# 20S-PHYSICS1B-4 Midterm 1

### **RYAN VUONG**

TOTAL POINTS

# 29 / 29.5

QUESTION 1 14 pts

#### 1.1 5/5

 $\checkmark$  + 1 pts Used Newtons Second Law for static equilibrium of the buoy with buoyant force and weight opposing each other.

 $\checkmark$  + 1 pts Noted that the weight of the buoy has magnitude  $\$  v/2

 $\checkmark$  + 2 pts Noted that the buoyant force on the buoy is \$\rho\_w V\_\mathrm{submerged} g\$\$

#### 1.2 8/8

✓ + 1 pts Wrote down Newton's Second Law  $F_B - Mg = M dot z$  (in terms of magnitudes) or  $\delta = M + M c g = M c a$  (in terms of vectors) ✓ + 2 pts Noticed that when weight is subtracted from total buoyant force, all that remains is the change in buoyant force due to the change in volume from the perturbation

✓ + 1 pts Noticed that after a small perturbation, volume displaced and therefore buoyant force will change relative to what it was in static equilibrium. ✓ + 2 pts Used geometry (similar triangles and difference of cone volumes) to determine the change in volume due to a perturbation is \$\$-(V/2)[1-(1-z/h)^3]\$\$ or something equivalent, OR correctly wrote down the small-\$\$z\$\$ approximation to this expression with a correct argument about how it was generated.

# $\sqrt{+1}$ pts Obtained the small-\$\$z\$\$ equation of motion \$\$\ddot z = -(3g/h) z\$\$.

+ **0.5 pts** Obtained partially-correct (incorrect sign) small-\$\$z\$\$ equation of motion \$\$\ddot z = (3g/h)

#### z\$\$.

 $\checkmark$  + 1 pts Correctly deduced angular frequency based on equation of motion written. (Answer just needs to be consistent with equation of motion, but note that correct answer is \$\$\sqrt{3g/h}\$\$.

#### 1.3 1/1

✓ + 0.25 pts Equated \$\$\omega\$\$ expression from

- 1.2 to \$\$2\pi/T\$\$, then solved for \$\$h\$\$.
- ✓ + 0.5 pts Used \$\$T = 1\,\mathrm s\$\$

 $\checkmark$  + 0.25 pts Obtained \$\$h\approx 0.74\,\mathrm m\$\$

+ 0 pts none of the above

#### QUESTION 2

8.5 pts

#### 2.1 3/3

#### $\checkmark$ + 3 pts Argument is air-tight.

+ **2.5 pts** Argument is essentially correct with one or two errors.

+ **2 pts** Reasonable attempt but a few serious flaws in argument.

+ 1 pts Something written but mostly incorrect.

+ **0 pts** Nothing correct.

#### 2.2 3.5 / 4

 $\checkmark$  + 1 pts Noted that for static equilibrium of the block, tension up the ramp and weight pulling down along the ramp need to sum to zero.

✓ + 1 pts Found that component of weight pulling down the ramp has magnitude \$Mgh/ell. ✓ + 0.5 pts Used the relation between wave speed, tension, and mass density  $\$v = \grt{F_T/mu}$ ✓ + 0.5 pts Used (or derived) the expression for the frequency of the  $\$n^{mathrm{th}}\$  harmonic  $\$f_n$ 

#### = nv/(2\ell)\$\$

 $\checkmark$  + 1 pts Combined all of these steps together to obtain  $f_n = \frac{n}{2}\$ 

#### $\checkmark$ - 0.5 pts No work shown for tension solution

- **0.5 pts** Did not simplify linear mass density into givens

- 0.5 pts Incorrect trigonometry
- No force balance shown for tension, it is unclear how you substituted a solution for tension in the velocity equation.

#### 2.3 1.5 / 1.5

 $\checkmark$  + 1 pts Used answer from before and/or similar argumentation to find the following expression for the linear mass density: \$\$\mu =

Mghn^2/(4\ell^3f\_n^2)\$\$

✓ + 0.5 pts Plugged in values and correctly computed \$\$\mu \approx 7\times 10^{-

3}\,\mathrm{kg}/\mathrm m = 7\,\mathrm g/\mathrm m\$\$

+ **1.125 pts** Incorrect answer, but used correct method based on solution from 2.2

- 0.1 pts Incorrect units
- 0.3 pts Math error
- + 0.75 pts Incorrect calculation for mu

#### **QUESTION 3**

7 pts

#### 3.1 6/6

 $\checkmark$  + 1 pts Correctly wrote down Bernoulli's Principle in symbolic form as applied comparing points 1 and 2 along a streamline.

