

A circular parallel-plate capacitor of plate area A and plate separation d is connected across a solenoidal inductor of radius a, length x and n turns per unit length. At the instant under consideration, the capacitor has a charge q (polarity shown above), and a current I is flowing through the circuit in the direction shown. We do not know the instantaneous rate at which the current is changing, but it may be possible to infer that from the other information we know.

You will be asked to draw vectors on the sketch above. When necessary, please use ⊙ and ⊗ to unambiguously resolve the direction of any azimuthal fields.

• 1a) (10 pts) Find the magnitude of the magnetic field at points inside the capacitor, located a distance r from the symmetry axis of the capacitor. Clearly sketch and label the direction of the magnetic field, the electric field and the Poynting vector field (in the region around the capacitor) on the figure above. Discuss the consistency between the flow of energy as indicated by the Poynting vector field and the changing state of charge on the capacitor.

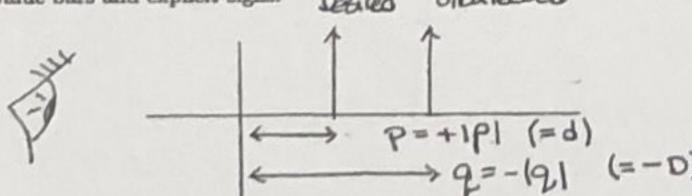
+==, î

I = dq (charging)

2) Evidence suggests that artists have used lenses and mirrors to assist them from at least as far back as the mid- to early- 1700's. While historians are likely to tell you that lenses, as a technical tool, were still many years off in the future, there are plenty of paintings from the era that portray subjects with spectacles (reading glasses). So the question is, was it possible to use reading glasses to project a (traceable) image of a physical object onto a screen?

Recall that reading glasses are used to correct for the migration of the "near point" away from the eye with age. For the following, we'll assume that a typical pair of reading glasses is designed for an uncorrected near-point that is a distance D from the lenses of the reading glasses, and a desired near-point that is a distance d from the lenses.

• 2a) (10 points) Think very carefully about this before you answer (a sketch might definitely help). If a person uses a typical pair of reading glasses to examine the fine detail on some object, where are they going to hold that object (in relation to the lens)? Where will the corresponding image appear? Will the image be real or virtual? Clearly identify the object and image distances (p and q, respectively) for this case - use absolute value bars and explicit signs.



They will hold the doject at the desired nearpoint. The image produced by the less should appear at the uncorrected nearpoint. That image will be <u>Virtual</u> as it appears on the opposite side to the energing light.

• 2b) (5 points) Find the focal length of the lens. Is it converging or diverging? Explain.

S= dD = d

D>d, f>0 => This is
a Converging lens

1b) (10 pts) Find the magnitude of the electric field at points inside the inductor, located a distance
r from the symmetry axis of the inductor. Clearly sketch and label the direction of the electric field
on the figure above.

on the figure above.

$$8\vec{\epsilon} \cdot d\vec{s} = -\frac{d\vec{\epsilon}}{dt}$$
 $E = -\frac{d}{dt}(\mu_0 \pi I \pi r^2)$
 $E = -$

1c) (10 pts) Find the magnitude of the Poynting vector at the boundary of the inductor. Clearly
sketch and label the direction of the Poynting vector field on the diagram above. Find the rate at
which energy is entering or leaving the inductor, and discuss the result.

2c) (10 points) Let's see if we can project an image of a physical object on a screen using this lens. If
the object is located a distance L >> D from the lens, will a projectable image be formed (explain),
if so, where, and what will be its magnification?

Not Surprising a distant object creates an image near the food point i

More to the pant, the image is real (9>0) and therefore something that can be projected.

Q= \frac{dDL}{DL-dL-dD}

M=-9\beta=-\frac{9}{L} = \frac{-dD}{DL-dL-dD}

• 2d) (5 points) Ok, I apologize, but we need some numbers to gauge the feasibility of the technique. Typical values for the relevant quantities are L = 4 m, D = 0.5 m and d = 0.1 m. How much distance will there be between the lens and the screen? If the physical object located at L is 2 m tall, how large will its image be? Does it seem likely an artist could use this technique to trace a nearly photographic image onto the screen?

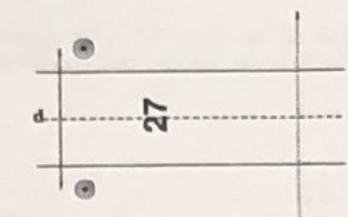
$$Q = \frac{(4m)(0.5m)(0.1m)}{2m^2 - 0.4m^2 - 0.05m^2} = \frac{0.2m^3}{1.55m^2} \approx \frac{4}{3} (\frac{1}{10})m \approx 0.13m$$

$$M = \frac{-0.05m^2}{2m^2 - 0.4m^2 - 0.05m^2} = \frac{-0.05m^2}{1.55m^2} \approx \frac{2.5}{8}.5 (\frac{1}{100}) \approx -0.033$$

M=1 => hi=2m,0.033 = 0,066m

The screen is a 13 cm behind the lens and the (inverted) image is about 7 cm tall...

It's going to be tight, but it's Probably Not impossible



A simple navigation system consists of two radio-frequency antennas fed in-phase with a signal of wavelength λ. The antennas lie along a line that runs perpendicular to the runway, they are equidistant from the center of the runway, and they are separated by a distance d. Incoming aircraft are supposed to locate the central maximum generated by the resultant signal and follow it to a safe landing on the airstrip below.

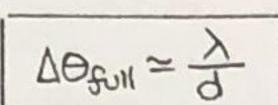
• 3a) (5 points) Find the full angular width of the central maximum (assume small angle approximations are relevant).

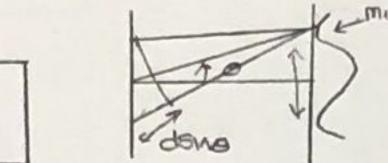
where is the first-order minimum?

AOTOT = (ZN+1) TE

T dSna = T

0~ 2 =





this is half the full width

• 3b) (5 points) Under what (approximate) conditions will there only be a central maximum? Small angles are probably not so relevant...

Sino = 2 to if a > T/2, we only have a central max

Alternately, and probably no less wrong... DO full ~ To

• 3c) (5 points) It might seem like a good idea to set things up so that there are no higher-order maxima to confuse the pilot, but it really isn't. Why? What compromise needs to be made?

If there are no higher-order maximos, that central max is wide and poloably not all that useful for lining up with the runway, we need to narrow the Central peak without introducing so many high-order peaks that it is confusing.

• 3d) (5 points) We can resolve the problem inherent with higher-order maximas by feeding each antenna with two in-phase radio signals - one with a wavelength \(\lambda_1 \) and the other with a wavelength λ_2 . Explain how this will fix the problem if the larger of λ_1 and λ_2 is not an integer multiple of the smaller (why is this condition important?).

Maxima: DOTOT = 2TCN ZT dane = 2TTW BUON= NA

if 7=222, the maximas line up Whenever N2=2N, for 196tance

if hi and he aren't related by an integer multiple, the only direction their maximas will line up together (N=Nz=0) is straight ahead - if the pilot is fined up with the runway, she should hear maximas at both wavelengths

• 3e) (10 points) A pilot decides to calibrate her groundspeed indicator. She flies along a path parallel to the line joining the antennas, a distance D from that line and notes the signal strength at wavelength λ_1 is fluttering at a rate F_1 beats per second. How fast is she flying?

Maximas occour when Sing = NA

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