

# Physics 1C Spring 2018 First midterm

TOTAL POINTS

**88 / 100**

QUESTION 1

11.a 5 / 5

- ✓ + 2 pts Positive
- ✓ + 3 pts explain why positive (RHR,  $v$  cross  $B$ .....)
- + 0 pts wrong

QUESTION 2

2 1.b 5 / 5

- ✓ + 5 pts correct
- + 2 pts Partial points for knowing  $F=qvB$
- + 2 pts Partial points for knowing  $mv^2/R=F$
- + 0 pts wrong

QUESTION 3

3 1.c 5 / 5

- ✓ + 5 pts Correct
- + 4 pts almost correct. Like knowing  $T=2\pi m/qB$ , but forget that we only have a semi circle here.
- + 2 pts partial points for knowing  $t=\pi R/v$ . (understand this is part of uniform circular motion)
- + 0 pts wrong

QUESTION 4

4 1.d 15 / 15

- ✓ + 5 pts semi circle
- ✓ + 5 pts CW
- ✓ + 5 pts correct R
- + 0 pts wrong

QUESTION 5

5 2 30 / 35

- + 35 pts Correct
- ✓ + 30 pts almost correct, but with some small errors.
- + 10 pts Kind of understand the problem but don't know the correct expression for magnetic field.

- + 5 pts nice try
- + 7 pts partial point, get the B field of pipe correct.  $B=0$  inside and  $B=u*I/2*\pi*r$  outside
- + 7 pts partial point, get the B field of wire correct.  $B=u*I/2*\pi*r$
- + 8 pts partial point, get the B field at the center of pipe correct.  $B_c=u*I_{wire}/2*\pi*3R$
- + 8 pts partial point, get the B field at point P correct.  $B_p=u*I_{wire}/2*\pi*R - u*I_{pipe}/2*\pi*2R$
- + 5 pts Partial point, get the ratio expression correct.  $B_p/B_c=-x$ .
- + 0 pts no point

QUESTION 6

6 3.a 8 / 8

- ✓ + 2 pts Identification of magnetic flux as magnetic field times area
- ✓ + 2 pts Correct (or almost correct) integration over non-constant magnetic field through the loop
- ✓ + 4 pts Correct final expression for magnetic flux
- + 0 pts No points

QUESTION 7

7 3.b 12 / 12

- ✓ + 4 pts Correct direction
- ✓ + 4 pts Correct (or almost correct) application of Faraday's Law (in some form)
- ✓ + 4 pts Correct expression for the current (up to a factor of +/-1)
- + 0 pts No points

QUESTION 8

8 3.c 8 / 15

- ✓ + 4 pts Calculate (or at least begin to calculate...) dissipated Ohmic power ( $P = I^2R$ )
- ✓ + 4 pts Calculate external power ( $P = F*v$ ) in full

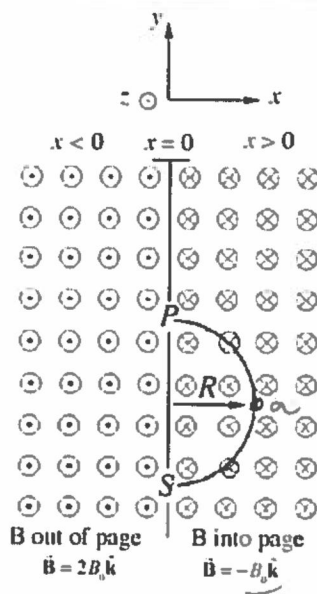
+ **7 pts** Correctly show that the two expressions are equal

+ **0 pts** No points

Physics 1C – Spring 2018: Midterm 1

This exam is closed book and closed notes. Electronics are not permitted, except for one calculator. Please show your full solution in the boxes provided (where the scanners can pick them up). Your solutions will be graded on correctness and coherence; results given with no details will receive zero credit. There is additional scratch paper attached so you can collect your thoughts first. Academic dishonesty is reported to the Office of the Dean of Students.

