MT1 Physics 1C F19(1)

Full Name (Printed)

Full Name (Signatu)

Student ID Number

Seat Number

 $E5$

- Do not peek at the exam until you are told to begin. You will have approximately 50 minutes to complete the exam.
- Don't spend too much time on any one problem. Solve 'easy' problems first. Go for partial credit!
- HINT: Focus on the concepts involved in the problem, the tools to be used, and the set-up. If you get these right, all that's left is algebra.
- Have Fun!

A uniform disk of charge Q and radius R spins about its perpendicular symmetry \bullet 1a) (10 points) axis with an angular velocity $\vec{\omega}$ (as shown in the left diagram above). Derive the (vector) magnetic dipole moment of the distribution

$$
u = NIA(T)
$$
 $\pm = \frac{Q}{nR^{2}}$ \rightarrow A=nR² \rightarrow
\n $u = Q \cdot \overrightarrow{x}$
\n $\overrightarrow{u} = Q \cdot \overrightarrow{x}$
\n $\overrightarrow{u} = \mu \overrightarrow{B}$
\n $\overrightarrow{B} = \frac{u_{0}T}{4n} \int \frac{d^{2}x^{2}}{r^{2}}$
\n $\overrightarrow{B} = \frac{u_{0}Q}{4n^{2}R^{4}} \int d\overrightarrow{s}$
\n $\overrightarrow{B} = \frac{u_{0}Q}{4n^{2}R^{4}} \int d\overrightarrow{s}$
\n $\frac{171}{4n^{2}R^{3}} \rightarrow \frac{u_{0}R^{3}|\tau|}{u_{0}q} = \mu \overrightarrow{C}$

A uniform sphere of charge Q and radius R spins about an axis that passes through \bullet 1b) (10 points) its center with an angular velocity $\vec{\omega}$ (as shown in the right diagram above). How large a contribution to the total magnetic dipole moment of the sphere will the infinitesimally-thin disk shown in the right diagram make?

$$
d\vec{B} = \frac{\mu_0 I_{ac}}{4 r_1^2 R^2} \frac{d\vec{L}}{R^2}
$$

$$
\frac{dE}{d\vec{B}} = \frac{4ln^{2}R^{4}}{4ln^{2}d\vec{l}}
$$

Derive the (vector) magnetic dipole moment of the spinning spherical distribution. \bullet 1c) (5 points)

$$
M = NIA
$$
 (1)
\n
$$
T = \frac{\overrightarrow{n}}{4\pi} \times \overrightarrow{6}
$$

\n
$$
\overrightarrow{6} = \frac{u_{0}I_{cm}}{4\pi} \int \frac{d\vec{l} \times \vec{c}}{R^{2}}
$$

\n
$$
\overrightarrow{6} = \frac{u_{0}I_{cm}}{4\pi R^{2}} \int \frac{u}{3} \pi R^{3} \quad |\tau| = \overrightarrow{4}
$$

\n
$$
\overrightarrow{6} = \frac{u_{0}I_{cm}}{13}R \qquad \frac{3\tau}{8} = \pi \overrightarrow{4}
$$

1d) (5 points) When placed in a uniform magnetic field B , the sphere precesses with an angular frequency Ω . Assuming its mass is also uniformly distributed, find the charge-to-mass ratio for the \bullet 1d) (5 points) sphere.

2) Two thin, parallel, conducting sheets of dimension $D \times W$ are separated by a distance d as shown $(D \gg W \gg d)$. The sheets each carry a *linear* current density K, one into the plane of the page, one out, as shown.

2a) (10 points) Use your knowledge of the magnetic field in and around long, wide current sheets to obtain a qualitative description of the magnetic field in the region between the sheets and in the regions outside the sheets. Follow that up by actually finding the magnetic field in each of those regions.

