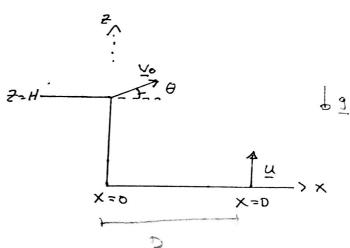
(25 Pts)

- 1. At time t=0, a ballistic missile is launched from the top of a mountain of height z=H located at x=0 with an initial velocity \mathbf{v}_0 that makes an angle θ with respect to the horizontal as shown. At t=0, a gunner on the ground is located at a distance D from the base of the mountain, and fires a shell vertically upward with an initial speed u.
- (9) a. Write the equations for the position $x_M(t)$ and $z_M(t)$ for the missile, and $z_S(t)$ for the shell.
- (6) b. Now express the height of the missile and the height of the shell as a function of the x-position of the missile.
- (10) c. Show that for the shell to hit the missile, the shell should be fired with an initial vertical speed given by

$$u = \frac{[H\cos\theta + D\sin\theta]}{D} v_0$$



a)
$$V_m(t) = v_0 \cos \theta t$$

 $Z_m(t) = v_0 \sin \theta t - \frac{1}{2}gt^2 + H + \frac{1}{2}G$
 $Z_S(t) = ut - \frac{1}{2}gt^2$

$$\frac{2}{N}(t) = v_0 \sin\theta \left(\frac{x_m(t)}{v_0 \cos\theta}\right) - \frac{1}{2}g\left(\frac{x_m(t)}{v_0 \cos\theta}\right)^2 = x_n(t) \tan\theta - \frac{g \times n(t)}{2v_0^2 \cos^2\theta}$$

$$\frac{2}{2}s(t) = u\left(\frac{x_m(t)}{v_0 \cos\theta}\right) - \frac{1}{2}g\left(\frac{x_m(t)}{v_0 \cos\theta}\right)^2$$

$$\frac{2v_0^2 \cos^2\theta}{2v_0 \cos\theta}$$

C)
$$H+v_0 \sin\theta t - fgt' = ut - fgt^2$$
 $ut = H+v_0 \sin\theta t'$
 $u = \frac{H+v_0 \sin\theta t}{t}$
 $u = \frac{D}{V_0 \cos\theta t}$
 $u = \frac{D}{V_0 \cos\theta t}$
 $u = \frac{D}{V_0 \cos\theta t}$
 $u = \frac{D}{D}$
 $u = \frac{D}{D}$

(30 Pts)

- 2. A block with mass M is pulled along a frictionless horizontal surface by an applied horizontal force F_a as shown. Block M is connected to a massless rope (Λ) that passes over a massless pulley and connects to a block with mass m_A located on an inclined plane with inclination angle θ as shown. Block m_A is connected to a third block with mass m_B on the inclined plane by a second massless rope (B) as shown.
- (9) a. Draw free body diagrams for each of the three blocks.
- (15) b. Assuming that the three blocks accelerate together, prove that the acceleration is given by

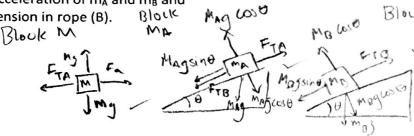
$$a = \frac{F_a - (m_A + m_B)gsin\theta}{m_A + m_B + M}$$

(6) c. Suppose that rope (A) breaks. Find the acceleration of m_A and m_B and the tension in rope (B).

ma rope a m

Block Ma

a)

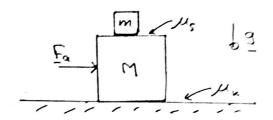


Because tensions all cand out st. peer time more work with the man that man more work with the more work as Fa-(ma+ma) y sind

C) Find
$$a = \frac{z F_{mt}}{z_{m}}$$
 $a = \frac{-M_{Ag}sind - F_{TB} - M_{Bg}sind}{M_{A} + M_{B}}$

- (30 Pts)
- 3. A block with mass M is pushed along a rough horizontal surface, with a coefficient of kinetic friction μ_k , by an applied horizontal force F_{α} as shown. A second block with mass m sits on top of block M. The coefficient of static friction between the surfaces of m and M is μ_s .
- (10) a. Draw free body diagrams for the two blocks.
- (10) b. If m does <u>not slip</u> relative to M, find the acceleration of the system.
- (10) c. Show that the <u>maximum</u> value of the applied force for which m remains at rest relative to M is given by

$$(F_a)_{MAX} = (m+M)(\mu_k + \mu_s)g$$



a)
$$f_s = \frac{1}{M}$$
 $f_s = \frac{1}{M}$
 $f_s = \frac{1$

C)
$$mg\mu_s = F_A - (m+m)g\mu_k - mg\mu_s \int$$

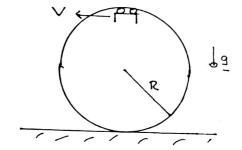
$$10 F_A = mg\mu_s + (M+m)g\mu_k + mg\mu_s$$

$$= (M+m)g\mu_s + (M+m)g\mu_k$$

$$= (M+m)g(Ms+\mu_k)$$

(15 Pts)

- 4. A thrilling roller coaster has a vertical circular loop with a radius R as shown.
- (10) a. Find the minimum circular speed at which the roller coaster must be traveling in order that an un –seat-belted passenger does not fall out at the top of the loop.
- (5) b. If the roller coaster travels at this same speed when it is at the bottom of the loop, show that a passenger's weight would be double its normal value.



a)
$$\frac{mv^2}{R} = my$$

$$v = \sqrt{R}$$
 $v = \sqrt{R}$

Find
$$\frac{mv^2}{R} = F_N - m_y$$

$$F_N = \frac{mv^2}{R} + m_y$$

$$F_N = \frac{mp_y}{R} + m_y$$

$$F_N = \frac{mp_y}{R} + m_y$$

$$F_N = 2m_y$$