**Problem 1.** The  $x$ - $y$  plane for  $x < 0$  is filled with a uniform magnetic field pointing out of the page,  $\mathbf{B} = 2B_0\hat{k}$  with  $B_0 > 0$ , as shown. The  $x$ - $y$  plane for  $x > 0$  is filled with a uniform magnetic field  $\mathbf{B} = -B_0\hat{k}$ , pointing into the page, as shown. A charged particle with mass  $m$  and charge  $q$  is initially at the point  $S$  at  $x=0$ , moving in the positive  $x$ - direction with speed  $v$ . It subsequently moves counterclockwise in a circle of radius  $R$ , returning to  $x = 0$  at point  $P$ , a distance  $2R$  from its initial position, as shown in the sketch.



- a. Is the charge positive or negative? Briefly explain your reasoning.

positive, since force is inwards and magnetic field points down, velocity goes from bottom to top  
 (ie @ pt. a,  $F$  is in  $-x$  direction,  $B$  field is in  $-z$  direction, velocity is in  $+y$  direction (RHR))

- b. Find an expression for the radius  $R$  of the trajectory shown, in terms of  $v$ ,  $m$ ,  $q$  and  $B_0$  as needed.

$$\frac{mv^2}{R} = qvB_0$$
$$R = \frac{mv}{qB_0}$$

- c. How long does the particle take to return to the plane  $x=0$  at point P, in terms of  $v$ ,  $m$ ,  $q$  and  $B_0$  as needed?

$$\omega = \frac{qB}{m}, \quad f = \frac{qB}{2\pi m}, \quad T = \frac{2\pi m}{qB}$$

To get to P (half of period), it takes  $\frac{\pi m}{qB_0}$

- d. Describe and sketch the entire subsequent trajectory of the particle after it passes point P. Define any relevant distances in terms of  $v$ ,  $m$ ,  $q$  and  $B_0$ .

after point P

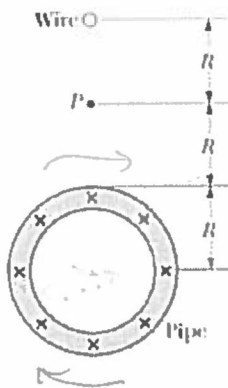
F still points towards  $x=0$ , but  $\mathbf{B}$  is directed up. There velocity will be curving the other way, making the particle still move upwards (RHR)

The magnitude of the  $\mathbf{B}$  field is twice as much as the  $\mathbf{B}$  field for  $x > 0$  so  $R$  will be half as big.

The new radius will be

$$R = \frac{mv}{2qB_0}$$

**Problem 2.** In the figure below a long circular pipe with outside radius  $R$  carries a (uniformly distributed) current  $I$  into the page. A long wire runs parallel to the pipe at a distance of  $3.00R$  from center to center. Find the current in the wire such that the ratio of the magnitude of the net magnetic field at point  $P$  to the magnitude of the net magnetic field at the center of the pipe is  $x$ , but it has the opposite direction.



