

Problem 1 (20 points)

a) $(25)_{11} = (x)_y$

Find base y , such that the number of non-leading zeros in x is maximum.
if base is small, need more digits

Example:

The number of non-leading zeros in 10021 is 2.
 The number of non-leading zeros in 204003 is 3.

b) $(A1965321)_{16} = (a)_8$
 Find the value for a .

a) $(25)_{11} = (5+2\alpha)_{10} = (27)_{10}$

$(27)_{10} =$

$(\frac{1}{16} \frac{1}{8} \frac{0}{4} \frac{1}{2} \frac{1}{1})_2 \rightarrow 1$

$24 \cdot 4 = 28$

$\frac{1}{27} \frac{0}{9} \frac{0}{3} \frac{0}{1} \rightarrow \boxed{3} = y$
 $\frac{0}{64} \frac{1}{16} \frac{2}{4} \frac{3}{1}$
10

b) $A1965321_{16} =$

A	1	9	6	5	3	2	1
01010	0001	11001	0110	0101	0011	0010	0001
2	4	4	5	4	5	1	4
1111	1111	1111	1111	1111	1111	1111	1111

$16 = 4 \text{ bits}$
 $8 = 3 \text{ bits}$

10

$a = 24145451441$

$1+2+4+8=15$

12	4	1	4	5	4	5	1	4	4	1
010	100	001	100	101	100	101	001	100	100	001
0	A	1	9	6	5	5	3	2	2	1

10

Problem 5 (20 points)

NAND NOR

Find all the 2 input gates which form universal sets by itself (Universal set with only one gate).
You can use constants 0 and 1.

NAND

a	b	NAND
0	0	1
0	1	1
1	0	1
1	1	0

NOT: $a' = \text{NAND}(a, a)$ (1, 0)

AND: $ab = \text{NAND}(\text{NAND}(a, b), \text{NAND}(a, b))$
OR: $a+b = (a'b')'$

a	b	f	f(a', b')	f(a', b)
0	0	1	1	1
0	1	0	1	1
1	0	1	0	1
1	1	1	1	0

NOT: $a' = \text{NOR}(a, 0)$

OR: $a+b = (\text{NOR}(a, b))'$
AND: $ab = (a+b)'$

NOT: $a' = f(a, 0)$
 $f(a', b) \rightarrow \text{NAND} \& \{\text{NAND}\}$
is universal so f is univ.

a	b	NOR
0	0	1
0	1	0
1	0	0
1	1	0

OTHERS:

a	b	f	g	h	i	j	k
0	0	0	0	0	1	1	1
0	1	1	0	0	1	0	0
1	0	0	1	0	0	1	0
1	1	0	0	1	0	0	1

a	b	h
0	0	0
0	1	1
1	0	0
1	1	0

$h(a, b') \leftrightarrow \text{NOR} \{ \text{NOR} \}$ is univ
so h is univ

a	b	g
0	0	1
0	1	1
1	0	0
1	1	1

AND, XOR, OR are not
OR: $a+b = g(a, a')$
OR: $a+b = g(a', b)$

NOT: $g(a, a')$
OR: $g(a', b)$

{OR, NOT} is universal so g is universal

a	b	j
0	0	0
0	1	0
1	0	1
1	1	0

$j(a', b) \leftrightarrow \text{NOR}$. {NOR} is univ
j is univ.

a	b	k	k(a', b')
0	0	0	1
0	1	1	1
1	0	1	1
1	1	1	0

ok

Problem 3 (20 points)

For a K-map, M denotes the number of prime implicants of the K-map, and N denotes the number of essential prime implicants of the K-map. Draw a 4×4 K-map that has the largest value of $P = M - N$ among all the 4×4 K-maps. For example, in the following 4×4 K-map, $M = 3$, $N = 2$, $P = M - N = 1$

	x_0				
	0	0	0	0	
	1	1	0	0	x_2
x_3	1	1	1	0	
	0	0	1	0	
	x_1				

	x_3/x_2			
x_1/x_0	1	0	1	1
	1	1	1	0
	0	1	0	0
	1	1	1	0

	x_3/x_2			
x_1/x_0	1	0	1	1
	1	1	1	0
	0	1	0	0
	1	1	1	0

$$M = 12$$

$$N = 0$$

$$P = 12$$

20

0

Problem 2 (20 points)

Create a state transition table that has 8 states, which satisfies the following conditions:

- 1) After minimization, it should have only 3 states.
- 2) Some states which are 2-equivalent are not 3-equivalent.

states which
are diff. if you
apply any input of
length 2

