

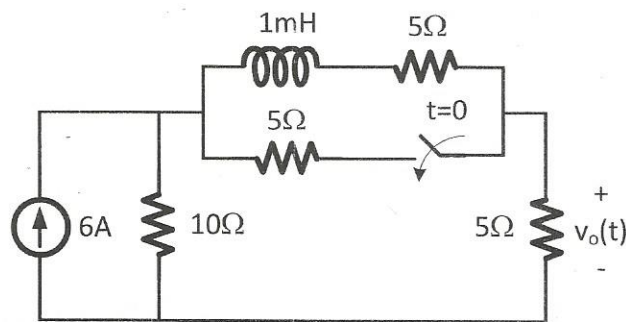
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Total of four questions (25 points each), three hours.

Box your answers.

Leave margin on your answer sheet for staple.

1. The circuit below has been idle (switch open) for a long time. At  $t = 0$  the switch is closed.
  - a) Give mathematical expression of  $v_o(t)$
  - b) Plot  $v_o(t)$

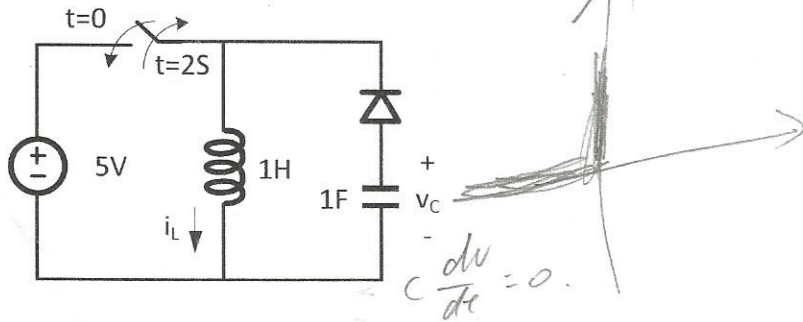


2. The circuit below is at zero state for  $t < 0$ , and the diode is ideal. The switch closes at  $t = 0$ , and opens at  $t = 2$ .
  - a) Calculate and plot  $i_L(t)$  as marked on the circuit
  - b) Calculate and plot  $v_C(t)$  as marked on the circuit

$$L \frac{di}{dt} = V_C$$

$$C \frac{dv}{dt} = i_C$$

$$L \frac{di}{dt^2} = \frac{dV_C}{dt}$$



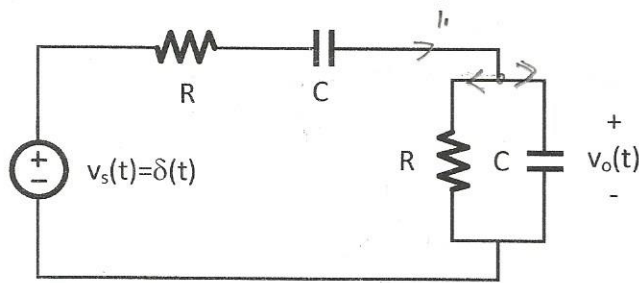
$$C \frac{dv}{dt} = 0$$

$$10 \cdot \frac{5}{2} = 25$$

$$5 \cdot \frac{5}{17.5} = \dots$$

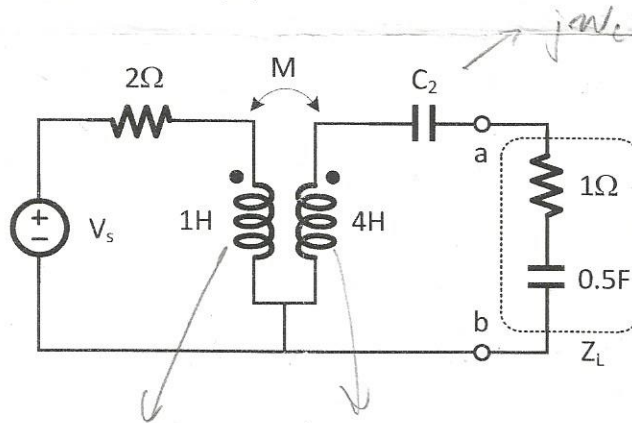
$$LC \frac{di}{dt^2} = i_C$$

3. In the following second-order circuit, R is resistance and C is capacitance.
- Calculate and plot the impulse response ( $v_o$  is the output);
  - Intuitively, find the values of  $v_o(0^+)$  and  $\frac{dv_o}{dt}(0^+)$ .



$$\left( \frac{16C_2 - 1}{4C_2 M} \right) I_2'$$

4. The following circuit is in sinusoidal steady state, and  $v_s(t) = 2 \cos 2t$ .
- Find the Thevenin equivalent on the left side of nodes a-b;
  - Determine the optimum values for  $M$  and  $C_2$  to deliver the maximum average power to the load  $Z_L$ ;
  - Calculate this maximum average power delivered to the load.



$$\left( \frac{16C_2 - 1}{4C_2 M} \right) I_2' + \dots$$

$$C \frac{dv_c}{dt} = I_2'$$

$$V_c =$$

$$I_2' + \frac{4}{M} I_2' - jM I_2' + j I_1'$$

$$I_1' = \frac{I_2' + \frac{4}{M} I_2' - jM I_2' + j I_1'}{-4C_2 M}$$

$$I_1' = I_1' - jM I_2' + j I_1'$$

$$I_1' = \frac{1}{-4C_2 M} I_2' + \frac{16C_2 - 1}{4C_2 M} I_2'$$