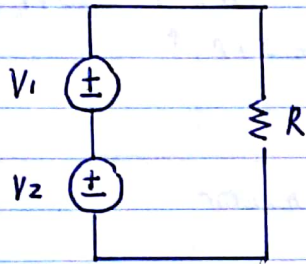


# WEEK 5 DISCUSSION MIDTERM ANS

#1



$$V_1(t) = A \sin \omega t$$

$$V_2(t) = 2A \sin \omega t$$

find  $\langle p(t) \rangle$  for R (average power consumed by resistor)

$$\langle p(t) \rangle = V_{\text{rms}}^2 R$$

↑  
over the resistor

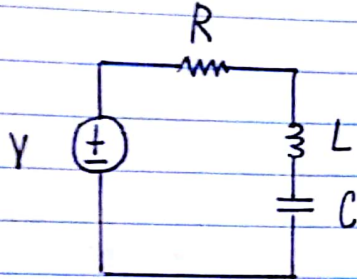
$$V_{\text{rms}}^2 = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} (V_1(t) + V_2(t))^2 dt$$

$$= \lim_{T \rightarrow \infty} \frac{1}{T} \left[ \int_{-T/2}^{T/2} V_1^2(t) dt + \int_{-T/2}^{T/2} V_2^2(t) dt + \int_{-T/2}^{T/2} 2V_1(t)V_2(t) dt \right]$$

$$= \frac{A^2}{2} + 2A^2 = \frac{5A^2}{2}$$

$$\langle p(t) \rangle = \frac{5A^2}{2R}$$

#2



Sine voltage source. we know  $V_{rms} = 5V$

2 conditions:

- when  $C = 0.2F$ ,  $I_{rms} = 1A$ ,  $P = 3W$

- when  $C = 1/45 F$ , same  $I + P \uparrow$

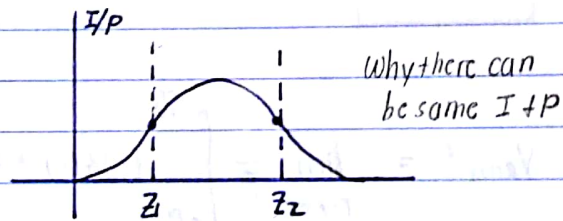
$L$  and  $C$  are lossless, only power dissipated should be from the resistor

↓

$$P = I^2 R$$

$$3 = (1)^2 R$$

$$R = 3\Omega$$



$$I_{rms} = \frac{V_{rms}}{|Z|} = \frac{5}{\sqrt{R^2 + (\omega L - 1/\omega C)^2}}$$

$$\textcircled{1} \quad 3^2 + (\omega L - 5/\omega)^2 = 5^2$$

$$\textcircled{2} \quad \omega L - 5/\omega = -(\omega L - 45/\omega)$$

$$\text{from } \textcircled{2} \Rightarrow 2\omega L = 50/\omega \Rightarrow \omega^2 L = 25$$

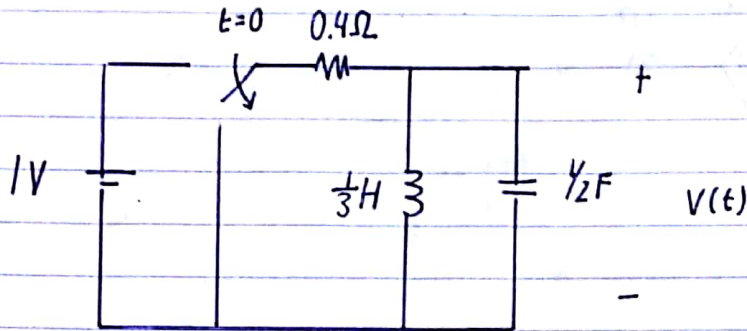
$$\text{from } \textcircled{1} \Rightarrow 9 + (\omega^2 L - 5)^2 / \omega^2 = 25$$

$$20^2 / \omega^2 = 16$$

$$\omega = 5 \text{ rad/s}$$

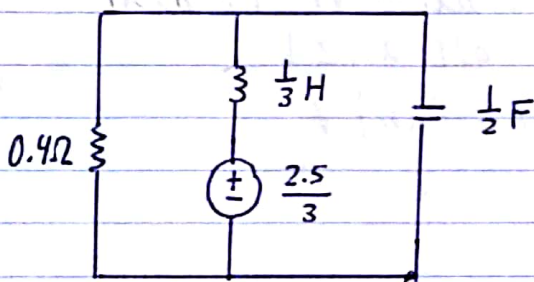
$$L = 1H$$

#3



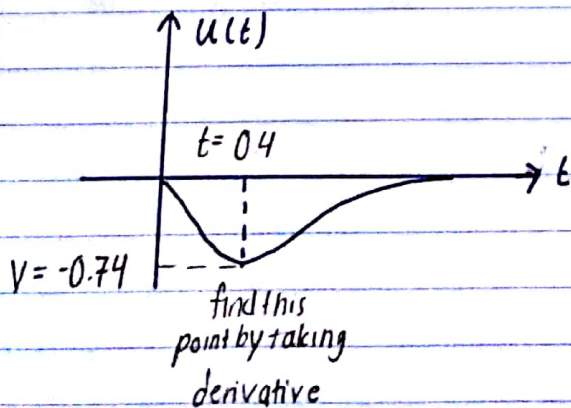
$$V_C(0^-) = 0V \quad i_L(0^-) = \frac{1}{0.4} = 2.5A$$

initial cond.



