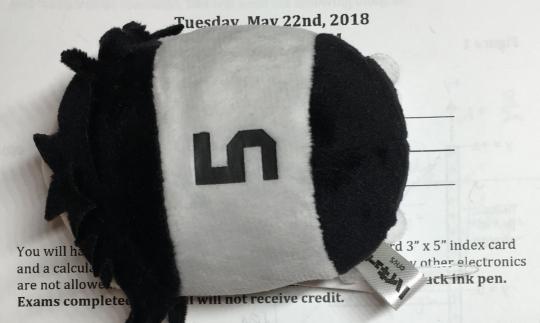
#### MIDTERM EXAM #2 Physics 1B Lecture 3 Instructor: Anton Bondarenko



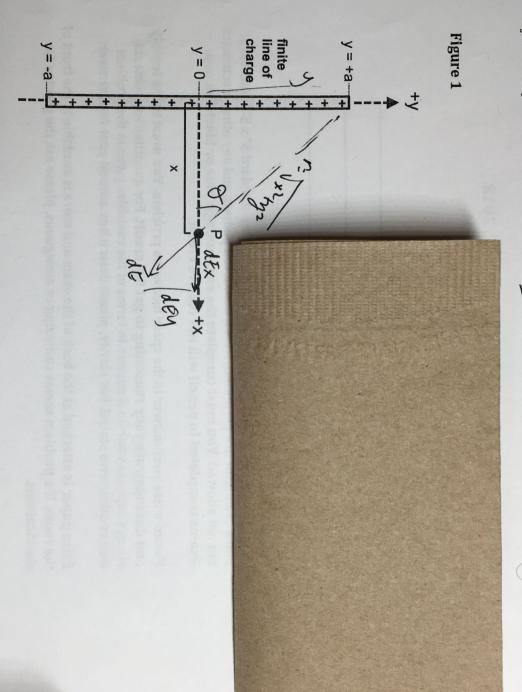
Please write your answer in the space below the problem. You must write legibly and demonstrate your reasoning to get full credit. For quantitative problems, always express your final answer in terms of the variables given in the problem unless otherwise stated. For clarity, please draw a box around your final answer.

Extra paper is attached at the back of the exam and more is available in the front of the room. If a problem seems confusing or ambiguous, please ask the proctor for clarifications.

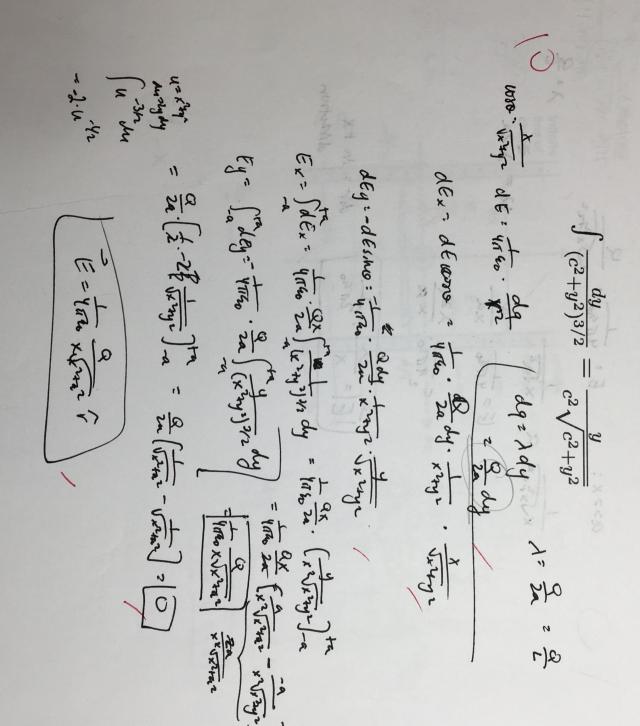
#### DO NOT TURN PAGE UNTIL INSTRUCTED

## Problem 1 (40 points total):

y=-a and y=+a. The line of charge has a uniform positive linear charge density  $\lambda$ . Figure 1 below shows a finite line of charge positioned along the y-axis between



the electric field at point *P*, which is located along the x-axis at a distance *x* from the line of charge. (2) Then, evaluate the integrals to obtain the magnitude and direction Part A (10 points): (1) Derive integral expressions for the x and y components of and fundamental constants. You will need the following integral: of the electric field at point P. Express your answer in terms of the given parameters