 $B \int B \cdot d\vec{5}$ = Un Im = $\frac{1}{1}$ W = $\frac{2}{1}$ $2BX = u_0$ kx $\frac{10}{3}$ top (artiste) = = = 140 M
 $\frac{10}{3}$ bottom (artiste) = = 140 M
 $\frac{10}{3}$ bottom (artiste) = = 140 M

e Faraday's law to calculate the self-inductance of the arrangement.

$$
n=\frac{d}{dt}
$$
\n
$$
v=\frac{d}{dt}
$$

Verify your answer for the self-inductance of the arrangement by using energy con- \bullet 2c) (10 points) Siderations.
 $W = \frac{1}{2} L T^2 \sqrt{F \cdot \vec{v}} = W \cdot \vec{v}$
 $V = \frac{FN}{W} +$
 $F_B = \pm \vec{c} \times \vec{B} = (\frac{KL}{N})(\omega)(\mu_0 k)$ $F_8 = \frac{\kappa^2 \omega^2}{\hbar \omega} \kappa_0 \kappa$ $\frac{1}{2}LI^{2}$ $K = \sqrt{\frac{1}{W}}$ $F_{B} = K\ddot{\omega} \pm u, \dot{u}$ $\frac{1}{\sqrt{2}} = 1$ $F_{B} = W^{2}W I \mu_{0}$ $\frac{1}{2}LT^{2}=K^{2}mI46\overrightarrow{V}=\frac{J=4Q}{T}=\frac{1}{X}$ $\frac{1}{2}LJ^{2} = \mu^{2}J^{2}Wm.$ $L = 2u^2ww_0 \sqrt{2}$

 \bullet 3d) (5 points) Sketch the phasor diagram that will describe how the impedance in branch 2 combines with the impedance in branch 1 to give us the effective impedance as seen by the voltage source. Clearly label the diagram with the relevant branch impedances (or inverse-impedances) and phase angles.

At what frequency will the effective impedance seen by the source look purely resistive? \bullet 3e) (5 points)

• 3f) (5 points) How large is the effective impedance when the driving frequency is tuned so that it is purely resistive?

2) Two thin, parallel, conducting sheets of dimension $D \times W$ are separated by a distance d as shown $(D \gg W \gg d)$. The sheets each carry a *linear* current density K , one into the plane of the page, one out,

2a) (10 points) Use your knowledge of the magnetic field in and around long, wide current sheets to obtain a qualitative description of the magnetic field in the region between the sheets and in the regions of outlied the

refering to the ampanin loop up top,
\$Bd5=/h+Ienc B= Mok à between plates $Bx = \mu b kx$ outside plates $\vec{B} = 0$

 $B = \mu b K$

. 2b) (10 points) Use Faraday's law to calculate the self-inductance of the arrangement.
 $C_{i} = -\frac{dE_{B}}{dt}$ is notice the relevant area is perpendicular to B
and spans the neapht is length of the arrangement,

 $E_i = -\frac{d}{dt} (B D d)$ 1= 1흁 $\delta_{i} = -\frac{d}{dt} (\mu_{o}KDd)$ $L = \mu_0 D d$ $E_{L} = -\frac{d}{dt} (\mu_{0} \mp \text{d})$ W $\mathcal{E}_i = -\mu_o \frac{\partial d}{\partial u} \frac{dF}{dt}$

 \bullet 2c) (10 points) Verify your answer for the self-inductance of the arrangement by using energy considerations

but $U_B = 1/2LT^2$ (since we picked up all the energy)

 S_{max} $L = \mu_{oDd}$ W

$$
\frac{1}{z_1} = \frac{1}{\sqrt{R^2 + (\omega L)^2}}
$$

$$
\frac{1}{z_2} = \omega C
$$

$$
\tan \alpha = \frac{\omega L}{R}
$$

 $510 \times = \frac{100}{21}$

• 3e) (5 points) At what frequency will the effective impedance by the $\frac{1}{z_2} = \frac{1}{z_1} \sin \alpha$ $\frac{Z_{1}}{R}\omega L$ From the diagram:

 ω

• $3f$) (5 points) How large is the effective impedance when the driving frequency is nurely resistive? that it is

 $\frac{1}{2} = \frac{1}{2}$ Cos ol $=\frac{R}{Z_1Z}$ $rac{1}{z}$

 $(uv)^2 = \frac{L}{C} - R^2$ $R^{2}+(10L)^{2}=\frac{L}{C}$ $z_1^2 = \frac{L}{C}$

 $Z = \frac{RC}{L}$