 $\checkmark$  + 0.5 pts Converted flow rate into speed using \$Q = Av\$\$

 $\checkmark$  + 0.5 pts Noted that \$\$A\_1 = \pi(d/2)^2\$\$ and \$\$A\_2 = \pi(D/2)^2\$\$

 $\checkmark$  + 1 pts Noted that only difference in heights of points 1 and 2 matters (or set one of them to zero) and plugged in \$\$H\$\$ accordingly.

 $\checkmark$  + 0.5 pts Made an argument as to why the

pressure to the right of the stopper equals \$\$p\_2\$\$ even after the screw is opened.

 $\checkmark$  + 0.5 pts Asserted that the pressure to the right of the stopper equals \$\$p\_2\$\$ even after the screw is opened.

 $\checkmark$  + 0.5 pts Made an argument as to why the pressure at the ram equals \$\$p\_2\$\$ even after the screw is opened (Pascal's Principle).

✓ + 0.5 pts Asserted that the pressure at the ram equals  $p_2$  even after the screw is opened. ✓ + 1 pts Computed the force on the ram by the fluid (and thus the force it exerts on the object it's crushing) by multiplying the pressure in the fluid in contact with the ram by the ram's area.

#### 3.2 1/1

√ + 1 pts Plugged in all values and got approximately
right answer \$\$F\_\mathrm{ram} \approx
412\,\mathrm N\$\$.

+ **0 pts** Plugged in values did not show approximately right answer \$\$F\_\mathrm{ram} \approx 412\,\mathrm N\$\$.

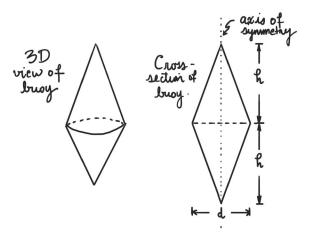
+ **0.25 pts** Found correct solution from incorrect 3.1 formula

## Physics 1B, Spring 2020, Midterm 1

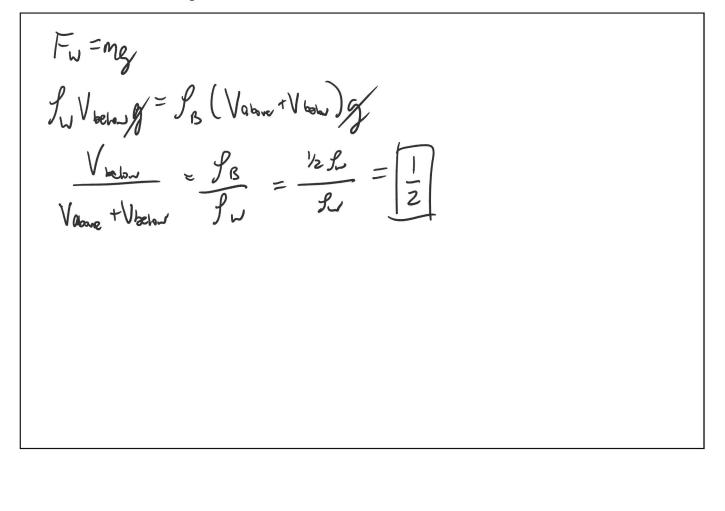
#### Instructions.

- 1. Complete this exam packet, and submit it to Gradescope before the end of the exam period.
- 2. Make sure all final work is in only the spaces provided, and make sure to upload a document of exactly the length of this packet.
- 3. If you are using a smartphone to generate a scan, please use a scanning app such as Adobe Scan to quickly generate an optimized PDF document.
- 4. There is extra space at the end of the packet in case the space below each problem isn't sufficient, but if you use that extra space, make sure to indicate that extra work is contained there when you show your work for a problem.
- 5. You are allowed to use the CCLE course page, the course textbook (OpenStax), and your notes, but you are not permitted to use any other internet resources.
- 6. A calculator (whatever type desired) is allowed.
- 7. You may not communicate about the contents of this exam with anyone during the exam period.
- 8. You may not logon to Campuswire during the exam period.
- 9. Josh and the TAs will not be free to answer clarifying questions about the exam during the exam period. If you believe there is an ambiguity, feel free to make a note of it to yourself and we will attempt to address it post-exam, but otherwise do your best to answer the questions based on what they say.
- 10. Violations of instructions pertaining to what you are not allowed to do during the exam will be considered cheating and will be reported to the Dean of Students.