Part B (10 points): Now, determine the magnitude and direction of the electric field at point P due to an infinitely long line charge by evaluating the expression

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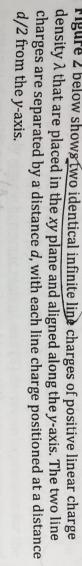
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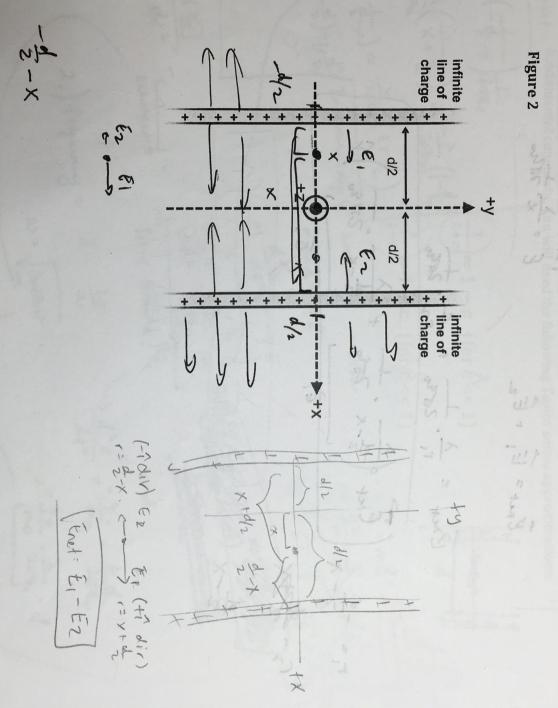
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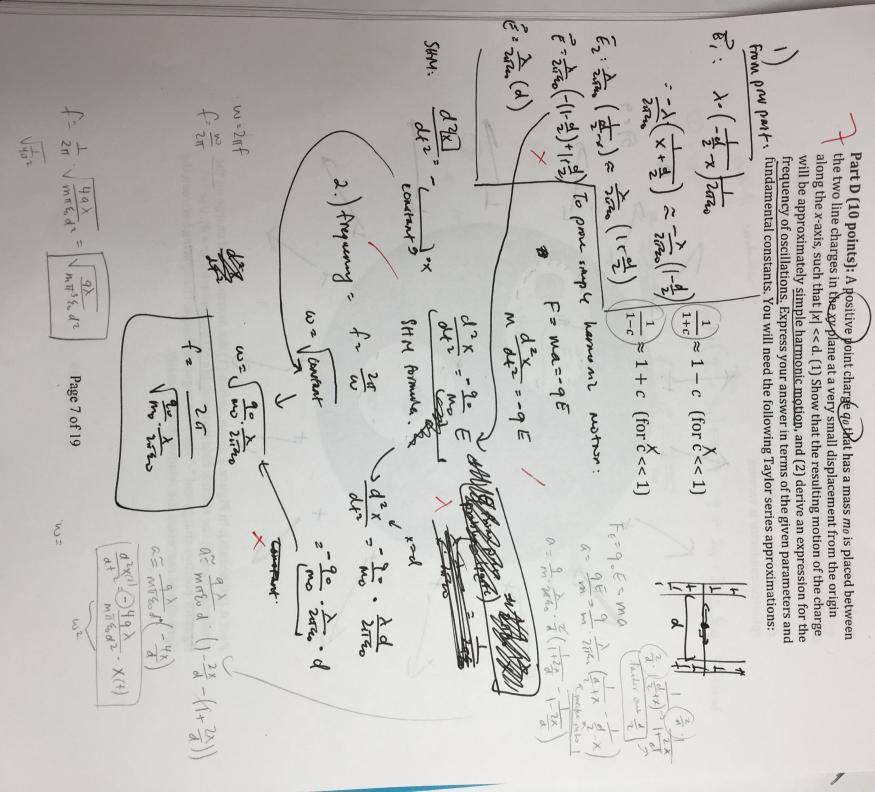
**Figure 2** below shows two identical infinite line charges of positive linear charge density  $\lambda$  that are placed in the xy plane and aligned along the y-axis. The two line charges are separated by a distance d, with each line charge positioned at a distance





