

• 1a) (10 points) A uniform disk of charge Q and radius R spins about its perpendicular symmetry axis with an angular velocity $\vec{\omega}$ (as shown in the left diagram above). Derive the (vector) magnetic dipole moment of the distribution.

• 1b) (10 points) A uniform sphere of charge Q and radius R spins about an axis that passes through its center with an angular velocity $\vec{\omega}$ (as shown in the right diagram above). How large a contribution to the total magnetic dipole moment of the sphere will the infinitesimally-thin disk shown in the right diagram make?

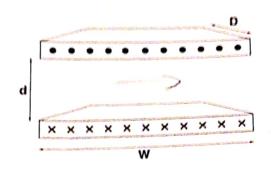
$$R' = R Sn\theta$$

$$\frac{QWR'^{2}}{4} = \frac{QWR^{2}Sn\theta}{4}$$

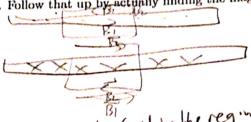
$$\frac{\text{QWR}^2 \text{Sno}}{4} = \frac{3 \text{Sno}}{2 \text{R}}$$

• 1c) (5 points) Derive the (vector) magnetic dipole moment of the spinning spherical distribution.

• 1d) (5 points) When placed in a uniform magnetic field B, the sphere precesses with an angular frequency Ω . Assuming its mass is also uniformly distributed, find the charge-to-mass ratio for the



- 2) Two thin, parallel, conducting sheets of dimension $D \times W$ are separated by a distance d as shown $(D\gg W\gg d)$. The sheets each carry a linear current density K, one into the plane of the page, one out, as shown.
 - 2a) (10 points) Use your knowledge of the magnetic field in and around long, wide current sheets to obtain a qualitative description of the magnetic field in the region between the sheets and in the regions outside the sheets. Follow that up by actually finding the magnetic field in each of those regions.



magnetic field in the region between is pointing to the Right. And the Prognetic Field Outside the sheets is 0.

B= MoKi.

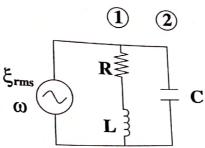
Use Faraday's law to calculate the self-inductance of the arrangement. 2b) (10 points)

Verify your answer for the self-inductance of the arrangement by using energy con-

In each short:
$$\frac{1}{2}L \cdot T^2 = \frac{1}{2} \cdot h_0 \left(\frac{dp}{\omega}\right) \cdot T^2$$

$$= \frac{1}{2} \cdot h_0 \left(\frac{dp}{\omega}\right) \cdot \left(\frac{k\omega}{\omega}\right)^2 = \frac{1}{2} \cdot h_0 \cdot \left(\frac{dp\omega}{\omega}\right) \cdot K^2$$

$$+ \frac{1}{2} \cdot h_0 \cdot \left(\frac{dp}{\omega}\right) \cdot \left(\frac{k\omega}{\omega}\right)^2 = \frac{1}{2} \cdot h_0 \cdot \left(\frac{dp\omega}{\omega}\right) \cdot \left$$



- 3) The following questions all refer to the circuit shown above. For convenience, we'll refer to the branch that contained the convenience as branch 2. that contains the resistor and inductor as branch 1 and the branch that contains the capacitor as branch 2.
 - 3a) (5 points) Find the RMS current through branch 1 and through branch 2.

$$\frac{2}{2} = R + i \Re$$

$$\frac{2}{2} = -i \Re$$

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$$\frac{2}{2} = \frac{2rms}{R} = \frac{2rms}{R}$$

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$$\frac{2}{2} = \frac{2rms}{R} = \frac{2rms}{R}$$
Will the current through branch 1 lead or lag the voltage across it? By how much?
$$\frac{2}{2} = \frac{2rms}{R} = \frac{2rms}{R}$$

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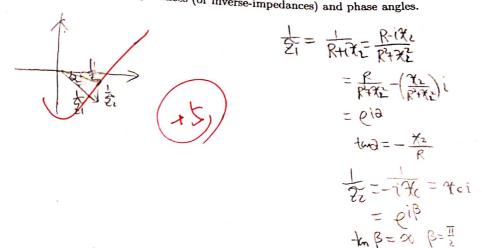
$$\frac{2}{2} = \frac{2rms}{R} = \frac{$$

Will the current through branch I lead or lag the voltage across it by
$$\varphi$$
 where $\tan \varphi = \frac{\chi_1}{R}$, $\Rightarrow 0$.

Thus, $=\frac{\xi_1 x_1}{21} = \frac{\xi_1 x_2}{R} = \frac{\xi_1 x_$

Will the current through branch 2 lead or lag the voltage across it? By how much? 3c) (5 points)

• 3d) (5 points) Sketch the phasor diagram that will describe how the impedance in branch 2 combines with the impedance in branch 1 to give us the effective impedance as seen by the voltage source. Clearly branch impedances (or inverse-impedances) and phase angles.



• 3e) (5 points) At what frequency will the effective impedance seen by the source look purely resistive?

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2} \cdot \frac{1}$$

• 3f) (5 points) How large is the effective impedance when the driving frequency is tuned so that it is purely resistive?