**1.** Bobbing Buoy. A buoy is a floating device that can have many purposes, but often as a locator for ships. Collin constructs a hollow metal buoy by welding together two identical cones of height h and diameter d. The resulting double-cone buoy has average density equal to half the density of seawater meaning that its total mass divided by total volume is half the density of seawater. Throughout this problem, you can ignore the air above the sea's surface.



**1.1.** When the buoy is at rest in a calm ocean, with its axis of symmetry perpendicular to the water's surface, what fraction of it will be submerged?

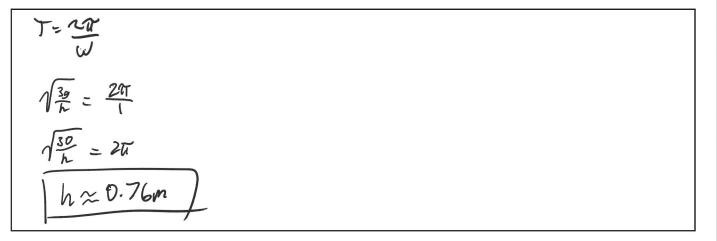


**1.2.** If the buoy is at rest at time t = 0 and is then pushed down slightly into the water and let go, what will be its angular frequency  $\omega$  of small oscillations in terms of the given variables? Note: the volume of a cone of height h and base area A is hA/3.

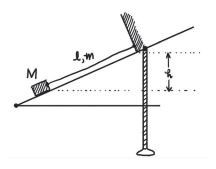
Fruch = Fi - Mg,  

$$\begin{aligned}
F_{nub} &= F_{i} - Mg, \\
\int_{Mg} f_{i} = \frac{2hA}{8} = \frac{2h(Td^{2})}{3} \\
\int_{bung} V_{hung} Q_{i} = f_{i} V_{bein} Q - f_{hung} V_{bung} Q \\
\int_{bung} V_{hung} Q_{i} = f_{i} V_{bein} Q - f_{hung} V_{bung} Q \\
\int_{hung} V_{bung} Q_{i} = f_{i} V_{i} Q \\
\int_{hung} V_{i} = h Td^{i} Q \\
\int_{hung} V_{$$

**1.3.** What should be the height h of each cone in the buoy so that the buoy will execute one oscillation period every second and therefore be usable as a clock with one-second accuracy?



2. Mills' Musical Machine. A Mills banjo is a musical instrument which relies on being placed near the surface of the Earth to operate. It consists of a block of mass M that is being prevented from sliding down a frictionless incline by a thin string of length  $\ell$  and mass m attached to a stationary wall. The steepness of the incline can be adjusted by adjusting the height h with a screw as indicated on the diagram. The string can be plucked like a guitar string. Assume that the block is sufficiently massive that the string can be treated as though it's fixed at both endpoints.



**2.1.** If all other variables besides h are held fixed, do you expect the frequencies of the harmonics on the string to increase, stay the same, or decrease if h is increased? Make as compelling a physical argument as you can without writing down any equations.

As h increases, tension increases because the string is getting more vertical. With a greater tension, the string would more faster when pluched because it would be more sensiture to plucking. As v increases, frequency increases because the String would be oscilleting and reaching creats at a faster rate. As 4

**2.2.** What is the frequency of the  $n^{\text{th}}$  harmonic of the string in terms of the variables given in the problem statement?

