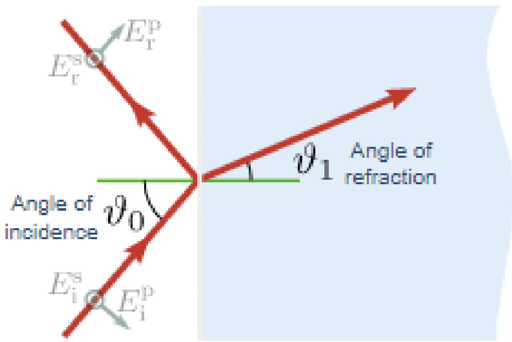
ECE170A Midterm

Nov. 10th 11am - 3pm PST

Due: submit the PDF version of your final mlx file by Nov.10th 15:00 PST on Gradescope

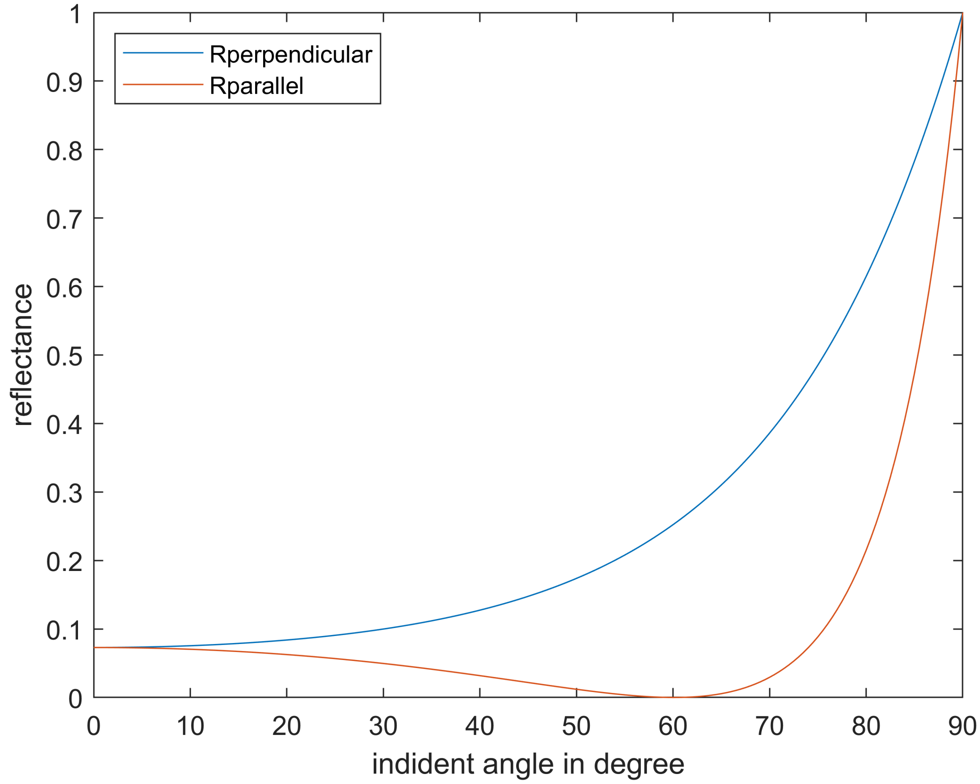
Problem 1 Fresnel Equations and Reflectance



Suppose the light beam of wavelength 2 μm incident from air to the material, given the refractive index in the air $n_0 = 1$ and the refractive index in the material $n_1 = 1.74$. Calculate the reflectance of p-polarized component (parallel to the incidence plane) and s-polarized (perpendicular to the incidence plane) component respectively and plot the reflectance of p-polarized component and s-polarized component vs. incidence angle (from 0-90 degrees).

