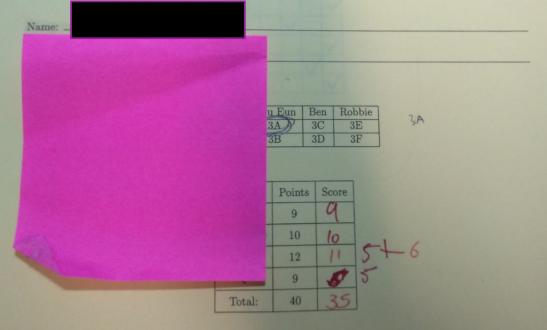
## Midterm 1

UCLA: Math 32B, Winter 2017

Instructor: Noah White Date: 30 January 2017

- This exam has 4 questions, for a total of 40 points.
- · Please print your working and answers neatly.
- Write your solutions in the space provided showing working.
- · Indicate your final answer clearly.
- You may write on the reverse of a page or on the blank pages found at the back of the booklet however these will not be graded unless very clearly indicated.
- Non programmable and non graphing calculators are allowed.



Question 1 is multiple choice. Once you are satisfied with your solutions, indicate your answers by marking the corresponding box in the table below.

Please note! The following three pages will not be graded. You must indicate your answers here for them to

Question 1.

Part	A	В	C	D
(a)	/			
(b)				/
(c)	V			
(d)	V			
(e)				V
(f)		V		
(g)				/
(h)			V	
(i)				V

- 1. Each of the following questions has exactly one correct answer. Choose from the four options presented
  - (a) (1 point) If  $\mathcal{R} = [-1,0] \times [2,6]$ , the integral  $\iint_{\mathcal{R}} \frac{1}{2} dA$  is equal to

(A)2

B. 0

C. 5

D. 4

She = dA

She = dxdy 

(b) (1 point) If  $\mathcal{R} = [0,1] \times [0,1]$ , the integral  $\iint_{\mathcal{R}} 4xy \, dA$  is equal to

C. -4

SS 4xydxdy S' 4x2 y / dy = S' 2y(1-0) dy - 822/ = 1-0 =

(c) (1 point) If  $\mathcal{B} = [-1,1] \times [0,1] \times [\bar{3},4]$ , the integral  $\iiint_{\mathcal{B}} -2 \, dV$  is equal to

SS-2 1+ dydz

535' -2(1+1) dyte = 53 8 -4y/s 5, 5, -2 x 1, dyde

= 54-4(1-0)dz = 6-42/3 = -4(4-3)

d) (1 point) If  $\mathcal{R} = [-2, 2] \times [3, 6]$ , the integral  $\iint_{\mathcal{R}} xe^{x^2+y^2} dA$  is equal to

(e) (1 point) If  $\mathcal{B} = [0,1] \times [0,3] \times [0,3]$ , the integral  $\iiint_{\mathcal{B}} 2x \ dV$  is equal to

B. 18

C. 1

Hint: integrate in the order dx dy dz

S'S' 2xdxdydz = 535° \$x2/ dydz

= \$ 53 y 13 = 53 - 0) dz

(f) (1 point) The Jacobian of the change of coordinates  $G(u,v)=(u^2+v,v^2+u)$ A. un+1

A. uv+1

4uv-1

C.  $2v^2 - 1$ 

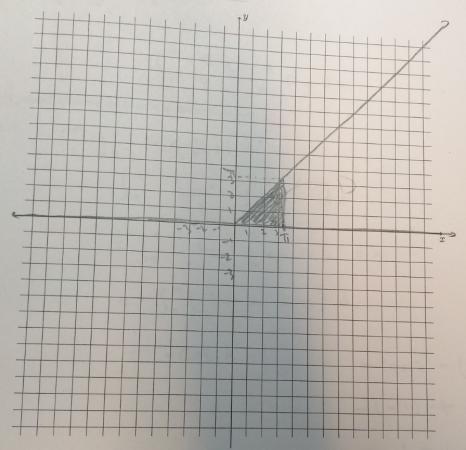
D.  $4u^2v^2$ 

Midterm 1 Winter, 2017 (g) (1 point) If  $\mathcal{D}$  is the region  $4 \leq x^2 + y^2 \leq 16$ , where  $y \geq 0$  then after changing to polar coordinates, the integral  $\iint_{\mathcal{D}} x \, dA$  becomes A.  $\int_0^{\pi} \int_2^3 r \cos \theta \, dr \, d\theta$ B.  $\int_0^{2\pi} \int_2^4 r^2 \sin \theta \, dr \, d\theta$ C.  $\int_0^{\pi} \int_2^4 r^3 \sin 2\theta \, dr \, d\theta$  $\int_0^\pi \int_2^4 r^2 \cos\theta \, dr \, d\theta$ 4565616 (h) (1 point) The integral of  $2\sqrt{x^2+y^2}$  over the disc  $x^2+y^2\leq 1$  is 550 2502 Aprobe B.  $2\pi$ 2 /2 /2 5 5 1845 749 Sin 563 / 90 8 2 503 - 513 250 300 -> [30] (i) (1 point) If  $\mathcal{D}$  is the region between the curves  $y=x^2$  and  $y=\sin(\frac{1}{2}\pi x)$  in the first quadrant then  $\mathcal{D}$  has the description A.  $0 \le x \le \pi$ ,  $\sin(\frac{1}{2}\pi x) \le y \le x^2$ B.  $0 \le x \le 1$ ,  $\sin(\frac{1}{2}\pi x) \le y \le x^2$ 0,25 C.  $0 \le x \le \pi$ ,  $0 \le y \le \sin(\frac{1}{2}\pi x)$ D  $0 \le x \le 1$ ,  $x^2 \le y \le \sin(\frac{1}{2}\pi x)$ 001

