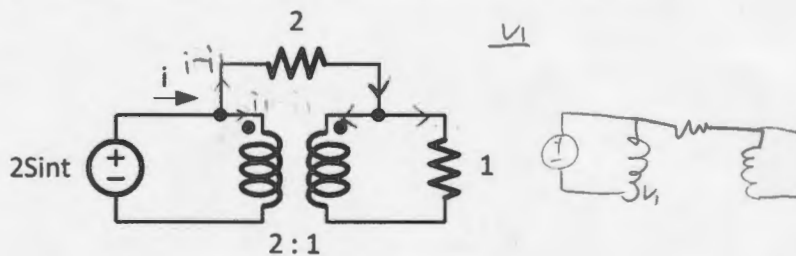
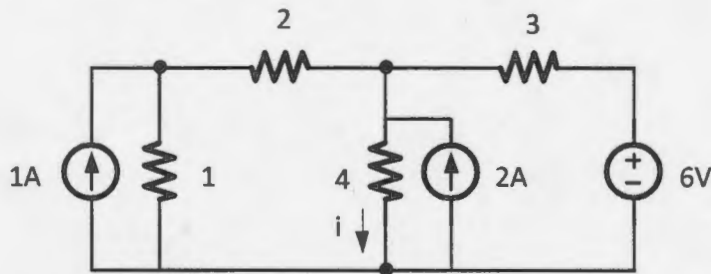


Total of 3 questions, 100 minutes.

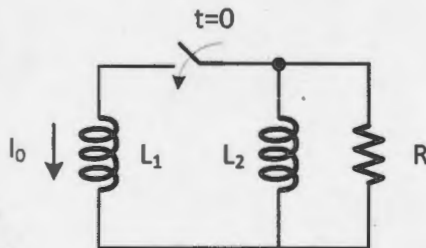
1. In the following circuit, the transformer is ideal. Find the current i (30 points).



2. Find the current i in the circuit below by a) node analysis, b) superposition (40 points).

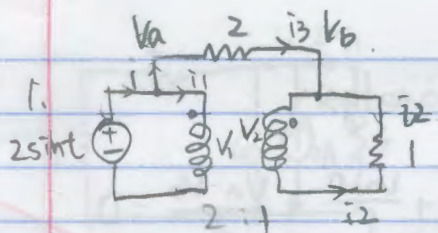


3. In the circuit below, inductor L_1 has an initial current of I_0 and the circuit has been idle for a long time. The switch is closed at $t = 0$. Plot and find the resistor voltage. What is the final current of the inductors at $t = \infty$ (40 points).



$$\frac{1}{L_1} + \frac{1}{L_2} = \frac{L_1 + L_2}{L_1 L_2}$$

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section D



$$\frac{V_1}{V_2} = \frac{N_1}{N_2} = \frac{2}{1}$$

$$V_1 = 2V_2 \quad \checkmark$$

$$V_a - V_b = V_1 - V_2$$

From KVL, $-2 \sin t + V_1 = 0$ $-V_2 + 1 \cdot i_2 = 0$ $i_2 = V_2$

$$V_1 = 2 \sin t$$

$$V_2 = \frac{1}{2} V_1 = \sin t$$

$$i_2 = \sin t \quad \frac{i_1}{i_2} = -\frac{N_2}{N_1} = -\frac{1}{2} \quad \checkmark$$

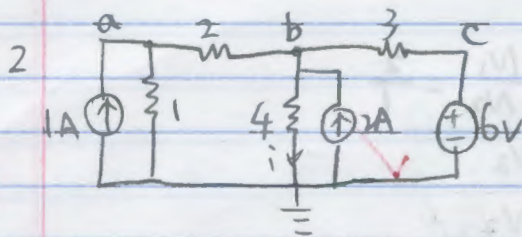
$$i_1 = -\frac{1}{2} i_2 = -\frac{1}{2} \sin t \quad (\text{different direction})$$

current from \$V_a\$ to \$V_b\$ is

$$i_3 = \frac{V_a - V_b}{2} = \frac{2 \sin t - \sin t}{2} = \frac{\sin t}{2}$$

$$i = i_3 + i_1 = \frac{\sin t}{2} + \frac{\sin t}{2} = \sin t$$

73
110



a) node analysis

for a

$$-1 + \frac{V_a - 0}{1} + \frac{V_a - V_b}{2} = 0$$

$$V_a + \frac{V_a - V_b}{2} = 1$$

$$3V_a - V_b = 2$$

for b. $\frac{V_b - V_a}{2} + \frac{V_b}{4} + \frac{V_b - V_c}{3} - 2 = 0$

$$6(V_b - V_a) + 3V_b + 4(V_b - V_c) = 24$$

$$-6V_a + 13V_b - 4V_c = 24 \quad -6V_a + 13V_b = 48$$

for c $V_c = 6V$

$$\begin{cases} 3V_a - V_b = 2 & \textcircled{1} \\ -6V_a + 13V_b = 48 & \textcircled{2} \end{cases}$$

