Physics 1C Spring 2017 Mid-term Exam 2 May 23, 2017

Time Limit: 90 Minutes

#### Exam Notes:

- This is a closed books, closed notes exam. No cheat sheets, please!
- Show all work, clearly and in order. Circle or otherwise indicate your final answers.
- Make sure to include units in your answers, when numerical values are given.
- Always take a few moments to double-check that your responses make sense.
- Good luck!

Grade Table (for grader use only)

Part	Points	Score
À	16	14
В	14	12
C	12	12
D	14	12
E	14	11

6

# Potentially useful equations and constants:

Maxwell's equations:

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0} \ , \quad \oint \vec{B} \cdot d\vec{A} = 0 \ , \quad \oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt} \ , \quad \oint \vec{B} \cdot d\vec{l} = \mu_0 I + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$$

Energy in capacitor:  $\frac{Q^2}{2C}$ , Energy in inductor:  $\frac{1}{2}LI^2$ , Inductance:  $L = \frac{\Phi_B}{i}$ 

L-R and L-C circuit in series: 
$$\tau = \frac{L}{R}$$
,  $\omega_0 = \sqrt{\frac{1}{LC}}$ 

L-R-C circuit in series: 
$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$
,  $\tan \phi = \frac{X_L - X_C}{R}$ 

Speed of light in vacuum: 
$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = 3 \times 10^8 \text{ m/s}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2 , \ \mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$$

Poynting vector and Intensity: 
$$\vec{S} = \frac{\vec{E} \times \vec{B}}{\mu_0}$$
,  $I = S_{avg}$ 

increases

### Part A

- 1. (2 points) Starting from zero, an electric current is established in a circuit made of a battery of emf  $\mathcal{E}$ , a resistor of resistance R and an inductor of inductance L. The electric current eventually reaches its steady-state value. What would be the effect of using an inductor with a larger inductance in this circuit?
  - A. The steady-state value of the current would be larger, but it would take the same amount of time to reach it.
  - B. The steady-state value of the current would be the same, but it would take more time to reach it.
  - C. The steady-state value of the current would be the same, but it would take the same amount of time to reach it.
  - D. The steady-state value of the current would be larger, but it would take more time to reach it.
  - E. The steady-state value of the current would be the same, but it would take less time to reach it.
- 2. (2 points) A capacitor, initially charged, and an inductor form an L-C circuit. When the electric current in the circuit is equal to zero how much energy is stored on each device?
  - A. Inductor: zero energy. Capacitor: zero energy
  - B. Inductor: Half of the maximum energy. Capacitor: Half of the maximum energy
  - Q. Inductor: maximum energy. Capacitor: zero energy
  - D. Inductor: zero energy. Capacitor: maximum energy
  - E. Inductor: maximum energy. Capacitor: maximum energy
- 3. (2 points) The average energy dissipated in an inductor, when part of a series R-L-C only R dissipates
  - (A.) zero.
  - B. proportional to the inductance.
  - C. proportional to both the inductance and frequency.
  - D. proportional to the frequency.
  - E. none of the above.

- 4. (2 points) A 12V DC battery is connected to the primary coil of a transformer. If the primary coil consists of 5 turns, the voltage across the secondary coil with 10 turns is:

B. equal to 12V C. less than 12V

VI NZ		0.1-1/
$12 = \frac{5}{10}$	= 1/2	24=4

5. (2 points) An electric field is created by a(n) \_\_\_\_\_, and an electromagnetic wave is generated by  $\hat{a}(n)$  \_\_\_\_\_.

K. static charge / constant current

B. static charge / constant magnetic field

C. changing magnetic field / static charge

D/static charge / accelerating charge

E. constant magnet / accelerating charge

6. (2 points) Which one of the following lists is a correct representation of electromagnetic waves from longer wavelength to shorter wavelength?

A. radio waves, infrared, microwaves, UV, visible, X-rays, gamma rays

B. radio waves, UV, X-rays, microwaves, infrared, visible, gamma rays

C. radio waves, microwaves, visible, X-rays, infrared, UV, gamma rays

D) radio waves, microwaves, infrared, visible, UV, X-rays, gamma rays

E. radio waves, infrared, X-rays, microwaves, UV, visible, gamma rays

7. (2 points) When light goes from one material into another material having a higher index of refraction,

A. its speed, wavelength, and frequency all decrease.

B) its speed and wavelength decrease, but its frequency stays the same.