[511 - 61 scho! ]

2. In this question we will consider the region  $\mathcal D$  which bounded by the lines

- y = x, and
- (a) (2 points) Sketch the region  $\mathcal D$  on the graph provided.



(b) (1 point) Express  $\mathcal D$  as a vertically simple region, i.e. in the form  $a \leq x \leq b, \ g_1(x) \leq y \leq g_2(x).$ 

(c) (1 point) Express  $\mathcal D$  as a horizontally simple region, i.e. in the form  $c \leq y \leq d, \ h_1(y) \leq x \leq h_2(y)$ .

(d) (2 points) Write the integral

as an iterated integral (in either order is fine)  $\iint_{\mathcal{D}} \frac{\sin x}{x} dA$ 

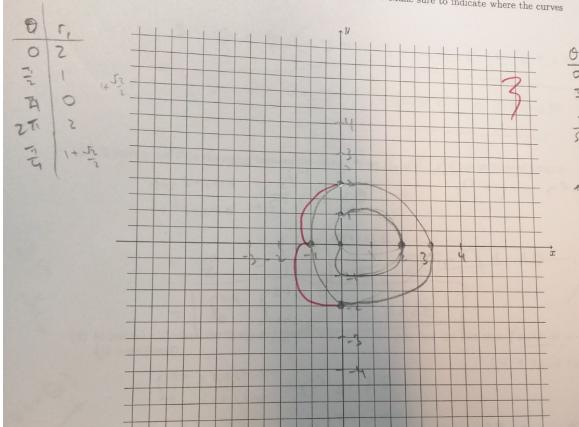
(e) (4 points) Evaluate the integral in the previous part.

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- 3. In this question, consider the curves  $r = 1 + \cos \theta$  and  $r = 2 + \cos \theta$ .
  - (a) (4 points) Sketch both the curves on the graph provided. Make sure to indicate where the curves



Midton aly for livery of is UCLA: Math 32B Midterm 1 (b) (2 points) Write the region between the two curves as a radially simple region, i.e in the form (D: 0 = 6 = 54) 1+ (0) 0 = ( = 5 + (0) 0 (c) (2 points) Let  $\mathcal{D}$  be the region between the curves. Write  $\iint_{\mathcal{D}} \sqrt{x^2 + y^2} \, dA$  as an iterated integral. (d) (4 points) Calculate the integral  $\iint_{\mathcal{D}} \sqrt{x^2 + y^2} \, dA$ . You may use the fact that  $\int \cos^2 \theta \, d\theta = \frac{1}{2}(\theta + \sin \theta \cos \theta)$ .  $\frac{1}{2}(\theta + \sin\theta\cos\theta)$ . 850 85 4610 165 ge 90 - 2 /3 /2+ 200 do = (3 /2+ 00) 3 (1+00) 3 (1+00) = 5211 (4+4000+0020)(2+000) = (1+2000+0020)(1+000) = 5211 (4+4000+0020)(2+000) = (1+2000+0020)(1+000) 3 8 + 122000 + 620120 + 1-320,0-320,20 do 0)

2 1211 7+9200 + 120520 00 = 1 (70+9520 + 500,200)

(onchosine · With of for UCLA: Math 32B Midterm 1 4. Consider the region  $\mathcal E$  in the intersection of the two balls  $x^2+y^2+(z-\frac12)^2\leq 1$  and  $x^2+y^2+(z+\frac12)^2\leq 1$ .  $\mathcal{E} = \{ \ (x,y,z) \in \mathbb{R}^3 \mid (x,y) \in \mathcal{D}, \ z_1(x,y) \leq z \leq z_2(x,y) \}$ for  $\mathcal D$  a region in the xy-plane. Your answer should specify what  $\mathcal D$  is. & - { (x y, z) & R3 (x,y) & x2 + y2 < 13/4, - 51-x2-y2 + 2 < 2 (51-x2-y2) (b) (5 points) Compute the volume of the region  $\mathcal{E}$ . = 51 55.9° Z | 11-x2-y2 - 2 | 11-x2-y2 - 1) Aydy polar! 6 51 5-1-42 (2]1-x2-y2-1)dxdy