

4

Math 61 Quiz Week 4 10 minutes. Use pen only

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SECTION: Cross one box below

Day \ T.A.	John	Zach	Sam
Tuesday	1A	1C	<input checked="" type="checkbox"/> 1E
Thursday	1B	1D	1F

Problem 1. Circle the option that applies. The number of 3-permutations of $\{1, 2, 3, 4, 5\}$ (i.e. injections from $X = \{1, 2, 3\}$ to $Y = \{1, 2, 3, 4, 5\}$) is

- (a) 15,
- (b) $3!$,
- (c) 30,
- (d) 10,
- (e) $5!$.

$5 \cdot 4 \cdot 3 = 60$

$\frac{n}{n-1}$
 $543 = 20 \cdot 3 = 60?$

$n=5, k=3 \rightarrow 5P_3 = \frac{5!}{(5-3)!}$

Problem 2. Circle the option that applies. The number of 3-combinations of $\{1, 2, 3, 4, 5\}$ is

- (a) 15,
- (b) $3!$,
- (c) 30,
- (d) 10,
- (e) $5!$.

$n=5, k=3$

$5C_3 = \frac{5!}{(5-3)! 3!} = \frac{5 \cdot 4}{2} = 5 \cdot 2 = 10$

$5C_3 = \frac{5 \cdot 4 \cdot 3}{3 \cdot 2 \cdot 1} = 10$

Problem 3. Circle the option that applies. How many nonnegative integer solutions are there to $x_1 + x_2 + x_3 + x_4 = 6$?

- (a) $\binom{6}{4}$,
- (b) $\binom{9}{3}$,
- (c) $\binom{10}{4}$,
- (d) $\binom{10}{3}$,
- (e) $\binom{9}{4}$.

$6=n, k=4$

$\binom{6+4-1}{4-1} = \binom{9}{3}$

Problem 4. Below are parts of the ninth and tenth row of Pascal's triangle: $\binom{9}{0}, \dots, \binom{9}{9}$ and $\binom{10}{0}, \dots, \binom{10}{10}$. Fill in the missing entries.

	1	9	36	84	126	126	84	36	9	1
1	<u>10</u>	45	<u>120</u>	<u>210</u>	<u>252</u>	<u>210</u>	<u>120</u>	<u>45</u>	<u>10</u>	1

$\frac{126}{36} = 3.5$
 $\frac{126}{84} = 1.5$
 $\frac{120}{36} = 3.33$
 $\frac{120}{84} = 1.43$