## MIDTERM EXAM #1 Physics 1A Lecture 2 Instructor: Anton Bondarenko

Friday, May 3<sup>rd</sup>, 2019 10:00 AM - 10:50 AM

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First name:	Miles	
University ID:		
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You will have **50 minutes** to complete this exam. One standard 3" x 5" index note card is permitted. Notes, books, cell phones, calculators, and any other electronics are not allowed. You must complete the exam using a blue or black ink pen. Exams completed in pencil will not receive credit.

Please write your answer in the space below the problem. You must write legibly and demonstrate your reasoning to get full credit. For quantitative problems, always express your final answer in terms of the variables given in the problem unless otherwise stated. For clarity, please draw a box around your final answer.

Extra paper is attached at the back of the exam and more is available in the front of the room. If a problem seems confusing or ambiguous, please ask the proctor for clarifications.

# DO NOT TURN PAGE UNTIL INSTRUCTED

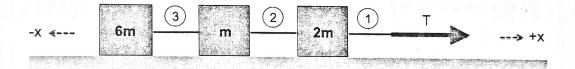
#### Problem 1 (40 points):

As shown in **Figure 1** below, three blocks of mass 2m, m, and 6m slide along a frictionless horizontal surface. The blocks are connected by identical strings of negligible mass, labeled 1, 2, and 3. The block-string system is sliding in the -x direction at constant speed when, at time t=0, a time-dependent tension force of magnitude T is applied in the +x direction to string 1. For times  $t \ge 0$ , the velocity vector of any point on the block-string system is described by the function

$$\vec{v}(t) = (\alpha t^2 - \beta)\hat{i}$$

where  $\alpha$  and  $\beta$  are positive constants. For this problem, you can assume that every part of the block-string system moves together and that the strings connecting the blocks are stretched out to their maximum lengths for all times  $t \ge 0$ .

Figure 1



**Part A (10 points):** Determine the acceleration vector of any point on the blockstring system as a function of time. Express your answer in terms of t,  $\alpha$ , and  $\beta$ .

$$\vec{a}(t) = \frac{d\vec{v}(t)}{dt}$$

**Part B (10 points):** A specific point of the block-string system is found to pass the origin at time t = 0. Determine the position vector of this point as a function of time. Express your answer in terms of t,  $\alpha$ , and  $\beta$ .

$$\vec{\chi}(t) = \int \vec{v}(t) dt$$

$$= \left(\frac{1}{3} \alpha t^3 - \beta t + C\right) \hat{i}$$

$$\overrightarrow{x}(t) = \left(\frac{1}{3} \alpha t^3 - \beta t\right) \hat{\iota}$$

Part C (10 points): What is the tension magnitude in string 1 at the time when the block-string system is instantaneously at rest? Express your answer in terms of m,  $\alpha$ , and  $\beta$ .

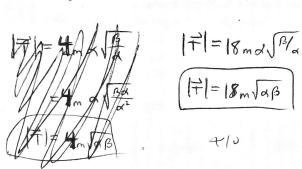
$$\vec{v}(t) = \vec{0}$$

$$\vec{0} = (\alpha t^2 - \beta) \hat{1}$$

$$\alpha t^2 - \beta = 0$$

$$t = \sqrt{\beta}$$

$$\vec{T} = m\vec{a} \rightarrow \vec{T} = m\alpha$$



Part D (10 points): What is the tension magnitude in string 2 at the time when the block-string system is instantaneously at rest? Express your answer in terms of m,  $\alpha$ , and  $\beta$ .

$$7m$$
 $T_2$ 
 $T_2$ 

$$|\overrightarrow{T_2}| = 7m(2\alpha\sqrt{B/\alpha})$$

$$|\overrightarrow{T_1}| = |4m\sqrt{\alpha}\beta|$$

218

## Problem 2 (40 points):

A daredevil wants to design a catapult that will launch him from one incline to another, as shown in Figure 2 below. Both inclines are identical, having a base length L and an angle of  $\alpha_0$  = 60°. The horizontal distance between the inclines is 2L. The daredevil initially stands on a platform at the bottom of the incline on the left. The combined mass of the daredevil and platform is  $M_1$ . The platform is connected via a rope and pulley to a vertically hanging counterweight of mass  $M_2$ . When the counterweight is released from rest, it descends and pulls the platform and daredevil up the incline. At the very top of the incline, the platform is stopped suddenly, launching the daredevil. The acceleration magnitude due to gravity is g.

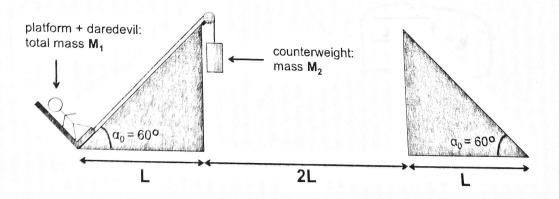
For this problem, you can assume the following:

- The daredevil is launched from the very top of the incline at the same speed that the platform attains just before it is stopped suddenly.
- The size of the platform is negligible with respect to the size of the incline, such that the distance that the platform travels can be approximated as the entire length of the incline and the height from which the daredevil is launched can be approximated as the height of the incline.
  - The friction between the platform and incline is negligible.
  - The mass of the rope and pulley and the friction of the pulley are negligible.
  - Air resistance is negligible.
  - The counterweight doesn't hit the ground before the daredevil is launched (e.g., it can keep descending into a hole in the ground).