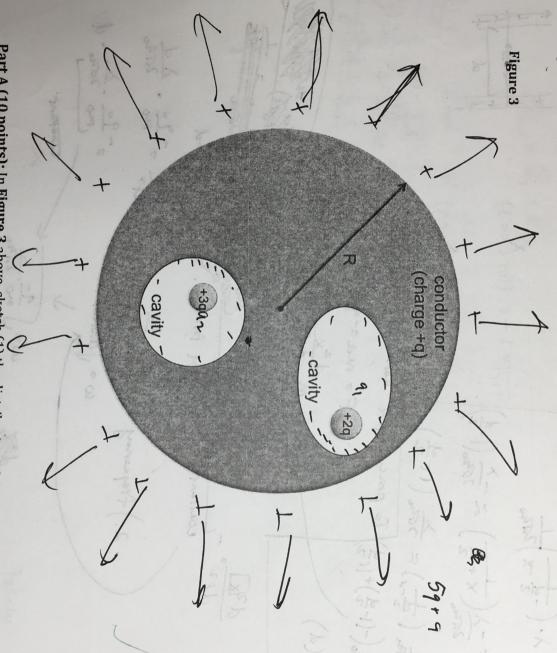
**Part C (10 points):** Determine the magnitude and direction of the electric field as a function of x in the range -d/2 < x < +d/2 in the xy plane (i.e., between the two line charges). Hint: use the result from Part B and the principle of superposition.

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### Problem 2 (30 points total):

spherical conductor is vacuum. charge +3q. For this problem, assume the space in the cavities and outside of the contains a positive point charge +2q, and the other cavity contains a positive point charge +q. The conductor also contains two internal cavities. One of the cavities As shown in Figure 3 below, a spherical conductor of radius R holds a net positive



signs should represent the relative charge density. signs for positive charge and "-" signs for negative charge. The spacing between the **Part A (10 points):** In **Figure 3** above, sketch (1) the distribution of charge on the conductor and (2) the electric field lines outside of the conductor (r > R). Use "+"

**Part B (10 points):** Determine the magnitude and direction of the electric field as a function of radial distance r from the conductor center (1) outside of the conductor (r > R) and (2) inside of the material of the conductor. Express your answer in terms of the given parameters and fundamental constants.

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Express your answer in terms of the given parameters and fundamental constants. determine the potential as a function of radial distance r from the conductor center (1) outside of the conductor (r > R) and (2) inside of the material of the conductor. Part C (10 points): Taking the electrostatic potential to be zero infinitely far away,

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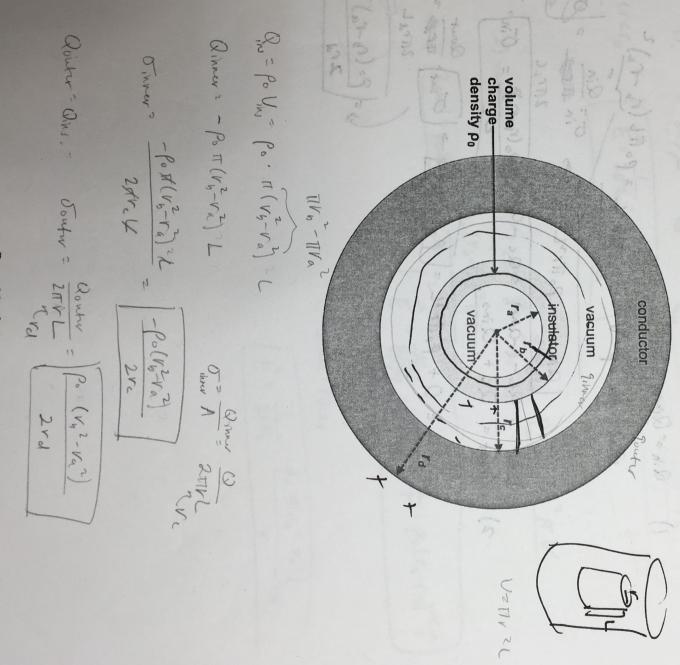
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# Problem 3 (30 points total):

