

## Q1

2 Points

How many solutions can a system of 3 linear equations with 5 variables have? Select all that could apply.

zero

one

two

three

infinitely many

## Q2

2 Points

For which values of  $a$ ,  $b$ ,  $c$ , and  $d$  is the following augmented matrix in reduced row-echelon form?

$$\left[ \begin{array}{cccc|c} 0 & b & 3 & 1 & d \\ 0 & 0 & 0 & c & 1 \\ 0 & a & 0 & 0 & 0 \end{array} \right]$$

Answer:

$a =$

0

$b =$

1

$c =$

0

$d =$

0

### Q3

3 Points

Find a function  $f(t)$  of the form  $f(t) = ae^{3t} + be^{2t} + ce^t$  such that  $f(0) = 1$  and  $f'(0) = 1$ . Is it unique?

Show your work!

Hint: Use the given conditions  $f(0) = 1$  and  $f'(0) = 1$  to set up a system of linear equations for  $a, b, c$ .

## Q4

3 Points

Solve the following differential equation (more precisely, find the solution of the initial value problem)

$$y'(t) = t^2 \sin(2t), \quad y(0) = 1.$$

Show your work!