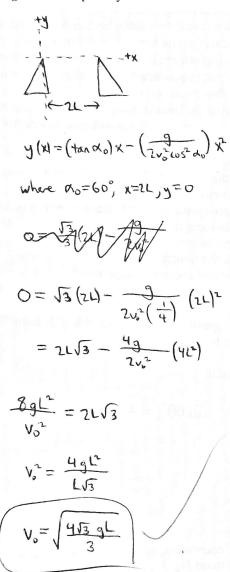
You may find the following relations helpful:

$$\sin 30^{\circ} = \frac{1}{2} \cos 30^{\circ} = \frac{\sqrt{3}}{2} \sin 60^{\circ} = \frac{\sqrt{3}}{2} \cos 60^{\circ} = \frac{1}{2}$$

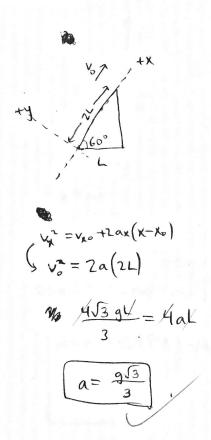
Figure 2



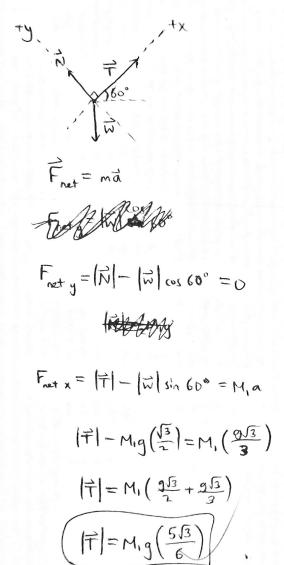
**Part A (10 points):** What is the speed with which the daredevil must be launched from the top of the incline on the left side in order to just reach the top of the incline on the right side? Express your answer in terms of L and g.



**Part B (10 points):** What acceleration magnitude must the platform have as it ascends the incline in order to attain the speed of Part A? Express your answer in terms of g.



**Part C (10 points):** What tension magnitude is required in the rope in order to achieve the acceleration magnitude from Part B? Express your answer in terms of  $M_1$  and g.





**Part D (10 points):** What counterweight mass  $M_2$  is required in order to achieve the acceleration magnitude from Part B? Express your answer in terms of  $M_1$ .



$$M_{ig}\left(\frac{5\sqrt{3}}{6}\right) - |\vec{W}| = M_{2}\left(\frac{9\sqrt{3}}{3}\right)$$

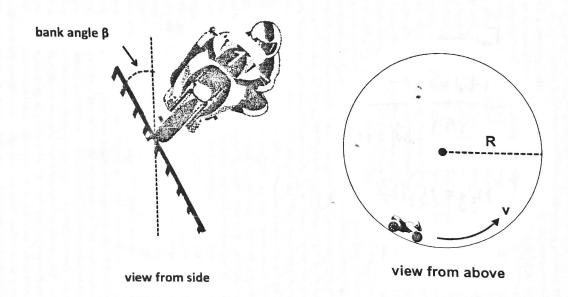
$$M_2 g = M_1 g \left( \frac{5\sqrt{3}}{6} \right) - M_2 g \left( \frac{\sqrt{3}}{3} \right)$$

$$M_2 = M_1\left(\frac{\sqrt{3}}{2}\right).$$

#### Problem 3 (20 points):

As shown in **Figure 3**, a motorcyclist rides at constant speed on the inside of a cylindrical wall banked at an angle  $\beta$  with respect to the vertical. The radius of the motorcycle's circular path is R and the coefficient of static friction between the motorcycle's tires and the wall is  $\mu_s$ . The acceleration magnitude due to gravity is g. For this problem, the sizes of the motorcyclist and motorcycle can be assumed negligible with respect to the radius of the cylindrical wall.

Figure 3



**Part A (10 points):** What is the slowest speed that the motorcyclist can maintain without skidding? Express your answer in terms of R,  $\mu_s$ , g, and  $\beta$ .

Frety = 
$$|\vec{N}| \sin \beta - \vec{w}$$
  $|\vec{N}| = \frac{mq}{\sin \beta}$   $|\vec{N}| = \frac{mq \cos \beta}{\sin \beta} - \frac{ms mq \sin \beta}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq \sin \beta}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$   $|\vec{N}| = \frac{q \cos \beta}{\sin \beta} - \frac{ms mq}{\sin \beta}$ 

**Part B (10 points):** Now assume that the banked wall shown in **Figure 3** becomes extremely icy, lowering the coefficient of static friction to zero. In order to avoid skidding up or down the wall, what amount of time must it take the motorcyclist to complete one revolution? Express your answer in terms of R, g,  $\beta$ , and fundamental constants.

$$V = \sqrt{Rg} \left( \frac{\cos \beta}{\sin \beta} \right)$$

$$\frac{2\pi R}{T} = \sqrt{Rg} \left( \frac{\cos \beta}{\sin \beta} \right)$$

$$T = \frac{2\pi R}{\sqrt{Rg} \left( \cot \beta \right)}$$

$$Rg \cot \beta$$

$$T = \frac{2\pi \sqrt{Rg} \cot \beta}{g \cot \beta}$$

$$I = \frac{2\pi \sqrt{Rg} \cot \beta}{g \cot \beta}$$

## **SCORING**

### Problem 1:

Part A: \_\_\_\_\_ / 10
Part B: \_\_\_\_\_ / 10
Part C: \_\_\_\_\_ / 10
Part D: \_\_\_\_\_ / 10
Total: \_\_\_\_\_ / 40

### **Problem 2:**

Part A: \_\_\_\_/v / 10
Part B: \_\_\_/v / 10
Part C: \_\_\_/v / 10
Part D: \_\_\_/ 10
Total: \_\_\_// 40

## Problem 3:

Part A: \_\_\_\_ < / 10 Part B: \_\_\_ / 10 Total: \_\_\_ < / 20

Total Midterm #1 Score  $\frac{94}{4}/100$