

**Q1**

5 Points

Consider the recursion relation

$$a_n = 9a_{n-1} - 20a_{n-2}$$

for  $n$  greater than or equal to 2, with the following initial conditions:

$$a_0 = 3$$

$$a_1 = 13$$

with initial conditions  $a_0 = 3$  and  $a_1 = 13$ .**Q1.1 Recurrence Relation**

1 Point

Find the roots of the auxiliary polynomial. Enter the smaller one in the following box.

**Q1.2**

1 Point

Now enter the larger of the two roots in the following box:

**Q1.3**

1 Point

Let  $r_1$  denote the smaller of the two roots of the auxiliary polynomial and let  $r_2$  denote the larger of the two roots.

We know from class that the solution to the recurrence relation subject to the initial conditions has the form  $c (r_1)^n + d (r_2)^n$ .

What is  $c$ ?

2

### Q1.4

1 Point

What is  $d$ ?

1

### Q1.5

1 Point

Use the formula you found for the solution to calculate  $a_5$  (give a numerical answer).

5173

## Q2 Graph

5 Points

Let  $G = (V, E)$  be a simple graph defined as follows: the vertex set  $V$  is the set  $\{1, 2, \dots, 13\}$ , and for any vertices  $v$  and  $w$ , there is an edge between  $v$  and  $w$  if and only if exactly one of  $v$  and  $w$  is even (and the other is odd).

### Q2.1 Graph

2.5 Points

Is  $G$  bipartite?

Yes, it is bipartite

No, it is not

**Q2.2**

2.5 Points

How many edges does  $G$  have?

42

## Quiz 5

● GRADED

**STUDENT**

David Xiong

**TOTAL POINTS**

**10 / 10 pts**

**QUESTION 1**

(no title)

**5 / 5 pts**

1.1 Recurrence Relation

1 / 1 pt

1.2 (no title)

1 / 1 pt

1.3 (no title)

1 / 1 pt

1.4 (no title)

1 / 1 pt

1.5 (no title)

1 / 1 pt

**QUESTION 2**

Graph

**5 / 5 pts**

2.1	Graph	2.5 / 2.5 pts
2.2	(no title)	2.5 / 2.5 pts