1. (a) (3 points) Find the unit vector which points in the same direction as (1,2,3).

let 
$$v = (1,2,3)$$
  
 $||v|| = \sqrt{||^2 + 2|^2 + 3|^2} = \sqrt{||y||}$ 

(b) (5 points) Let v, w be vectors in  $\mathbb{R}^3$  such that ||v|| = 2, ||w|| = 3 and such that  $v \cdot w = 0$ . Find ||v + w||.

V. w = 0, therefore v and w are orthogonal, so 
$$||v||^2 + ||w||^2 = ||v+w||^2$$

(c) (5 points) Let v = (1, 2, 0) and let w = (2, 1, 3). Write w as the sum of two vectors r, s, so that w = r + s, and such that r is parallel to v, and s is perpendicular to v.

$$S = (7.1,3) - (4,4,0) = (6,-3,3)$$

2. (10 points) Find the angle between the planes x + 2y + z = 1 and x - y - 2z = 0. Then, find a parametrization for the line of intersection of these planes.

(10 points) Find the angle both find a parametrization for the line of intersection of these planes.

(1) points Find the angle both find a parametrization for the line of intersection of these planes.

(1) 
$$x + 2y + 2 = 1$$

(1)  $x - 2y + 2 = 1$ 

(1)  $x - 2y - 2 = 0$ 

(2)  $x - 2y - 2 = 0$ 

(3)  $x - 2y - 2 = 0$ 

(4)  $x - 2y - 2 = 0$ 

(5)  $x - 2y - 2 = 0$ 

(6)  $x - 2y - 2 = 0$ 

(7)  $x - 2y - 2 = 0$ 

(8)  $x - 2y - 2 = 0$ 

(9)  $x - 2y - 2 = 0$ 

(1)  $x - 2y - 2 = 0$ 

(2)  $x - 2y - 2 = 0$ 

(3)  $x - 2y - 2 = 0$ 

(4)  $x - 2y - 2 = 0$ 

(5)  $x - 2y - 2 = 0$ 

(6)  $x - 2y - 2 = 0$ 

(7)  $x - 2y - 2 = 0$ 

(8)  $x - 2y - 2 = 0$ 

(9)  $x - 2y - 2 = 0$ 

(1)  $x - 2y - 2 = 0$ 

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(4)  $x - 2y - 2 = 0$ 

(5)  $x - 2y - 2 = 0$ 

(6)  $x - 2y - 2 = 0$ 

(7)  $x - 2y - 2 = 0$ 

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(7)  $x - 2y - 2 = 0$ 

(8)  $x - 2y - 2 = 0$ 

(9)  $x - 2y - 2 = 0$ 

(1)  $x - 2y - 2 = 0$ 

(2)  $x - 2y - 2 = 0$ 

(3)  $x - 2y - 2 = 0$ 

(4)  $x - 2y - 2 = 0$ 

(5)  $x - 2y - 2$ 

$$z = -1$$

$$x = 1 - 2(\frac{4}{3}) - (-1)$$

$$x = 1 - \frac{8}{3} + 1$$

$$x = 2 - \frac{8}{3}$$

$$x = -\frac{2}{3}$$

$$\left(-\frac{2}{3}, \frac{1}{3}, -1\right)$$
 lies in the intersection

$$(-\frac{2}{3}, \frac{1}{3}, -1)$$
 lies in the intersection 
$$(-\frac{2}{3}, \frac{1}{3}, -1)$$
 lies in the intersection between the two planes.
$$(-\frac{2}{3}, \frac{1}{3}, -1)$$
 lies in the intersection between the two planes.

3. In each of the following items, an equation is listed. This equation describes a quadric surface in  $\mathbb{R}^3$ . That is, each equation describes a set of points (x,y,z) in three-dimensional Euclidean space. For each such equation, identify the type of surface to which the equation corresponds. You can choose from the following labels: Paraboloid, Hyperboloid, Cone, Ellipsoid, Cylinder. You do not need to show any work in this section. No partial credit will be given in this section.

(a) (2 points)  $2x^2 + 3y^2 = 1 - z^2$ PARABOLOID HYPERBOLOID CONE ELLIPSOID CYLINDER (circle one)

(b) (2 points)  $z^2 - 2y^2 + 10z^2 = 0$  |  $|z^2 - 2y^2 = 0$  | PARABOLOID HYPERBOLOID CONE ELLIPSOID CYLINDER (circle one)

(c) (2 points)  $2x^2 + 3y^2 = z^2$ PARABOLOID HYPERBOLOID CONE ELLIPSOID CYLINDER (circle one)

- (d) (2 points)  $z^2 + 100y^2 = 100$ PARABOLOID HYPERBOLOID CONE ELLIPSOID CYLINDER (circle one)
- (e) (2 points)  $y^2 + 4z^2 = x^2 + 1$ PARABOLOID HYPERBOLOID CONE ELLIPSOID CYLINDER (circle one)
- (f) (2 points)  $4x = y^2 + z^2/4$  PARABOLOID HYPERBOLOID CONE ELLIPSOID CYLINDER (circle one)

4. (10 points) Consider the following three points in  $\mathbb{R}^5$ :

$$(5,3,2,3,1), (5,3,0,1,2), (5,3,0,1,0).$$

Consider the triangle which has these three points as its vertices. Find the area of this triangle.

let 
$$P = (2,3,1)$$
  
let  $Q = (0,1,2)$   
let  $P = (0,1,0)$   
 $PQ = (0,1,2) - (2,3,1) = (-2,-2,1)$   
 $QP = (0,1,0) - (0,1,2) = (0,0,-2)$ 



5. (10 points) Compute:

$$\left[ (1,2,1) \times \left( \left[ (1,2,1) \times (3,4,1) \right] \times \left[ (1,2,1) \times (5,7,9) \right] \right) \right] \times (4,10,3).$$

Hint: There is a way to do this problem without doing any computations.

Make sure to justify your answer. (If you compute all of these cross products explicitly, and you get the wrong answer, you will get at most half credit.)