Z. its speed decreases but its wavelength and frequency both increase.

D. its speed decreases but its frequency and wavelength stay the same.

E. its speed increases, its wavelength decreases, and its frequency stays the same.

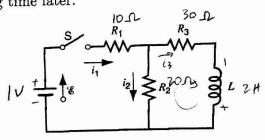
8. (2 points) A ray of light traveling in a material of index of refraction  $n_1$  strikes the boundary with another transparent material of index of refraction  $n_2$ . If there is no transmitted ray and all of the light intensity is reflected, what can you conclude about the indices of refraction of these two materials?

A. 
$$n_1 \ge n_2$$
B.  $n_1 > n_2$ 
C.  $n_1 = n_2$ 
D.  $n_1 \le n_2$ 

$$\begin{array}{c} A. & n_1 \geq n_2 \\ \hline B. & n_1 > n_2 \\ \hline C. & n_1 = n_2 \\ \hline D. & n_1 \leq n_2 \\ \hline E. & n_1 < n_2 \\ \end{array} \quad \text{water} \rightarrow \begin{array}{c} n_1 \\ \hline 0 \\ \hline \end{array}$$

### Part B

- 1. (6 points) At t=0, let  $Q=Q_0$ , and I=0 in an LC circuit composed of only an inductor and a capacitor.
  - 2 (a) (3 points) At the first moment when the energy is shared equally by the inductor and the capacitor, what is the charge on the capacitor?
  - $\beta$ (b) (3 points) How much time has elapsed in terms of the period T?
- 2. (8 points) In the figure below,  $\mathcal{E}=1$  V,  $R_1=10$   $\Omega$ ,  $R_2=20$   $\Omega$ ,  $R_3=30$   $\Omega$ , and L=2 H. Find the values of  $i_1$ ,  $i_2$ 
  - $\mathcal{Z}(a)$  (2 points) immediately after switch S is closed,
  - ∠(b) (2 points) a long time later,
  - $_{\text{\tiny $V$}}$  (c) (2 points) immediately after switch S is opened again,
  - 7 (d) (2 points) a long time later.



$$(1/a) t=0, Q=Q_0, 1=0$$

$$1/a t=0, Q=Q_0, Q=Q$$

$$Q = If(c)$$

$$Q =$$

$$\begin{aligned}
& \{-iR_1 - iR_2 = 0 \\
& 1 - i(10 + 20) = 0
\end{aligned}$$

$$30i = 1$$

$$(b) i_1 = i_2 + i_3$$

$$i_2R_2 - i_3R_3 = 0$$

$$\{-i_1R_1 - i_2R_2 = 0
\end{aligned}$$

$$1 - 10i_1 - 20i_2 = 0$$

$$1 - 10(i_2 + i_3) - 20i_2 = 0$$

$$1 - 20i_3 = 0$$

$$1 - 20i_3 = 0$$

in= = + 3

(a) i,=i2

(Extra Space)

(c) inductor is source now

$$e^{t=0^{+}}$$
,  $V=LI^{2}$ 
 $e^{t=0^{+}}$ ,  $V=LI$ 

Ldi = 
$$i(P_2 + P_3)$$
 $like 1V$  source

$$like 1V$$
 source

Part C

- 1. (12 points) In a certain *RLC* circuit, operating at 60 Hz, the maximum voltage across the inductor is twice the maximum voltage across the resistor, while the maximum voltage across the capacitor is the same as the maximum voltage across the resistor.
  - (a) (4 points) What is the phase relationship between the voltage across the *RLC* circuit and the current running through it?
  - (b) (4 points) If the AC source is actually a US wall power plug ( $V_{rms} = 120 \text{ V}$ ), what should be the circuit's resistance in order to obtain a maximum current of 300 mA?
- 2. (4 points) In a certain RLC circuit, when the AC voltage source has a particular angular frequency  $\omega$ , the peak voltage across the inductor is 6 times greater that the peak voltage across the capacitor. Determine  $\omega$  in terms of the resonant frequency  $\omega_0$  of this circuit.

(a) 
$$f = 60 \text{ Hz}$$
,  $V_l = 2 \text{ VR}$ 

$$V_c = \text{VR}$$

$$V_l + \text{VR} = \frac{\text{VL-VR}}{\text{VR}} = \frac{\text{Wl-}\frac{1}{\text{WR}}}{\text{VR}}$$

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$$V_l = \frac{\text{VL-VR}}{\text{VR}}$$

$$V_l = \frac{\text{VR}}{\text{VR}} = \frac{\text{V$$

$$V_{e}V$$

$$V$$

drauit ...

- 1. (14 points) He-Ne lasers are very commonly used in physics demonstrations. They produce light of wavelength  $\sim$ 630 nm with typical electric field amplitude of  $\sim$ 1 kV/m.
  - (a) (2 points) What is the frequency of this laser beam?
  - (b) (3 points) If  $E = E_{max} \sin(kx + \omega t)$  and  $\vec{E} \parallel \hat{y}$ , what are the values of k and  $\omega$ ?
  - (c) (4 points) Write the vector equation for  $\vec{B}(\vec{r},t)$ , the magnetic field of the laser beam.
  - (d) (2 points) Does the laser beam transport any energy? If yes, in what direction?
  - (e) (3 points) What is the intensity of this laser beam?

