MT2 Physics 1C F18

Full Name (Signature)

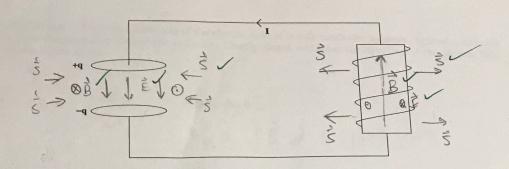
Parth lendertor

Full Name (Signature) Student ID Number ________ 04-930-490 **Seat Number**

Problem	Grade	
1	24	/30
2	18 (18)/30
3	8	/30
Total	50	/90



- Do not peek at the exam until you are told to begin. You will have approximately 50 minutes to complete the
- Don't spend too much time on any one problem. Solve 'easy' problems first. Go for partial credit!
- HINT: Focus on the concepts involved in the problem, the tools to be used, and the set-up. If you get these right, all that's left is algebra.
- Have Fun!



A circular parallel-plate capacitor of plate area A and plate separation d is connected across a solenoidal inductor of radius a, length x and n turns per unit length. At the instant under consideration, the capacitor has a charge q (polarity shown above), and a current I is flowing through the circuit in the direction shown. We do not know the instantaneous rate at which the current is changing, but it may be possible to infer that from the other information we know.

You will be asked to draw vectors on the sketch above. When necessary, please use \odot and \otimes to unambiguously resolve the direction of any azimuthal fields.

• 1a) (10 pts) Find the magnitude of the magnetic field at points inside the capacitor, located a distance r from the symmetry axis of the capacitor. Clearly sketch and label the direction of the magnetic field, the electric field and the Poynting vector field (in the region around the capacitor) on the figure above. Discuss the consistency between the flow of energy as indicated by the Poynting vector field and the changing state of charge on the capacitor.

B: $\mu_0 \Lambda I$ (for induction) $E = \frac{1}{3}, \quad q = CV \Rightarrow V = \frac{q}{C}$ $\int \vec{B} \cdot dl = \mu_0 \left(i_C + \mathcal{E}_0 \right) \frac{d\Phi_E}{dt} = \mu_0 \mathcal{E}_0 \frac{d\Phi_E}{dt}$ $B \cdot 2\pi r = \mu_0 \mathcal{E}_0 \quad d\Phi_E$ $E = \frac{g}{G_0 \Lambda}$ $B \cdot 2\pi r = \mu_0 \mathcal{E}_0 \quad d\Phi_E$ $E = \frac{g}{G_0 \Lambda}$ $\Phi_E = \int \vec{E} \cdot d\vec{r} = \vec{E} \cdot f \Lambda = Cd$ $\vec{E} \cdot \vec{E} \cdot \vec{E} \cdot \vec{E} \cdot \vec{E} = Cd$ $\vec{E} \cdot \vec{E} \cdot$

Flow of energy is inwurds, which makes rense cause capacital is losing charge

$$\int \vec{E} \cdot d\vec{l} = -\partial \vec{p}_{0}, \quad \vec{g} = \mu_{0} N I$$

$$\vec{p}_{0} = \int \vec{B} \cdot d\vec{n} = \mu_{0} N I (\pi r)$$

$$\vec{E} = \mu_{0} N \pi r^{2} dI$$

• 1c) (10 pts) Find the magnitude of the Poynting vector at the boundary of the inductor. Clearly sketch and label the direction of the Poynting vector field on the diagram above. Find the rate at which energy is entering or leaving the inductor, and discuss the result.

$$\vec{S} = \frac{1}{18} |\vec{B}| |\vec{E}| \qquad \vec{E}(\alpha) = \frac{1}{18} |\vec{B}| |\vec{B$$

$$P = \int \vec{S} \cdot d\vec{A} = |\vec{S}(\vec{a})| \int d\vec{A} = |\vec{S}(\vec{a})| 2\pi\alpha x = -2\mu_0 n^2 \pi^2 \alpha^3 I dI$$

since of is (), p is (1). This is consistent since the direction of the Poynting vector, show every leaving the inductor. (È is ravially actuards)

2) Evidence suggests that artists have used lenses and mirrors to assist them from at least as far back as the mid- to early- 1700's. While historians are likely to tell you that lenses, as a technical tool, were still (reading glasses). So the question is, was it possible to use reading glasses to project a (traceable) image of Recall that reading glasses are used.

