

ECE3 Spring 2020

Name

Family (Last) Name

Name

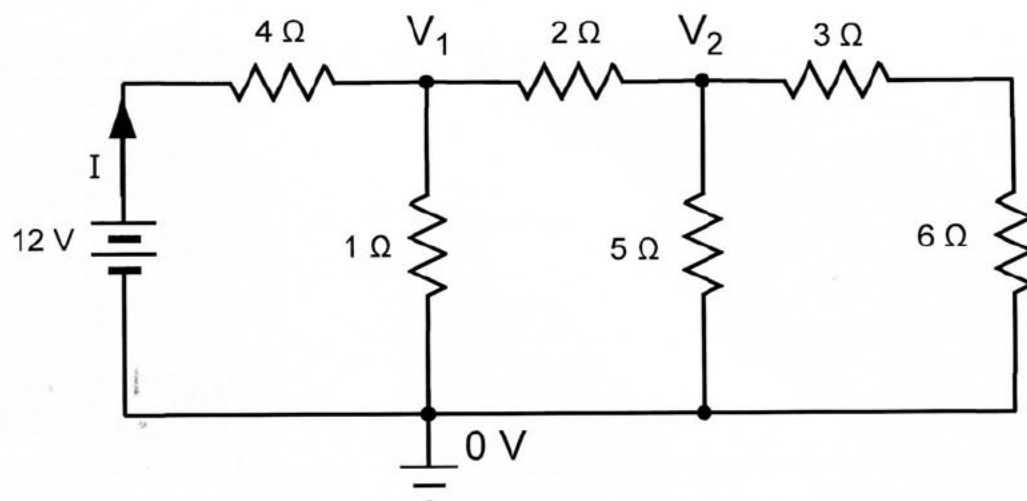
Final Exam

UID

**DO NOT OPEN UNTIL
INSTRUCTED TO DO SO.**

- We will copy some graded exam papers for archival purposes!
- Put your name in the blank on EVERY page.
- Show your setup.
- Circle your answers.
- Add notes to help the graders determine your intentions.

Problem	Value	Score	Problem	Value	Score
1a	1		4	25	
1b	1		5	15	
1c	1		6a	5	
1d	1		6b	5	
1e	4		7a	8	
2	20		7b	8	
3	6		TOTAL	100	95



1

•IF YOU ARE PRINTING THE TEST AND WRITING ON IT, USE THE NEXT PAGE FOR ANSWERS.

- Using Node Voltage Analysis, write an Ohm's Law expression (in terms of V_1 and V_2) for the current going through the $4\ \Omega$ resistor.
- Under the same assumption, write an Ohm's Law expression (in terms of V_1 and V_2) for the current through the $1\ \Omega$ resistor.
- Continuing, write an expression (in terms of V_1 and V_2) for the current through the $2\ \Omega$ resistor.
- Now, combine the answers to 1a,b,c into a KCL equation for Node 1.
- Write the KCL equation for Node 2 (in terms of V_1 and V_2).

2

You now have 2 equations in 2 unknowns. Solve them for V_1 and V_2 .

3

Now that you know V_1 , you can compute I .

USE THIS PAGE FOR CALCULATIONS

$$1.) a. V_1 - 12 = I_4(4)$$

$$b. V_1 - 0 = I_1(1)$$

$$V_1 = I_1$$

$$c. V_1 - V_2 = I_2(2)$$

$$d. I_4 + I_1 + I_2 = 0$$

$$\frac{V_1 - 12}{4} + V_1 + \frac{V_1 - V_2}{2} = 0$$

$$e. \frac{V_2 - V_1}{2} + \frac{V_2}{5} + \frac{V_2}{9} = 0$$

$$2.) 4 \left(\frac{V_1 - 12}{4} + V_1 + \frac{V_1 - V_2}{2} \right) = 0$$

$$V_1 - 12 + 4V_1 + 2V_1 - 2V_2 = 0$$

$$\Rightarrow V_1 = 2V_2 + 12$$

$$V_1 = \frac{2V_2 + 12}{1}$$

$$V_1 = \frac{2 \cdot \frac{540}{421} + 12}{1}$$

$$V_1 = \frac{6132}{2947}$$

$$V_1 = \frac{876}{421} \text{ V} \approx 2.08 \text{ V}$$

$$3.) I = \frac{12 - V_1}{4}$$

$$I = \frac{12 - \frac{876}{421}}{4}$$

$$I = \frac{1044}{421} \text{ A} \approx 2.48 \text{ A}$$

$$\left(\frac{V_2 - \frac{2V_2 + 12}{2}}{2} + \frac{V_2}{5} + \frac{V_2}{9} \right) = 0$$

$$c30 \left(\frac{5V_2 - 12}{14} + \frac{V_2}{5} + \frac{V_2}{9} \right) = 0$$

$$225V_2 - 540 + 126V_2 + 170 = 0$$

$$421V_2 = 540$$

$$V_2 = \frac{540}{421} \text{ V} \approx 1.28 \text{ V}$$

4

Find V_x . V_x :