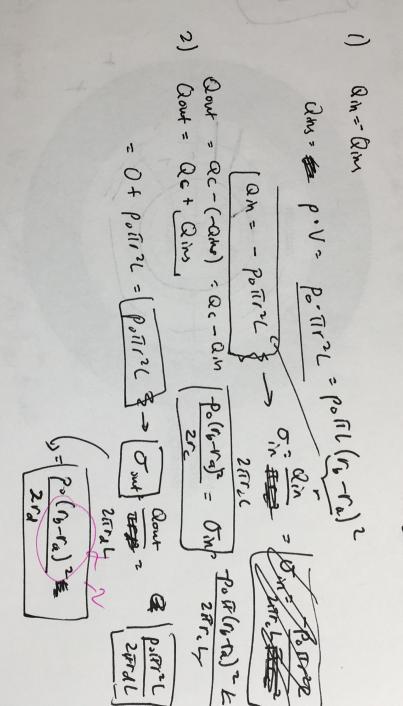
**Figure 4** shows the cross-section of an infinitely long insulating tylindrical shell of inner radius  $r_a$  and outer radius  $r_b$  that has a uniform positive volume charge density  $\rho_0$ . The insulating shell is centered within an infinitely long uncharged conducting cylindrical shell of inner radius r<sub>c</sub> and outer radius r<sub>d</sub>.

Figure 4

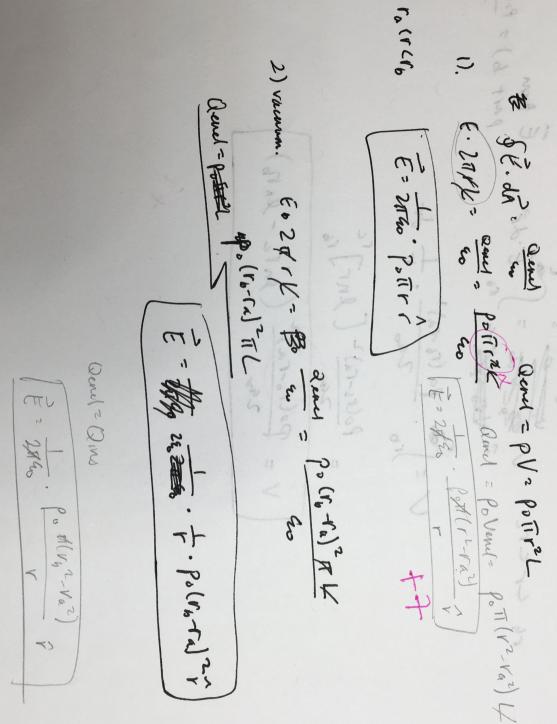


Part A (10 points): Determine the surface charge density on (1) the inner surface of the conducting shell and (2) the outer surface of the conducting shell. Express your answers in terms of the given parameters and fundamental constants.

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shell ( Part B (10 points): Determine the magnitude and direction of the electric field as a rb) and (2) in the vacuum region between the insulating shell and the conducting fundamental constants.  $r < r_c$ ). Express your answers in terms of the given parameters and



**Part C (10 points):** Calculate the voltage (i.e., the magnitude of the potential difference) between the outer surface of the insulating shell  $(r = r_b)$  and the inner surface of the conducting shell  $(r = r_c)$ . Express your answer in terms of the given parameters and fundamental constants.

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#### SCORING

### Problem 1:

### Problem 2:

Part A: \_\_\_\_/10
Part B: \_\_\_\_/10
Part C: \_\_\_\_/10
Total: \_\_\_\_/30

### Problem 3:

Part A: \_\_\_\_/10
Part B: \_\_\_\_/10
Part C: \_\_\_/10
Total: \_\_\_/30

Total Midterm #2 Score 90 / 100