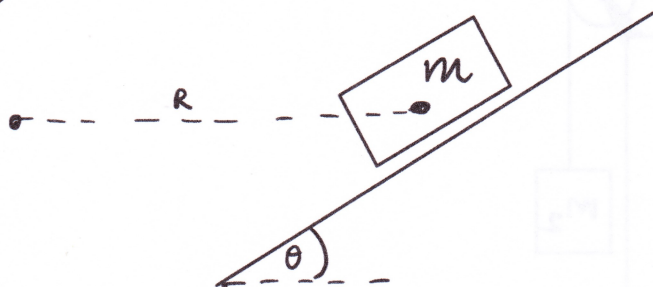


Challenge Problem Set 1

(Nayana Rajapakse)

1

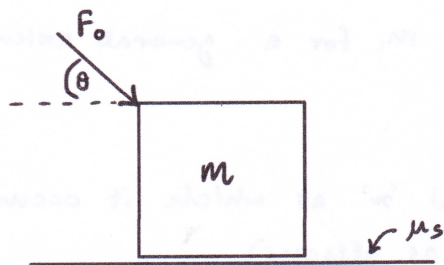


A car (represented with box) is on a banked circular track expecting to drive in circular motion.

here $\theta \geq \tan^{-1}(\mu_s)$ where μ_s is the static friction coefficient between the track and the car. R and m are the radius of the expected circular motion and the mass of the car respectively.

- Show that the car can't remain in equilibrium unless it is moving.
- Find the minimum speed at which the car must travel to avoid sliding down.
- Find the maximum speed at which the car can travel without sliding on the ramp.
- Now articulate an argument from which you could have deduced the answer you got for (d) from that of (c) without redoing the work.
- Summarize the results found in (c) and (d) to write down the range of the car's speed in circular motion without sliding.

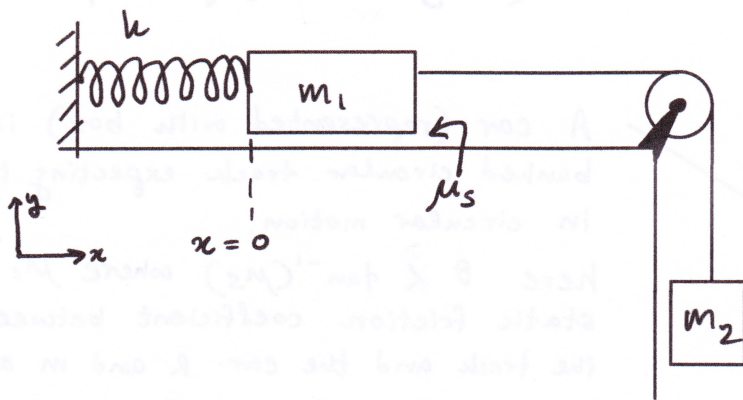
2



As shown a box with mass m is sitting on a rough surface where the static friction coefficient between the two surfaces is μ_s . An external force F_0 is applied on the box as shown making an angle θ with the horizontal.

- Find the maximum allowed F_0 (i.e, $F_{0,max}$) such that the box would still remain in equilibrium.
- Now F_0 is slightly increased above the value found in (a) making the box to move. Soon after that F_0 is brought back to the value found in (a). Conceptually explain why the box will not return to equilibrium.
- After performing the steps in part (b) obtain expression for the acceleration of the block in terms of μ_s, μ_k, θ and g where μ_k is the kinetic friction coefficient

3



Two boxes with masses m_1 and m_2 are connected with a rope and are setup as shown in the figure. μ_s and μ_k are static and kinetic frictional coefficient between the box and the horizontal table. m_1 is connected to spring with a spring constant k which is then connected to a wall as shown. Initially the spring is relaxed. definition of $x=0$ is shown.

(a) If $\mu_s < m_2/m_1$ show that the system will not be in equilibrium with spring relaxed.

For the subsequent parts assume $\mu_s < m_2/m_1$

(b) For a general extension ' x ' of the spring, find an expression for acceleration of m_1 and tension of the string.

(c) Find ' x ' (call it x_0) at which instantaneous acceleration is zero.

(d) Find an expression for the velocity ' v ' of m_1 for a general extension ' x '

$$\left(\text{use } a = \frac{dv}{dt} = v \frac{dv}{dx} \right)$$

(e) Find the maximum of v (call it v_{max}) and ' x ' at which it occurs. (you may use any results obtained above as always)

(f) Find the maximum extension of the spring and the acceleration of m_1 and tension of the string at that moment