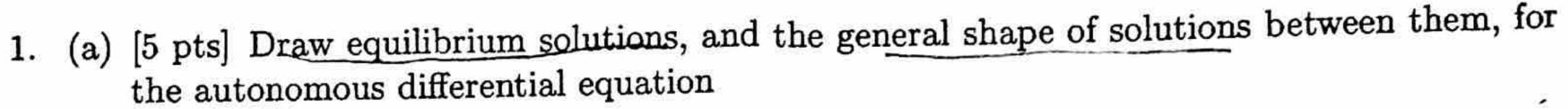
STUDENT NAME: __
STUDENT ID NUMB

Directions

Answer each question in the space provided. Please write clearly and legibly. Show all of your work—your work must both justify and clearly identify your final answer. No books, notes or calculators are allowed.

For instructor use only

Page	Points	Score
2	10	9
3	10	10
4	10	VV
5	10	(N)
Total:	40	39





phase like:

$$y' = (y^2 - 3y - 2)\sin(\pi y). = f(y)$$

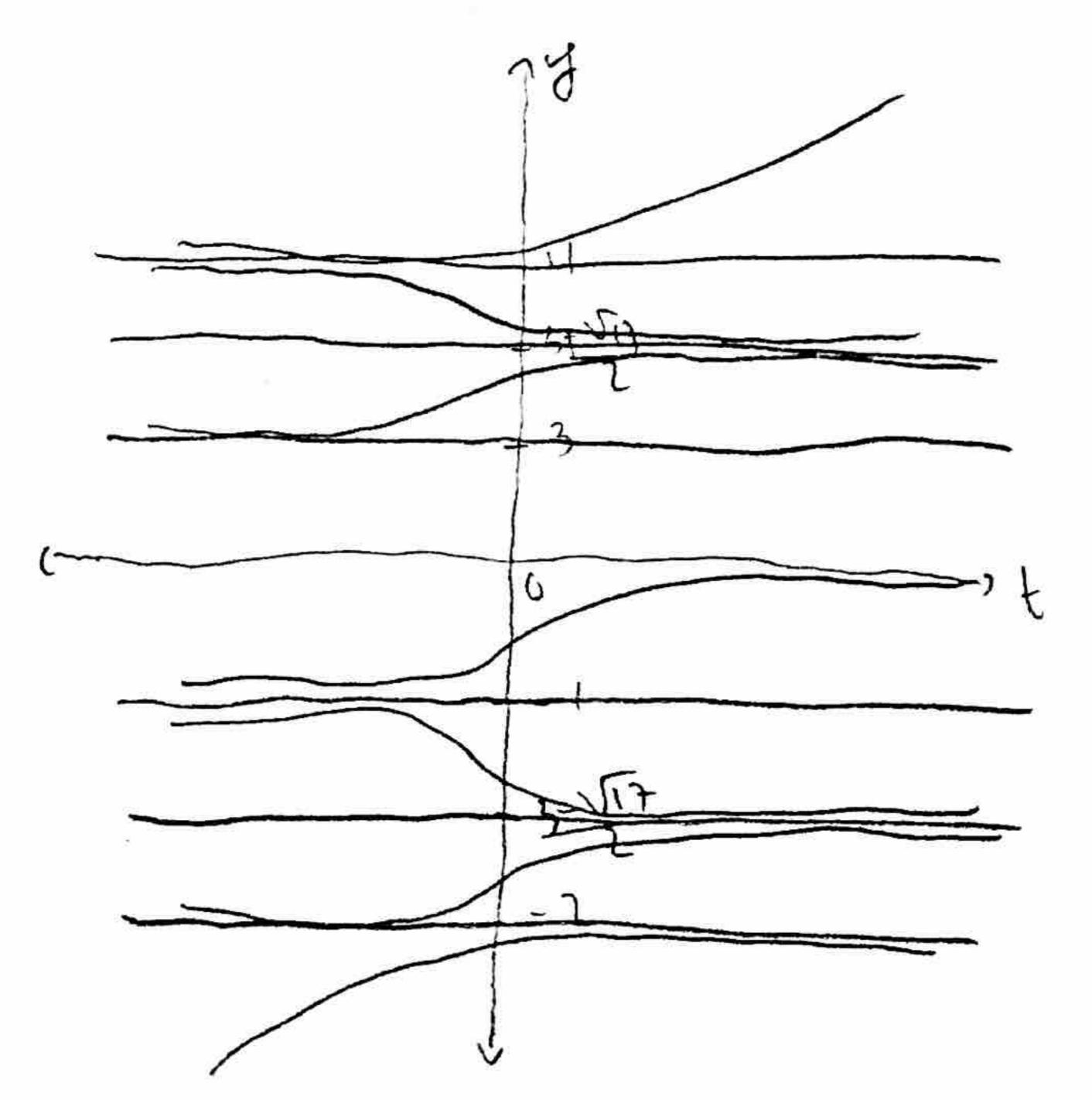
507 ~ betiter

Include at least 5 equilibrium lines near the origin.

(3.7) - 3(3.7) - 1 3.7 (1-3-7) 015 - 1 (-1)

3-VIA (CC+>>>+CCC+>>>>+CCC+>>>>+CCC+>>>>

(b) [5 pts] Describe the stability of all equilibrium points for the differential equation above. There should be some special cases, and then some statements that hold for entire families of equilibrium points.



For all y = k equilibrium solutions, if k is even and between

Setween $y = 3 \pi \sqrt{17}$ and $3 - \sqrt{17}$ we equilibrium stable

I then it is stable, if k is odd, then unstable

If $y = 3 \pi \sqrt{17}$, then if y = k, and k is even

then stable holds for it y = k.

The reverse holds for it y = k.

2. (a) [8 pts] Find the equations of motion (ie solve the initial value problem) for a mass of 2kg on a spring having spring constant $72kg/s^2$ in a liquid with damping constant 24kg/s,

(b) [2 pts] How fast is the spring moving at time t = 1?

$$x'(4) = -6e^{-6t} + 8e^{-6t} - 48te^{-6t}$$

 $x'(1) = -6e^{-6} + 8e^{-6} - 48e^{-6}$
 $2e^{-6} - 48e^{-6} = [-46e^{-6} mls]$