Let  $I_0 =$  current in the wire

B field of wire @ P

$$B \cdot 2\pi R = \mu_0 I_0$$

$$B = \frac{\mu_0 I_0}{2\pi R}$$

B field at center of pipe

due to the wire

$$B \cdot 2\pi(3R) = \mu_0 I$$

$$B = \frac{\mu_0 I}{6\pi R}$$

$$3 - \frac{3\mu_0 I}{2\mu_0 I_0} = x$$

$$3 - x = \frac{3I}{2I_0}$$

$$I_0 = \frac{3I}{(3-x)2}$$

B field of pipe @ P

$$B \cdot 2\pi(2R) = \mu_0 I$$

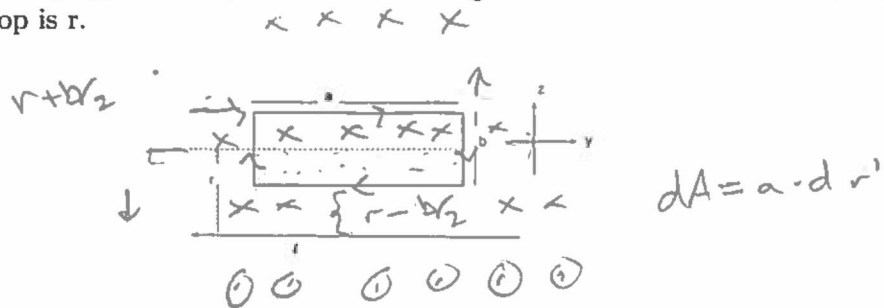
$$B = \frac{\mu_0 I}{4\pi R}$$

$$\frac{\frac{\mu_0 I_0}{2\pi R} - \frac{\mu_0 I}{4\pi R}}{\frac{\mu_0 I_0}{6\pi R}} = x$$

$$\frac{6\mu_0 I_0 - 3\mu_0 I}{2\mu_0 I_0} = x$$

$$\frac{6\mu_0 I_0}{2\mu_0 I_0} - \frac{3\mu_0 I}{2\mu_0 I_0} = x$$

**Problem 3.** A rectangular loop of wire with length  $a$ , width  $b$ , and resistance  $R$  is placed near an infinitely long wire carrying current  $i$ , as shown in the figure. The distance from the long wire to the center of the loop is  $r$ .



- a. Find an expression for the total flux through the loop.

$$\begin{aligned} B &= \frac{\mu_0 i}{2\pi r} \\ \Phi &= \int B \cdot dA = \frac{\mu_0 i}{2\pi} \int \frac{1}{r'} a \cdot dr' = \frac{\mu_0 i a}{2\pi} \int_{r-b/2}^{r+b/2} \frac{dr'}{r'} \\ \Phi &= \frac{\mu_0 i a}{2\pi} \left[ \ln(r+b/2) - \ln(r-b/2) \right] \end{aligned}$$

- b. What is the magnitude and direction of the current flowing in the circuit as it is pulled away from the wire with velocity  $\mathbf{v} = v_0 \hat{k}$ .

$$\begin{aligned} \mathcal{E} &= -\frac{d\Phi}{dt} = -\frac{d\Phi}{dr} \cdot \frac{dr}{dt} \quad v = \frac{dr}{dt} \quad I = \frac{\mathcal{E}}{R} \\ \mathcal{E} &= -\frac{\mu_0 i a}{2\pi} \left[ \frac{1}{r+b/2} - \frac{1}{r-b/2} \right] \cdot v_0 \hat{k} \end{aligned}$$

as the loop is pulled away, the flux will decrease. An induced B field will be generated into the page by Lenz's law, will induce a current clockwise with magnitude

$$\frac{-\frac{\mu_0 i a}{2\pi} \left[ \frac{1}{r+b/2} - \frac{1}{r-b/2} \right] \cdot v_0}{R}$$

- c. Show that to maintain this motion, the rate at which the external force is doing work on the loop is equal to the rate at which energy is being dissipated in the loop.

Energy dissipated = power

$$P = I^2 R =$$

$$\left( \frac{-\frac{M_0 a i}{2\pi} \left[ \frac{1}{(r+b/2)} - \frac{1}{(r-b/2)} \right] v_0}{R} \right)^2 \cdot R =$$

$$\frac{\left[ \frac{-M_0 a i}{2\pi} \left( \frac{1}{r+b/2} - \frac{1}{r-b/2} \right) v_0 \right]^2}{R}$$

External power

$P = F \cdot v$  since velocity is constant,

$$F_{ex} = F_B$$

$F_B$  on the sides w/ length  $b$  cancel,  $F_{Bret} =$

$$\frac{I a M_0 i}{2\pi(r-b/2)} - \frac{I a M_0 i}{2\pi(r+b/2)} = \frac{I a M_0 i}{2\pi} \left( \frac{1}{r-b/2} - \frac{1}{r+b/2} \right)$$

Since  $P_{dis} = P_{Ex}$ , the work done is the same as the energy dissipated