$$\textcircled{1} \times 13 \quad 39V_a - 13V_b = 26 \quad \textcircled{3}$$

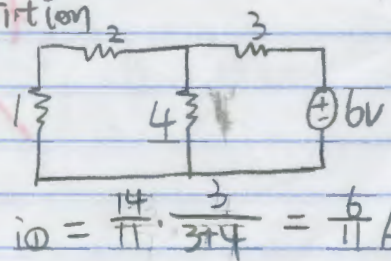
$$\textcircled{3} + \textcircled{2} \quad 33V_a = 74 \quad V_a = \frac{74}{33} \quad V_b = \frac{52}{11} = 4.72V$$

$$= 2.24V$$

$$i = \frac{V_b}{4} = \frac{52}{11} \div 4 = \frac{13}{11}V = 1.18A$$

② superposition

close 1A, 2A

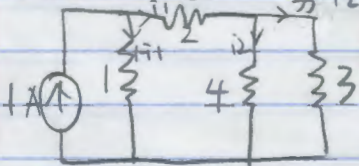


$$R_{eq} = \frac{(1+2) \times 4}{1+2+4} = \frac{12}{7}$$

$$I = 6 \div (3 + \frac{12}{7}) = \frac{14}{11}A$$

$$i_0 = \frac{14}{11} \cdot \frac{3}{3+4} = \frac{6}{11}A$$

close 2A, 6V



$$\frac{3 \times 4}{3+4} = \frac{12}{7} \Omega$$

$$i_1 (2 + \frac{12}{7}) = 1 (1 - i_1)$$

$$\frac{26}{7} i_1 = 1 - i_1$$

$$\frac{33}{7} i_1 = 1 \quad i_1 = \frac{7}{33}$$

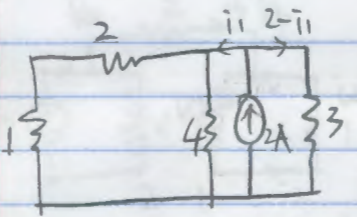
$$4i_2 = 3(\frac{7}{33} - i_2) \quad 4i_2 = \frac{7}{11} - 3i_2$$

$$i_2 = \frac{1}{11}A$$

$$i_0 = \frac{1}{11}A$$

close 1A, 6V

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$$\frac{5 \times 4}{3+4} = \frac{12}{7} \Omega$$

$$\frac{12}{7} i_1 = 3(2 - i_1)$$

$$\frac{12}{7} i_1 = 6 - 3i_1 \quad \frac{33}{7} i_1 = 6$$

$$i_1 = \frac{14}{11} \text{ A}$$

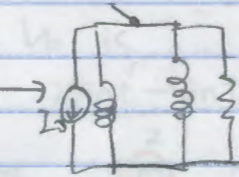
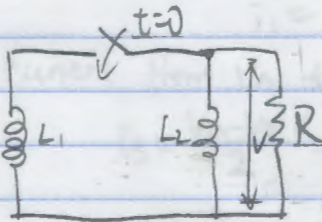
$$\frac{14}{11} \text{ A} \cdot \frac{3}{3+4} = \frac{6}{11} \text{ A}$$

$$i_3 = \frac{6}{11} \text{ A}$$

$$So \quad i = \frac{6}{11} + \frac{6}{11} + \frac{1}{11} = \frac{13}{11} \text{ A} = 1.18 \text{ A}$$

40

3



$$V = L \frac{di}{dt}$$

25

$$V_R(0^-) = 0$$

$$V_R(0^+) = I_0 R$$

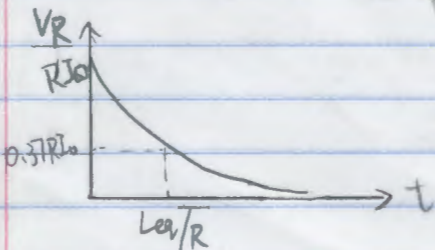
$V_R(\infty) = 0$ as all energy is dissipated by resistor

$$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$$

$$V_R(t) = 0 + (R I_0 - 0) e^{-\frac{t}{\tau}}$$

$$= R I_0 e^{-\frac{(L_1 + L_2) R t}{L_1 L_2}}$$

$$\tau = \frac{L}{R} = \frac{L_1 L_2}{(L_1 + L_2) R}$$



Because of flux conservation

$$L_1 I_0 = L_{eq} I$$

$$L_1 I_0 = \frac{L_1 L_2}{L_1 + L_2} I$$

$$I = K I_0 \frac{L_1 + L_2}{L_1 L_2}$$

$$= \frac{I_0 (L_1 + L_2)}{L_1 L_2}$$