Recall that reading glasses are used to correct for the migration of the "near point" away from the eye with age. For the following, we'll assume that a typical pair of reading glasses is designed for an uncorrected near-point that is a distance D from the lenses of the reading glasses, and a desired near-point that is a distance d from the lenses.

• 2a) (10 points) Think very carefully about this before you answer (a sketch might definitely help). If a person uses a typical pair of reading glasses to examine the fine detail on some object, where are they going to hold that object (in relation to the lens)? Where will the corresponding image appear? Will the image be real or virtual? Clearly identify the object and image distances (p and q, respectively) for this case—use absolute value bars and explicit signs.

N Puncornelled

It will be a real object: \P = 1P1

Image will appear on same side,
magnifie), "(empé), erect, victual 9= -191

• 2b) (5 points) Find the focal length of the lens. Is it converging or diverging? Explain.

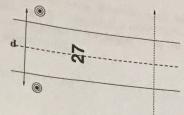
The focal length of the lens will be (1), so it is (convergines) to correct for far significances

 $\frac{1}{f} = \frac{1}{p} + \frac{1}{2} \Rightarrow \frac{1}{f} = \frac{1}{|p| - |q|}$ $f = \frac{1}{p} + \frac{1}{2} \Rightarrow \frac{1}{f} = \frac{1}{|p| - |q|}$ Ms!!

• 2c) (10 points) Let's see if we can project an image of a physical object on a screen using this lens. If if so, where, and what will be its magnification?	
If an object is at L>>0 in have a distant object, at fer point.	
A propertable image will be formed:	
inc. The marked image will	
form on the suren.	2
M= -9 and in this case, since 1pt >> D, 191 >> D we can false the magnification as -1	
• 2d) (5 points) Ok, I apologize, but we need some numbers to gauge the feasibility of the technique. Typical values for the relevant quantities are $L=4$ m, $D=0.5$ m and $d=0.1$ m. How much distance will there be between the lens and the screen? If the physical object located at L is 2 m tall, how large will its image be? Does it seem likely an artist could use this technique to trace a nearly photographic image onto the screen?	
2	
L1, distance between lons and sine = $D-d=0.4m$.	
Since Magnification is ~1, the image will show beignt	
16 10h = ~1 ·	

Yes, it seems likely.

P=



A simple navigation system consists of two radio-frequency antennas fed in-phase with a signal of wavelength λ . The antennas lie along a line that runs perpendicular to the runway, they are equidistant from the center maximum generated by the resultant signal and follow it to a safe landing on the airstrip below.

• 3a) (5 points) Find the full angular width of the central maximum (assume small angle approximations are relevant).

Angular note of central mas = [] Poes not follow dsinor staro = (2m)? For maxima 2

• 3b) (5 points) Under what (approximate) conditions will there only be a central maximum?

 $y_m = \frac{Rm\lambda}{d}$ dsin $\theta \simeq \partial + a_n \theta = (2m) \frac{\lambda}{2}$.

If $\lambda = \frac{\pi}{2}$ is $\lambda = 0$. Here, for any m, $y_m = a_m = 1$.

• 3c) (5 points) It might seem like a good idea to set things up so that there are no higher-order maxima to confuse the pilot, but it really isn't. Why? What compromise needs to be made?

It works are no vigher order maxima, the bilot was to a fall part on, and are to lard society.

• 3d) (5 points) antenna with two in-phase radio signals - one with a wavelength λ_1 and the other with a wavelength λ_2 . Explain how this will fix the problem if the larger of λ_2 and λ_2 is not an integer multiple of the antenna with two in-phase radio signals - one with a wavelength λ_1 and the other with a wavelength smaller (why is this condition important?).

We take the superposition of the two nandersthe interference

25ind & dtand = (2m+1) 1 (WLOG, take dz 7),) + dshe = otand = (2m+1) 1/2 3 same makamas differenty graers!

You = Don (Art dz) of if $\lambda_1 = c\lambda_2$, then You would have the

same maximes, since it como se watter as you = Don(c+1)(1/2) = Don/2

• 3e) (10 points) A pilot decides to calibrate her groundspeed indicator. She flies along a path parallel to the line joining the antennas, a distance D from that line and notes the signal strength at wavelength λ_1 is fluttering at a rate F_1 beats per second. How fast is she flying?

beat francacy is given by Frigt If - Fz!,

$$f_1 = \frac{c}{\lambda_1}$$
 and $f_2 = \frac{c}{\lambda_2}$