$W = \frac{n \pi}{L} V$
$V = \sqrt{\frac{F_T}{u}} = \sqrt{\frac{M_g  s_{MO}}{u}} = \sqrt{\frac{M_g  (\frac{h}{z})}{\binom{m}{p}}} = \sqrt{\frac{M_g h}{m}}$
$\omega = \frac{n \pi}{l} \sqrt{\frac{Ngh}{m}}$
$W = \frac{2\pi}{s} = 2\pi f$ $\int f = \frac{n}{2l} \sqrt{\frac{M_{gh}}{m}}$

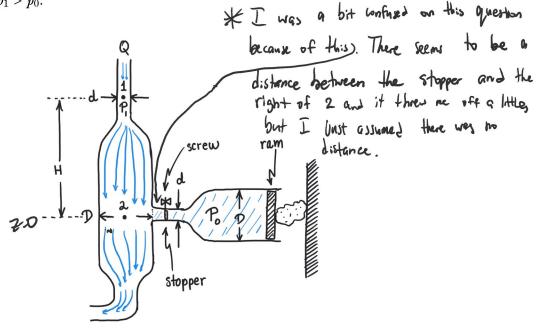
**2.3.** If the block has a mass of 20 kg, the height h is 0.5 m, the string has a length of 0.77 m, and the 5th harmonic has frequency 445 Hz, what is the linear mass density  $\mu$  of the string?

$$44S = \frac{5}{2(0.77)} \sqrt{\frac{20(10)(0.5)}{0.77}}$$

$$137.06 = \sqrt{\frac{129.9}{M}}$$

$$M = 0.007 \frac{15}{3} M$$

3. In the apparatus below, the Dynamic Aqua Crusher, water is injected into a vertical channel at a volume flow rate Q. The diameter of the channel at point 1 is d, and its diameter at point 2 is D. To the right of point 2 is a horizontal channel blocked by a stopper. The small diameter of this horizontal channel is d, and the large diameter is D. To the right of the stopper is a chamber with static water. When the stopper is clamped in place by a screw, the pressure in the chamber is  $p_0$ . When the clamp is unscrewed, the stopper is free to move. At the right-hand end of the chamber is a ram that can be used to crush things against a wall. Let  $\rho$  be the density of water,  $p_1$  be the pressure at point 1 in the vertical channel, and H be the vertical distance between points 1 and 2. You may assume that  $p_1 > p_0$ .



**3.1.** Suppose that the clamp is unscrewed and the stopper is free to move. Find an expression in terms of the given variables for the force exerted by the ram on whatever it's crushing in this circumstance.

$$\begin{split} \rho_{i} + \frac{1}{2} \int V_{i}^{2} + \int g H &= \rho_{2} + \frac{1}{2} \int V_{2}^{2} + \int g(0) \\ \rho_{i} + \frac{1}{2} \int \left(\frac{Q}{A_{i}}\right)^{2} + \int g H = \rho_{2} + \frac{1}{2} \int \left(\frac{Q}{A_{i}}\right)^{2} \\ \rho_{i} + \frac{1}{2} \int \left(\frac{Q}{\pi \left(\frac{A}{2}\right)}\right)^{2} + \int g H = \rho_{2} + \frac{1}{2} \int \left(\frac{Q}{\pi \left(\frac{A}{2}\right)}\right)^{2} \\ \rho_{i} + \frac{8Q^{2}g}{\pi^{4}} + \int g H = \rho_{2} + \frac{8Q^{2}g}{\pi^{4}} \\ \rho_{z} = \rho_{i} + \frac{8Q^{2}g}{\pi^{2}} \left(\frac{1}{d^{4}} - \frac{1}{D^{4}}\right) + \int g H \end{split}$$

$$\begin{aligned} \rho_{Z} &= \frac{F_{r_{q_{m}}}}{A_{p}} \\ F_{rom} &= \frac{\pi}{\pi} \left(\frac{D}{z}\right)^{2} \left(\rho_{1} + \frac{8}{\pi^{2}} \frac{Q^{2} \rho}{\pi^{2}} \left(\frac{1}{d^{4}} - \frac{1}{D^{4}}\right) + \int_{g} H \right) \end{aligned}$$

**3.2.** If d = 1 cm, D = 5 cm, H = 1 m,  $p_1 = 2 \times 10^5 \text{ Pa}$ ,  $p_0 = 10^5 \text{ Pa}$ , and  $Q = 100 \text{ cm}^3/\text{s}$ , what is the magnitude of the force that the ram exerts on the object it's crushing?

$$F_{\text{Max}} = \mathcal{T}\left(\frac{.05}{2}\right)^{2} \left(2_{\text{HD}}^{5} + \frac{8\left((10^{-4})^{4}\right)^{2}}{7^{4}}\left(\frac{.00}{(.01)^{4}}\right) + (1000(10)(1))\right)$$

$$= \frac{1413.86N}{1413.86N}$$

Space for extra work.

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