You should have two curves in the same plot. The horizontal axis is the incidence angle (in degree), the vertical axis is the reflectance.

```
n=1.74;
theta=0:0.5:90;
Rperpendicular=((cosd(theta)-(n*n-sind(theta).*sind(theta)).^0.5)./(cosd(theta)+(n*n-sind(theta
Rparallel=(((n*n-sind(theta).*sind(theta)).^0.5-n*n.*cosd(theta))./((n*n-sind(theta).*sind(the
plot(theta,Rperpendicular,theta,Rparallel)
xlabel('indident angle in degree')
ylabel('reflectance')
legend({'Rperpendicular','Rparallel'},'Location','northwest');
```



Problem 2 Diffraction Angles of Reflection Gratings

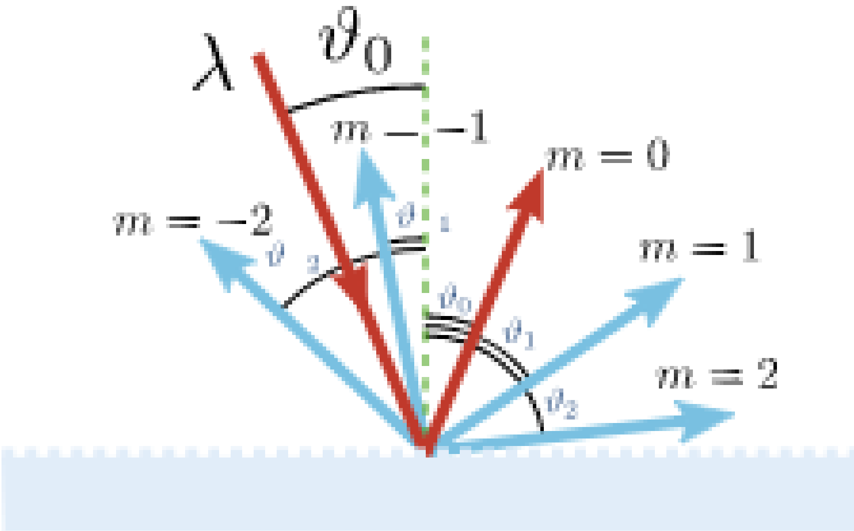
Consider a reflection grating with a period $d = 1.25\ \mu m$. A collimated light wave is incident on the grating at an angle of 25°. Find the diffraction angle of order $m = -3,\ -2,\ -1,\ 1$ and plot the diffraction angles vs. wavelengths λ (from $400\ \mathrm{nm}$ to $1600\mathrm{nm}$).

You should have 4 curves in the same plot. The horizontal axis is the wavelength (in nm), the vertical axis is the diffraction angle (in degree)

note:

1. not every wavelength in the range is valid for all orders of diffraction angles, you may need to first find a cut-off wavelength for each order. For wavelength greater than the cut-off wavelength, there will be no valid solution because the value of sin() function cannot be larger than 1.

2. the diffraction angles could have negative values. Given the light is incident from the left of the normal, we define the reflected light on the right of the normal to have positive diffraction angle, the reflected light on the left of the normal to have negative diffraction angle. (In the figure below for example, the cases where m=0,1,2 have positive angles and the cases where m=-1, -2 have negative values.)




```
d=1.25*10^(-6);
m1=1;
m2=-1;
m3=-2;
m4=-3;
upper1=(1-sind(25))*d/m1
```

```
upper1 = 7.2173e-07
```

```
lower1=(-1-sind(25))*d/m1
```

```
lower1 = -1.7783e-06
```

```
upper2=(1-sind(25))*d/m2
```

```
upper2 = -7.2173e-07
```

```
lower2=(-1-sind(25))*d/m2
```

```
lower2 = 1.7783e-06
```

```
upper3=(1-sind(25))*d/m3
```

```
upper3 = -3.6086e-07
```

```
lower3=(-1-sind(25))*d/m3
```

```
lower3 = 8.8914e-07
```

```
upper4=(1-sind(25))*d/m4
```

```
upper4 = -2.4058e-07
```

```
lower4=(-1-sind(25))*d/m4
```

```
lower4 = 5.9276e-07
```

```
lamda1=400*10^(-9):20*10^(-9):721.73*10^(-9);
lamda2=400*10^(-9):20*10^(-9):1600*10^(-9);
lamda3=400*10^(-9):20*10^(-9):889.14*10^(-9);
lamda4=400*10^(-9):20*10^(-9):592.76*10^(-9);
theta1=asind(m1.*lamda1./d+sind(25));
theta2=asind(m2.*lamda2./d+sind(25));
theta3=asind(m3.*lamda3./d+sind(25));
theta4=asind(m4.*lamda4./d+sind(25));
plot(lamda1,theta1,lamda2,theta2,lamda3,theta3,lamda4,theta4)
legend({'m = 1','m = -1','m = -2', 'm = -3'},'Location','northeast');
```