EE10 Midterm II

Department of Electrical Engineering, UCLA

Winter 2014

Instructor: Prof. Gupta

- 1. Exam is closed book. Calculator and one double sided cheat-sheet is allowed.
- 2. Cross out *everything* that you don't want me to see. Points will be deducted for everything wrong!
- 3. No points will be given without proper explanations
- 4. Time allotted: 75 minutes

		920
x **		
	7	

Problem	Maximum Score	Your Score
1	8	7+1
2	8	8
3	8	8
4	6	6
Total	30	29+1

Q1. 8points: (5+3)

(a) A car travels at a constant speed along a bumpy road. As a result of the bumps, the velocity of the car's axle perpendicular to the road is V (t). Taking into account the dynamics of the car's suspension system, the equation of motion for the body of the car (the chassis) can be formulated as follows:

$$M\frac{du}{dt} + Bu(t) + K \int_{-\infty}^{t} u \, dt = -M \frac{dV}{dt}$$

where u(t) is the velocity of the body of the car (relative to the axle), M is the mass of the car, K is the spring constant of the springs connecting the body to the axle, and B is the coefficient of viscous damping for the shock absorbers. In this problem, you will be asked to make a circuit model corresponding to the equation of mechanical dynamics from the Equation, and then you will use the model to investigate the car's motion due to the bumpy road.

Node

Voltage

Similar to

$$C \frac{de(t)}{dt} + \frac{1}{Re(t)} + \frac{1}{L} \int_{-\infty}^{t} (t) dt = \frac{R}{US} + \frac{1}{L} \int_{-\infty}^{t} (t) dt = \frac{1}{L} \int_{-\infty}^{t} (t) dt$$

The circuit above is proposed to model Equation, where the node voltage e(t) is identified with the car body's velocity u(t). Determine the values of v_s , C, L, and R in terms of the parameters in Equation so that the solution for e(t) will be identical to the solution of Equation for u(t).

(b) A second order circuit shows an underdamped natural response $i(t) = \exp(-t)\cos(2t + pi/3)$. What is the characteristic equation for this circuit?

$$i(t) = e^{-t} \cos(2t + \frac{\pi}{3})$$

$$= e^{-t} \left(C_1 \cos 2t + C_2 \sin 2t \right)$$

$$b = 2a$$

$$b = 2$$

$$Let a = 1$$

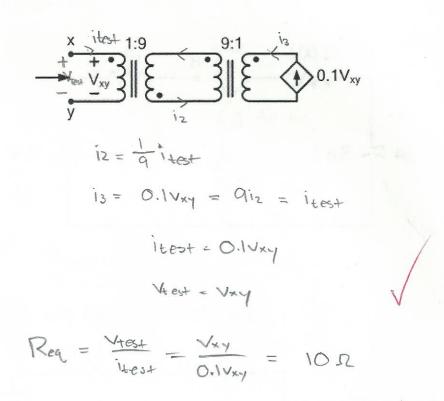
$$S = -1 + 2i = -b + \sqrt{b^2 - 4(a)(c)}$$

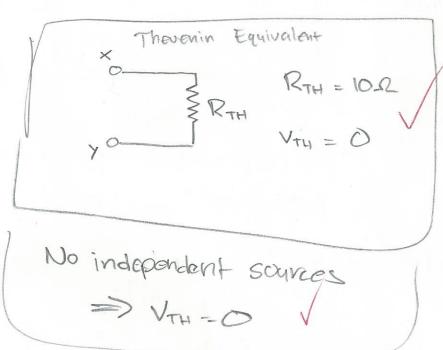
$$S_{13}S_2 = -1 + 2i$$

$$S_{24}S_{15}S_$$

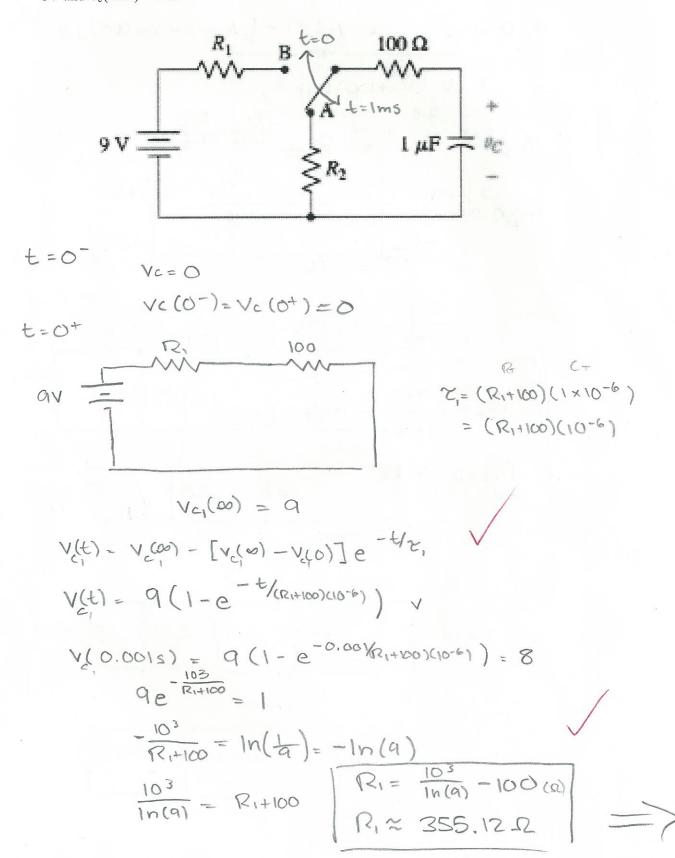
Q2. 8 points

Find the Thevenin Equivalent seen between nodes x and y. Assume that the transformers are ideal.





The switch in the circuit below has been in position A for long time. It is switched to position B at t=0 and back to position A at t=1ms. Find R1 and R2 such that $v_c(1ms) = 8V$ and $v_c(2ms) = 1V$.



$$V_{c}(1ms) = 8V = V_{c2}(0t)$$

$$V_{c}(\infty) = 0$$

$$V_{c}(t) = V_{c2}(\infty) - [V_{c2}(\infty) - V_{c2}(0t)] e^{-tc/2t}$$

$$V_{c2}(t) = 8 e^{-(t-0.001)}$$

$$V_{c2}(0.002) = 8e^{-(0.002-0.001)}$$

$$e^{-(0.002-0.001)}$$

$$e^{-(0.002-0.001)} = V_{8}$$

$$-\frac{10^{3}}{R_{2}+100} = In(V_{8}) = -In(8)$$

$$R_{2} = \frac{10^{3}}{1n8} - 100 (a)$$

$$R_{2} \approx 380.90 \Omega$$

Q4. 6 points

A long time after the connections have been made, find out the value of $v_{\rm x}$ if there is an inductor present between a and b.

