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• You have 5 minutes

• No calculators

• Show sufficient work

1. Consider four linearly independent vectors  $\vec{v}_1, \vec{v}_2, \vec{v}_3,$  and  $\vec{v}_4$  in  $\mathbb{R}^6$ . Find

$$\text{rref} \begin{bmatrix} | & | & | & | \\ \vec{v}_1 & \vec{v}_2 & \vec{v}_3 & \vec{v}_4 \\ | & | & | & | \end{bmatrix}.$$

IF the vectors are linearly independent,

$$\text{rref} \begin{bmatrix} | & | & | & | \\ \vec{v}_1 & \vec{v}_2 & \vec{v}_3 & \vec{v}_4 \\ | & | & | & | \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Because, rref of a matrix of linearly independent vectors will have a rank equal to the number of these linearly independent vectors.