(a) 
$$C = \lambda f$$
  
 $f = \frac{C}{\lambda} = \frac{3 \times 10^8}{630 \times 10^7} = 4.76 \times 10^{14} + 2$ 

(b) 
$$\vec{E} = E_{max} \sin(kx + \omega t) \hat{y}$$
  
 $k = \frac{2\pi}{\lambda} = \frac{2\pi}{630 \times 10^{7} m} = \frac{9.97 \times 10^{6} \frac{1}{m}}{630 \times 10^{15} \text{ rad/s}} = k$   
 $\omega = 2\pi f = 2\pi \left( 4.76 \times 10^{14} \text{Hz} \right) = 2.99 \times 10^{15} \text{ rad/s} = \omega$ 

Bo = Epc = (1x103 V/m) (3x108 M/s)  $X = r \omega s \theta$   $B_0 = F_0 C = (1x)$   $Y = r s in \theta$   $B_0 = 3 \times 10^{11} T$ 

$$\overline{B}(x,t) = (3x10''7) \sin \left[ (9.97x10'\frac{1}{m})x + (2.99x10'^{5} \text{ rad/s})t \right] \hat{2}$$

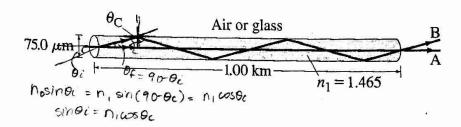
$$\cos \theta ?$$

(d) Yes, in the 
$$\hat{x}$$
-direction .+  $\frac{3}{2}$   
(e)  $1 = \frac{E_{max}^2}{2\mu_{oc}} = \frac{(1x10^3 \text{ m})^2}{2\mu_{o}(3x10^6 \text{m})} = \boxed{1326 \text{ W/m}^2} + \frac{3}{2}$ 

Part E

n, sinde = 1

Oc= 43.05°)



- 1. (14 points) Two light rays A and B of identical lasers travel down a cylindrical optical fiber of diameter  $d = 75\mu m$ , length  $\ell = 1 km$ , and index of refraction  $n_1 = 1.465$ . Ray A travels a straight path down the fiber's axis, whereas ray B propagates down the fiber by repeated reflections at the critical angle each time it impinges on the fiber's boundary.
  - (a) (2 points) What is the speed of light in the optical fiber?
  - (b) (2 points) If the light has a wavelength of 440 nm in the optical fiber, what is the actual wavelength of our laser (measured in air)?
  - (c) (6 points) Determine the extra time it takes for ray B to travel down the entire fiber in comparison with ray A, when the fiber is surrounded by air.
  - (d) (2 points) If, instead, the optical fiber is surrounded by a cylindrical glass "cladding"  $(n_2 = 1.460)$ , how do you expect the time calculated in (c) to change? Explain.
  - (e) (2 points) Would you expect your answer in (c) to be different if a green laser was used instead of a red one? Explain.

(a) 
$$n_{1} = \frac{C}{V} V = \frac{C}{n_{1}} = \frac{3 \times 10^{8} \, \text{m/s}}{1.1465}$$
 $V = 2.05 \times 10^{8} \, \text{m/s}}$ 
 $V = 2.05 \times 10^{8} \, \text{m/s}}$ 

(b)  $\lambda_{0} = 440 \times 10^{-9} \, \text{m}$ 
 $\lambda_{0} = \frac{\lambda_{0}}{n_{1}} = \frac{440 \times 10^{-9} \, \text{m}}{1.465}$ 
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 $\lambda_{0} = \frac{\lambda_{0}}{n_{1}} = \frac{\lambda_{0}}{$ 

## (Extra Space)

- (d) If  $n_2 = 1.460$  instead of  $n_2 = 1$ , the critical angle would increase and the time for ray B to reach the end would decrease and approach the time for ray A to reach the end  $\frac{1}{2}$  as  $Bc \rightarrow \frac{11}{2}$ , the ray B would approach a straight line that does not touch the "walls" of the fiber.
- of a red laser and the frequency is larger than that of the red laser. Since  $n = \frac{C}{2}$  and  $V = \lambda f$  and in a medium, wavelength Although V decreases and frequency stays the same, because the frequences also differ, the ending relocity in the medium would be the same. Just as in a racuum, both green and red lasers travel  $C = 3 \times 10^8 \, \text{m/s}$ . So no, the answer to part (c) would not differ.