$$-I_2 - 3I_2 + \frac{V_x}{3} = 0$$

$$I_2 = \frac{V_x}{12}$$

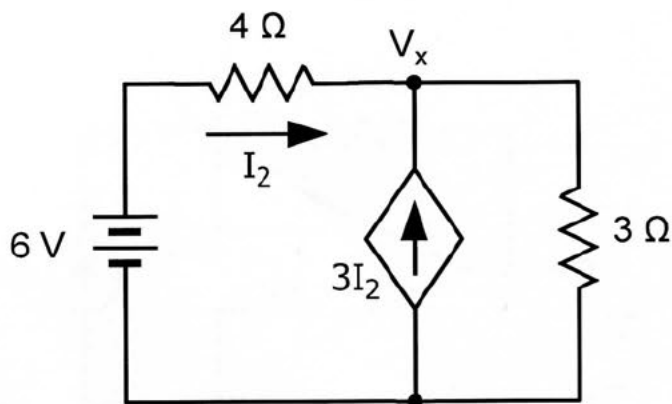
$$V_x = 12I_2$$

$$V_x = 12\left(\frac{6 - V_x}{4}\right)$$

$$V_x = 18 - 3V_x$$

$$4V_x = 18$$

$$V_x = \frac{9}{2} = 4.5 \text{ V}$$



$$6 - V_x = I_2 \cdot 4$$

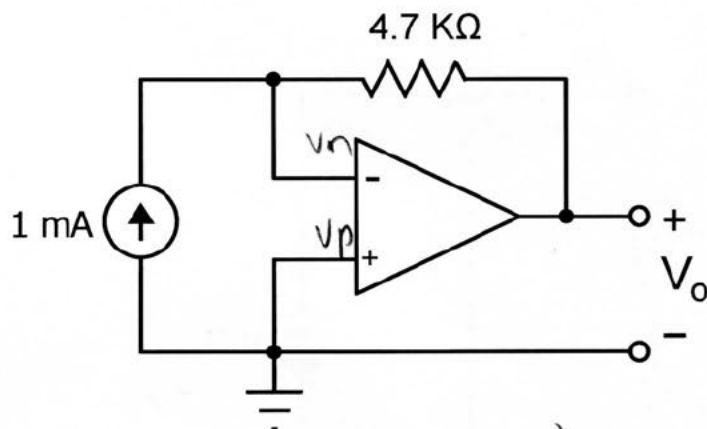
$$I_2 = \frac{6 - V_x}{4}$$

5

Find V_o .

$$0 - V_o = \frac{0.001}{4700}$$

$$V_o \approx 0.21 \mu\text{V}$$

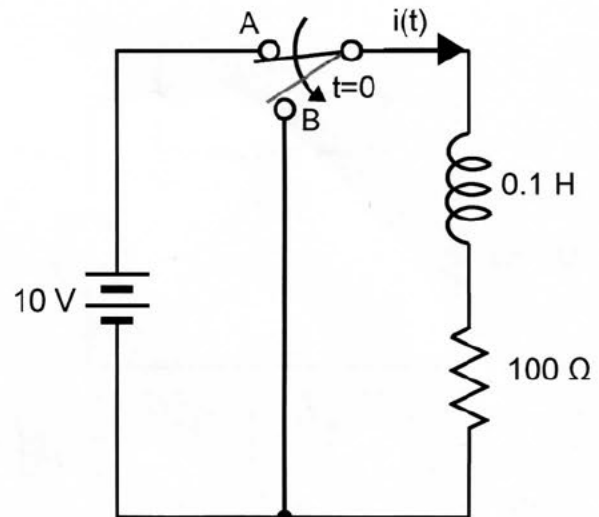


$$v_n = v_p = 0$$
$$i_n = 0 = i_p$$

6

The switch has been in position A for a Long Time. At $t=0$, it moves instantaneously from A to B. Find the trajectory of the current $i(t)$.

- What is the current $i(0^-)$?
- What is the current $i(0^+)$?



a. The inductor opposes changes in current, so $i(0^-) = i(0^+)$

$$a. i(0^-) = \frac{10}{100} = \boxed{0.1A}$$

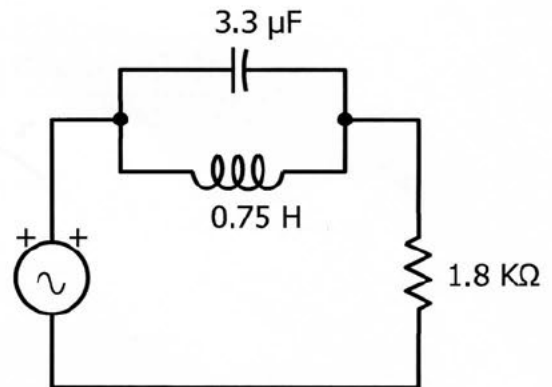
$$b. i(0^+) = i(0^-) = \frac{10}{100} = \boxed{0.1A}$$

7

In this circuit, $\omega = 6283$ rad/s.

a. Find Z_L .

b. Find Z_C .



$$a. Z_L = j\omega L$$

$$Z_L = j(6283)(0.75)$$

$$Z_L \approx 4712.25j \Omega$$

$$b. Z_C = -j \frac{1}{\omega C}$$

$$Z_C = -j \frac{1}{(6283)(3.3E-6)}$$

$$Z_C \approx -48.23j \Omega$$