22S-MATH-33B-LEC-3 Midterm Exam one

JUSTIN SHEU

TOTAL POINTS

100 / 200

QUESTION 1

1 50 / 50

√ - 0 pts Correct

- 1 pts Click here to replace this description.
- 50 pts Click here to replace this description.
- 2 pts Click here to replace this description.
- 3 pts Click here to replace this description.
- 4 pts Click here to replace this description.
- 25 pts Click here to replace this description.

QUESTION 2

2 0/50

+ **50 pts** Correct: if \$\$s(t)\$\$ is the weight of salt at time \$\$t\$\$, then

\$s(t) = 80 e^{-t/25}\$\$, and the concentration is \$c(t) = $\frac{4}{5} e^{-t/25}$ \$\$

√ + 0 pts Problem not selected

+ **15 pts** \$\$s'(t) = \left(\textrm{rate in} \right) - \left(

\textrm{rate out} \right)\$\$

\$\$=0 - 4\cdot \frac{s(t)}{100}\$\$

+ 20 pts Get the general solution

\$s(t) = C \cdot e^{-t/25}\$\$

+ 15 pts Use the initial condition

\$\$80= s(0) = C\$\$ to get the particular solution

\$\$s(t) = 80 e^{-t/25},\$\$\$ so \$\$c(t) = \frac{4}{5} e^{-t/25}\$\$\$

QUESTION 3

3 50 / 50

√ - 0 pts Correct

- 50 pts (Did not select Question 3)
- 20 pts Incorrect placement of c
- 30 pts Error
- 40 pts Unsolved
- 15 pts Correct solution but did not find explicit

form (i.e. solve for y)

- 25 pts (shifting so the total points are out of 100)

QUESTION 4

4 0 / 50

- + **15 pts** Correct separation of variables and/or integrating factor.
 - + 15 pts Correct integrals.
 - + 10 pts Correctly solved for y (general solution).
- + **10 pts** Correctly used the initial condition to find the particular solution.

$\sqrt{+0}$ pts Did not choose this problem.

+ 25 pts Click here to replace this description.

University of California, Los Angeles Spring 2022

Instructor: C. Wang Date: April 22, 2022

MATH 33B: Differential Equations MIDTERM EXAM 1

Last Name	Sheu
First Name	Justin
Student ID	405773496
TA Name	Yan Tao
	QlandQ3

Last Name Shew , First Name Jushy

Student ID 405773 496

Q1

25 Points

Check whether the following differential form is closed and exact.

$$\underbrace{(2t+5y)dt+(5t-6y)dy}$$

$$\frac{\partial Q}{\partial t} = \frac{\partial}{\partial t} \left(5 + - 6 \gamma \right) = 5$$

$$\frac{2\lambda}{9b} = \frac{2\lambda}{9} \left(5 + 2\lambda \right) = 2$$

Thus, $\frac{\partial Q}{\partial t} - \frac{\partial P}{\partial y} = 5.5 = 0$, so the differential form is closed.

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Last Name	Sheu	_,First Name_	Just/n
Student ID_	405773496	_	
Q2 25 Points			

A tank contains 100 gallons of brine made by dissolving 80 lb of salt in water. Pure water runs into the tank at the rate of 4 gallons/minute, and the mixture, which is kept uniform by stirring, runs out at the same rate. Find the amount of salt in the tank at any time t. Find the concentration of salt in the tank at any time t.

$$y'(t) = rate in - rate out$$

rate $in \neq t$ and $in = 0$ lbs/min

rate $in \neq t$ and $in = 0$ lbs/min

rate out = $49a$ /min $\frac{y(t)}{v(t)} = \frac{4y(t)}{100gol} = \frac{y(t)}{25}$
 $y'(t) = 0 - \frac{y(t)}{25} = -\frac{100gol}{25}$

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Student ID 405773496

Q3

25 Points

Solving the following separable differential equation (you need to give general solution in explicit form):

$$dy/dt = ty$$

$$\frac{\partial u}{\partial t} = ty$$

$$\frac{\partial v}{\partial t} = t + \partial t$$

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Student ID			
G/4 25 Points			
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the interval of exity $y'(t) + \frac{y(t)}{1-t} = 0$			

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