

D 11. What is $P(A \text{ and } B)$?
 a. 0.102%. b. 0.193%. c. 0.204%. d. 0.226%. e. None of the above.

$$\binom{3}{2} \times 100$$

D 12. What is $P(A|B)$?
 a. 1.05%. b. 2.42%. c. 2.67%. d. 3.85%. e. None of the above.

$$\frac{P(A \cap B)}{P(B)} = \frac{\binom{3}{2}}{\binom{13}{2}}$$

For the next two problems, suppose you are playing 20 hands of Texas Holdem. Let X = the number of times you get dealt AK out of your first 10 hands, and Y = the number of hands where you get dealt at least one club, out of hands 11 through 20. Let $Z = 4X + 2Y$.

C 13. What is $E(Z)$?
 a. 8.12. b. 8.33. c. 9.31. d. 9.89. e. None of the above.

$$4 \times 0.119208$$

e. None of the above.

X B 14. What is $\text{Var}(Z)$?
 a. 5.95. b. 7.95. c. 11.8. d. 13.3. e. None of the above.

$$9) \beta_2 = \rho \frac{\sigma_y}{\sigma_x} = \frac{0.5 \times 3}{5} = 0.5 \times 0.6 = 0.3$$

$$16 = \beta_1 + 0.3(20)$$

$$\beta_1 = 10$$

$$9 = (0.3)^2 (25) + \text{var}(\epsilon)$$

$$\text{var} \epsilon = 6.75 = 2.60^2$$

$$Y = 10 + 0.3(30) = 19$$

$$E(X) = 10 \times \frac{16}{\binom{52}{2}} = 0.1206$$

$$E(Y) = 1 - P(\text{no clubs}) = 1 - \frac{\binom{39}{2}}{\binom{52}{2}} \times 10 = 4.41$$

$$Z = 4(0.1206) + 2(4.41) = 9.31$$

A 1. Suppose your opponent bets 3 times the number of chips in the pot when she has a pocket pair, AK, or AQ. In fact, you know she does this 30% of the time when she has a pocket pair, 60% of the time when she has AK, and 40% of the time when she has AQ. Given only this, and no info about your cards or anyone else's cards, what is the probability that she has AK?

- a. 24.4% b. 31.4% c. 40.0% d. 43.2% e. None of the above.

B 2. Suppose $X = 1$ with probability $1/2$, and $X = -1$ with probability $1/2$. What is the moment generating function of X ?

- a. 1. b. $e^{-1/2} + e^{1/2}$ c. $1/2 + e^{1/2}$ d. $1/2 + e^{1/2} + e^{2/2}$ e. None of the above.

B 3. Suppose you are in a winner take all tournament with 1000 chips left. You have $Q\heartsuit 10\heartsuit$. The board is $2\heartsuit 3\heartsuit 4\spadesuit$. There are 400 chips in the pot when the betting on the flop is done. You are up against one opponent who you believe has $5\clubsuit 6\clubsuit$ for a straight. The turn is the $7\spadesuit$. Your opponent now goes all in for 100 chips. Should you call? Assume only knowledge of your cards, the board, and your opponent's cards.

- a. Yes, because your probability of winning is 22.4% which is greater than the necessary 16.7% you need to justify a call.
 b. Yes, because your probability of winning is 20.5% which is greater than the necessary 16.7% you need to justify a call.
 c. No, because your probability of winning is 20.5% which is less than the necessary 29.2% you need to justify a call.
 d. No, because your probability of winning is 20.0% which is less than the necessary 29.2% you need to justify a call.
 e. None of the above.

$$\frac{35}{45}(600) - \frac{35}{44}(400)$$

23 4 7 -
5 6

A 4. Continuing the previous problem, what was your opponent's expected profit, in chips, gained due to luck when the $7\spadesuit$ was revealed as the turn card? Recall that at this point the pot size was 400 chips.

- a. 63.6 b. 72.9 c. 81.4 d. 85.5 e. None of the above.

C 5. Suppose X and Y are bivariate normal with mean 0 and variance 1, and $cov(X, Y) = 0.2$. What is $cov(5X+Y, 4X-2Y)$?

- a. 12.2 b. 14.8 c. 16.8 d. 19.1 e. None of the above.

$$20 - 6 \times 0.2 - 2 = 16.8$$

For the next two problems, let $X = N(0, 0.3^2)$. Let $\epsilon = N(0, 0.2^2)$ where ϵ is independent of X , and let $Y = 7 + 0.4X + \epsilon$.

$$E(7 + 0.4X + \epsilon) = 7 + 0.4 \times 0 = 7$$

A 6. What is $E(Y|X)$?

- a. $7 + 0.4X$ b. $0.4X + \epsilon$ c. 7 d. $7 + 0.4X + 0.2$ e. None of the above.

D 7. What is $cov(X, Y)$?

- a. 0 b. 0.025 c. 0.032 d. 0.036 e. None of the above.

$$0.4 \text{ var}(X) + \text{cov}(X, \epsilon)$$

$$0.4 \times 0.3^2$$