$$\begin{aligned} V(s) &= -\frac{2.5}{3} \cdot \frac{1}{1+sL(6+sC)} \\ &= -\frac{2.5}{3} \cdot \frac{1}{1+sL(6+sC)} = -\frac{2.5}{3} \cdot \frac{1}{1+s^2 \frac{5}{3} + s^2/6} \\ &= -5 \cdot \frac{1}{s^2 + 5s + 6} = -5 \left( -\frac{1}{s+3} + \frac{1}{s+2} \right) \end{aligned}$$

$$v(t) = \mathcal{L}^{-1} V(s) = -5(-e^{-3t} + e^{-2t}) = 5e^{-3t} - 5e^{-2t}$$



$$\frac{dv(t)}{dt} = 0$$

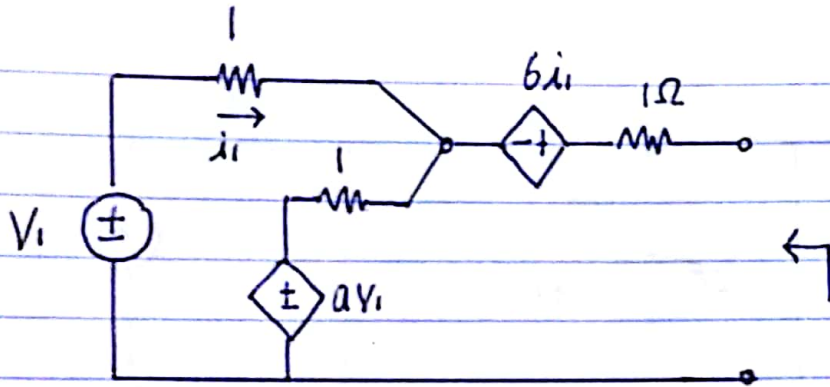
$$-15e^{-3t} + 10e^{-2t} = 0$$

$$2e^{-2t} = 3e^{-3t}$$

$$t = 0.4s$$

$$e^t = 1.5 \Rightarrow v(t) = -0.74V$$

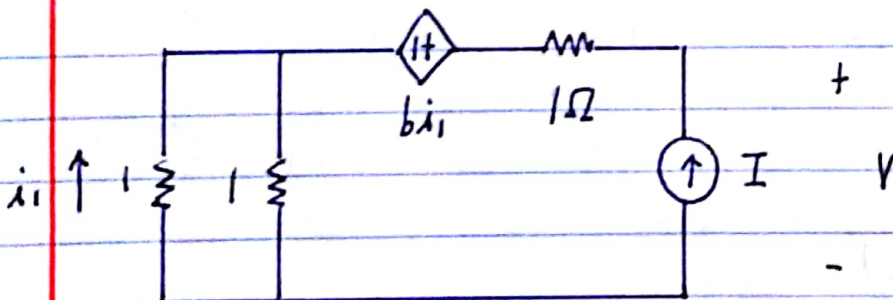
#4



① OC Voltage

$$i_1 = \frac{(V_1 - aV_1)}{2}$$

$$\begin{aligned} V_T &= V_1 - i_1 \cdot 1 + b i_1 = V_1 - (1-b) i_1 \\ &= V_1 [1 - (1-b)(1-a)/2] \\ &= \frac{V_1}{2} [1 + a + b - ab] V \end{aligned}$$



$$i_1 = -\frac{I}{2}$$

$$V = -\frac{I}{2} \cdot 1 - \frac{I}{2} \cdot b + I \cdot 1$$

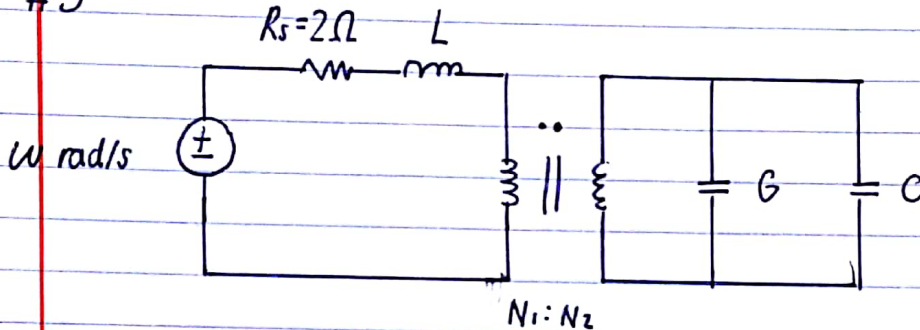
$$\frac{V}{I} = \frac{1}{2} (1-b) \Omega$$

find  $\omega L$  and  $N_1/N_2$  to deliver max power to  $G$

$$G = 2\text{S} \quad C = 1\text{S}$$

Siemens

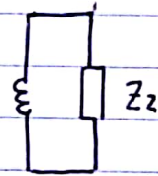
#5



Driving Point Impedance

$$Z_2 = \frac{1}{G + j\omega C} = \frac{1}{G^2 + (\omega C)^2} - j \frac{\omega C}{G^2 + (\omega C)^2}$$

$$= \left( \frac{2}{5} - j \frac{1}{5} \right) \Omega$$



$$\frac{Z_1}{Z_2} = \left( \frac{N_1}{N_2} \right)^2$$

$$Z_1 = Z_2 \left( \frac{N_1}{N_2} \right)^2$$

$$R_s = \frac{2}{5} \left( \frac{N_1}{N_2} \right)^2$$

$$\frac{N_1}{N_2} = \sqrt{5}$$

$$\omega L = \frac{1}{5} \cdot 5 = 1 \Omega$$

