

EEM16 Quiz #1

AURORA BEVERLEY YEH

TOTAL POINTS

18 / 20

QUESTION 1

1 (a)-(c) 7.5 / 7.5

- ✓ - 0 pts (a) Correct
- ✓ - 0 pts (b) Correct
 - 1 pts (b) incorrect literals
 - 1 pts (b) not fully
- ✓ - 0 pts (c) Correct
 - 1 pts (c) N instead of $\sim N$
 - 1 pts (c) not fully
 - 1 pts (c) not conjunctive
 - 0.5 pts (c) error in literals

(f) more factoring possible

QUESTION 2

2 (d)-(h) 10.5 / 12.5

- 0 pts (d) Correct
 - 1 pts (d) missing/incorrect prime implicant
 - 1.5 pts (d) incorrect Kmap
 - ✓ - 1 pts (d) missing or incorrect essential
 - 0 pts (e) Correct
 - ✓ - 0.5 pts (e) too many terms
 - 1.5 pts (e) incorrect term
 - ✓ - 0 pts (f) Correct
 - 2.5 pts (f) incorrect factoring
 - ✓ - 0 pts (g) Correct
 - 0.5 pts (g) excess or lack of factoring
 - 0.5 pts (g) partial application of DeMorgan
 - 2.5 pts (g) incorrect DeMorgan
 - ✓ - 0 pts (h) Correct
 - 1 pts (h) missing or extra input/internal inversions
 - 1.5 pts (h) incomplete erroneous design
 - 0.5 pts (h) missing output inversion
 - 0.5 pts (h) too many inversions (not optimized)
 - 2 pts (h) not NAND
 - 2.5 pts (h) incorrect
- 0.5 Point adjustment**

Quiz #1

Name (Last, First): Yeh, Aurora

Student Id #: 305110110

Do not start working until instructed to do so.

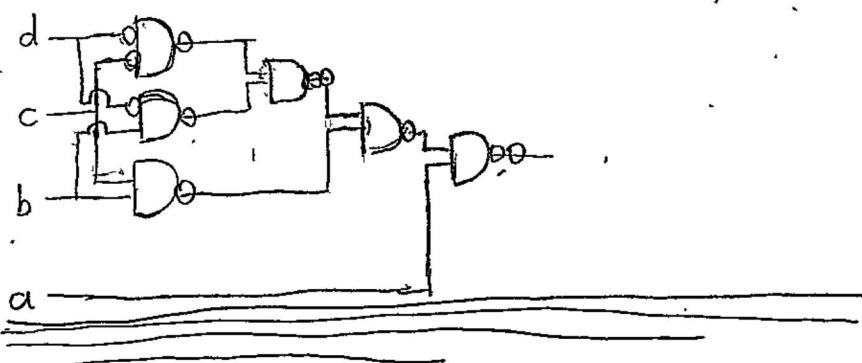
1. You must answer in the space provided for answers after every question. We will ignore answers written anywhere else in the booklet. All pages in this booklet must be accounted for otherwise it will not be graded.
2. This quiz is closed book/notes.
3. You may not use any electronic device.

Following table to be filled by course staff only.

	Maximum Score	Your Score
TOTAL	20	

$$\begin{aligned} T[0] &= a \\ T[1] &= b \\ T[2] &= c \\ T[3] &= d \end{aligned}$$

$$\begin{aligned} \neg a \vee (\neg d \wedge \neg c) \vee (\neg d \wedge b) \vee (c \wedge b) \\ \cancel{\neg a \wedge (\neg (d \vee c) \vee \neg (d \wedge b) \vee \neg (c \vee \neg b))} \\ \therefore \quad \quad \quad \end{aligned}$$



$$(((\overline{T[3]} \wedge \overline{T[2]}) \wedge (\overline{T[3]} \wedge T[1])) \wedge (T[2] \wedge T[1])) \wedge (T[0])$$

$\Sigma \Sigma$

$$\neg ((\neg (\neg d \wedge \neg c) \wedge \neg (\neg d \wedge b)) \wedge \neg (b \wedge c)) \wedge a$$

$$((\neg d \wedge \neg c) \vee (\neg d \wedge b) \vee (b \wedge c)) \wedge a \quad \text{yea that's the same}$$

Recall from Homework #1 where we have the 4 DNA nucleotides of G, C, T, and A. Let us represent them using 4-bit thermometer code, $t[3:0]$, where G=4'b0001, C=4'b0011, T=4'b0111, and A=4'b1111. A logic is used to indicate whether the input $t[3:0]$ corresponds to a nucleotide. The output of this logic is N.

(a) Complete the truth table for N.

T[3]	T[2]	T[1]	T[0]	N
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

(b) Write the expression for N in Fully-Disjunctive Normal Form.

$$N = \{ (\neg T[3] \wedge \neg T[2] \wedge \neg T[1] \wedge T[0]), (\neg T[3] \wedge \neg T[2] \wedge T[1] \wedge \neg T[0]), \\ (\neg T[3] \wedge T[2] \wedge \neg T[1] \wedge \neg T[0]), (T[3] \wedge \neg T[2] \wedge \neg T[1] \wedge \neg T[0]) \}$$

(c) Write the expression for $\neg N$ in Fully-Conjunctive Normal Form

$$\neg N = \{ (\neg T[3] \vee T[2] \vee T[1] \vee \neg T[0]) \wedge (T[3] \vee \neg T[2] \vee \neg T[1] \vee \neg T[0]), \\ (\neg T[3] \vee \neg T[2] \vee \neg T[1] \vee \neg T[0]) \wedge (\neg T[3] \vee \neg T[2] \vee \neg T[1] \vee \neg T[0]) \}$$

- (d) Draw the Karnaugh Map of the Truth Table. Circle the prime implicants, indicate which one(s) are essential (if any).

		T[2]	T[3]		
		T[3:2]	T[3]		
		00	01	11	10
T[1:0]	00	0	0	0	0
	01	1	0	0	0
	11	1	1	1	0
	10	0	0	0	0

All are
essential

- (e) Using the K-map in (d) as the minimized 2-level logic, write the sum-of-product expression using the fewest number of terms and literals.

$$N = (\sim T[3] \wedge \sim T[2] \wedge T[0]) \vee (\sim T[3] \wedge T[1] \wedge T[0]) \vee (T[2] \wedge T[1] \wedge T[0])$$

- (f) Can you do better (reduce the number of literals), by using Boolean properties? If so, write the expression and indicate which property you used.

$$N = T[0] \wedge (\sim T[3] \wedge \sim T[2]) \vee (\sim T[3] \wedge T[1]) \vee (T[2] \wedge T[1])$$

Property: factoring

- (g) Use DeMorgan's theorem and write the inverse of the function in (f).

$$\sim N = \sim T[0] \vee ((T[3] \vee T[2]) \wedge (T[3] \vee \sim T[1]) \wedge (\sim T[2] \vee \sim T[1]))$$

- (h) Show a combinational circuit that implements N from (f) (with T[3:0] as inputs) using only 2-input NAND gates.

This is a mess...