3. [10 pts] Find the general solution to the differential equation

$$y'' + y = (\sec^2 t)^{-}$$

79 y = e (ws bt) = wst (You will need the formula $\int \sec t dt = \ln|\sec t + \tan t|$)

variation of param?

$$y'' + y = 0$$

$$\lambda^{2} + 1 = 0$$

$$\lambda^{2} = 0 + 1i - 16 = 1$$

$$y_{1} = 0 + 1i - 16 = 1$$

$$y_{2} = 0 + 1i - 16 = 1$$

$$y_{3} = 0 + 1i - 16 = 1$$

$$y_{4} = 0 + 1i - 16 = 1$$

$$y_{5} = 0 + 1i - 16 = 1$$

$$y_{7} = 0 + 1i - 16 = 1$$

$$V_1' = -\frac{9}{9} \frac{y_L}{y_L} = -\frac{9}{9} \frac{y_L}{y_L} = -\frac{5}{9} \frac{c^2 t}{sin} t = -\frac{sin^4}{69^2 t}$$

$$V2' = .9Y1 = 9Y1 = See t cost = 1 cost = see t$$

$$V_1 = -\int \frac{\sin t}{\cos^2 t} dt = \int \frac{\sin t}{du = -\sin t} dt = 0$$

$$\int \frac{dw}{u^2} = -\int \frac{1}{u^2} dt = -\int \frac{1}{u^$$

4. [10 pts] Suppose that y_1 and y_2 are two solutions to the second order homogeneous differential equation

$$y'' + p(t)y' + q(t)y = 0.$$

Prove that the Wronskian of y_1 and y_2 , denoted W(t), satisfies its own differential equation

$$W'(t) = p(t)W(t).$$

(You cannot use the formula $W(t) = W(t_0)e^{\int p(t)dt}$ in this problem - in fact this problem is a part of the proof of that formula) Hint: Differentiate the standard formula for W, and use the fact that both y_1 and y_2 satisfy the homogeneous equation to make a substitution for the second derivatives in your empression

fact that both
$$y_1$$
 and y_2 satisfy the homogeneous equation to make a substitution for the second derivatives in your expression

 $V_1 (Y_1 / Y_2) = (Y_1, Y_2)$
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