## UCLA Department of Electrical Engineering EE101A – Engineering Electromagnetics Fall 2018 Midterm, November 13, 2018, (100 minutes)

Name:



Student number:



This is a closed book exam – you are allowed 2 pages (A4 size) of notes (front + back). You are allowed to use a calculator. You are NOT allowed to use other electronic devices such as laptops and cell phones.

Check to make sure your test booklet has all of its pages – both when you receive it and when you turn it in.

Remember – there are several questions, with varying levels of difficulty, be careful not to spend too much time on any one question to the exclusion of all others.

Exam grading: When grading, we focusing on evaluating your level of understanding, based on what you have written out for each problem. For that reason, you should make your work clear, and provide any necessary explanation. In many cases, a correct numerical answer with no explanation will not receive full credit, and a clearly explained solution with an incorrect numerical answer will receive close to full credit. CIRCLE YOUR FINAL ANSWER.

If an answer to a question depends on a result from a previous section that you are unsure of, be sure to write out as much of the solution as you can using symbols before plugging in any numbers, that way you will still receive the majority of credit for the problem, even if your previous answer was numerically incorrect.

Please be neat – we cannot grade what we cannot decipher.

	Topic	Max Points	Your points
Problem 1	Electrostatics	15	15
Problem 2	Plane Wave	15	15
Problem 3	Faraday's Law	30	20
Problem 4	Capacitor	20	20
Problem 5	Ampere's Law	20	20
Total		100	90

### Midterm

EE101A – Engineering Electromagnetics
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Constants (SI units):

$$\varepsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$
  
 $\mu_0 = 4\pi \times 10^{-7} \text{H/m}$ 

#### 1. Electrostatics (15 points)

Which of the two following expressions does not meet the electrostatic field assumptions? Explain why.

(A): 
$$\vec{E} = 3[(5x + 2z^2)\hat{x} + 2yz\hat{y} + (4xz + y^2)\hat{z}]$$

(B): 
$$\vec{E} = 2[(2x + y^2)\hat{x} + (3xy + z^2)\hat{y} + (2yz)\hat{z}]$$

if static then.

$$\nabla \times \vec{E} = 0$$
 (=)  $\frac{\partial \vec{E}_i}{\partial y} = \frac{\partial \vec{E}_j}{\partial z} = \frac{\partial \vec{E}_j}{\partial z}$ 

$$\frac{\partial \mathcal{E}_{x}}{\partial z} = \frac{\partial \mathcal{E}_{z}}{\partial x}$$

A: 
$$\frac{\partial \ell z}{\partial y} = y$$
  $\frac{\partial \ell y}{\partial z} = y$   $\sqrt{B} = \frac{\partial \ell z}{\partial y} = 2z$   $\frac{\partial \ell y}{\partial z} = 2z$   $\sqrt{B} = \frac{\partial \ell z}{\partial y} = 2z$ 

A: 
$$\frac{\partial \mathcal{E}_x}{\partial z} = 42$$
  $\frac{\partial \mathcal{E}_z}{\partial x} = 42$   $\sqrt{B} = \frac{\partial \mathcal{E}_{xx}}{\partial z} = 0$   $\frac{\partial \mathcal{E}_z}{\partial x} = 0$   $\sqrt{C}$ 

A: 
$$\frac{\partial Ey}{\partial x} = 0$$
  $\frac{\partial Ex}{\partial y} = 0$   $\frac{\partial Ex}{\partial x} = \frac{\partial Ey}{\partial y} = \frac{\partial Ex}{\partial y} = \frac{\partial Ex}{$ 

B does not since 
$$\nabla \times \vec{\epsilon}_8 \neq 0$$
 therefore  $\frac{\partial B}{\partial t} \neq 0$ 

# 2. Plane Wave (15 points)

The magnetic field of a wave propagating through a certain nonmagnetic material is given by  $\vec{H} = \hat{z} \cdot 45 \cos(2\pi \times 2 \times 10^8 t + 2\pi \cdot y) \pmod{mA/m}$ 

Find the following:

- (a) The direction of wave propagation.
- (b) The phase velocity.
- (c) The wavelength in the material.
- (d) The relative permittivity of the material.

(e) The electric field phasor.

and it's a pluc sign

(b). 
$$u_0 = \frac{\omega}{k} = \frac{2\pi \cdot 2 \cdot 10^8}{2\pi} = 2.10^8 \text{ m/s}.$$

(c). 
$$\lambda = \frac{2\lambda}{k} = \frac{2\lambda}{2\lambda} = 1 \text{ m.}$$

(d). Since up = 2.108 m/s and 
$$\frac{1}{\sqrt{\mu_0 \epsilon_0}} = 3.108 m/s$$
 :  $\sqrt{\epsilon_0} = \frac{3}{2} \epsilon_1 = \frac{9}{6} = 2.25$ 

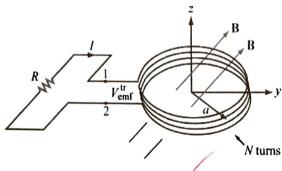
$$= \frac{1}{\sqrt{\mu_0 \epsilon_0 \epsilon_0}}$$

Since 
$$\vec{E} = \vec{J} \cdot \vec{H} = \sqrt{\frac{63.10^{-3}}{P.85.10^{-32}. L-25}} \cdot \vec{H} = \sqrt{\frac{2.5.10^{-3}}{P.85.10^{-32}. L-25}}} \cdot \vec{H} = \sqrt{\frac{2.5.10^{-3}}{P.85.10^{-3}. L-25}}} \cdot \vec{H} = \sqrt{\frac{2.5.10^{-3}}{P.85.10^{-3}}} \cdot \vec{H} = \sqrt{\frac{2$$

## 3. Faraday's Law (30 points)

An inductor is formed by winding N turns of thin conducting wire into a circular loop of radius a. The inductor loop is in the x-y plane with its center at the origin, and connected to a resistor R, as shown in the figure below. In the presence of a magnetic field  $\vec{B} = B_0(\hat{y} + 2\hat{z}) \cos \omega t$ , where  $\omega$  is the angular frequency. Find the following parameters:

- (a) the magnetic flux linking a single turn of the inductor;
- (b) the  $V_{emf}^{tr} = V_1 V_2$ , given that N = 20,  $B_0 = 0.2$  T, a = 15 cm, and  $\omega = 10^3$  rad/s;
- (c) the polarity of  $V_{emf}^{tr}$  at  $\omega t = \pi/2$ ;



(b) 1 1 10 5 12 2

z. 87. (0.15)2. 103. sin 103t

= 0.87.225 · Sinjo3t = 17 500 565.5 Sin 1000t (V)

(c). when wt = }

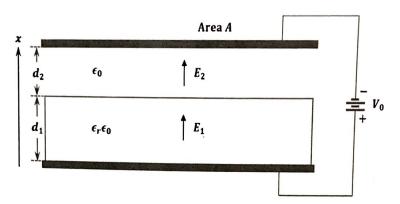
then Very = N.Bo. > 22a2. w(V) is linear dependent on w

X

## 4. Capacitor (20 points)

A parallel plate capacitor with electrodes of area A has its upper electrode in a free space region of thickness  $d_2$  in series with a solid dielectric of thickness  $d_1$  and dielectric relative permittivity  $\epsilon_r$ . The  $x = d_1$  interface has no free surface charge.





- (a) What are the electric field  $E_1$  and  $E_2$  in the dielectric and free space regions?
- (b) What is the free surface charge density on the lower electrode?
- (c) What is the capacitance C of the capacitor?

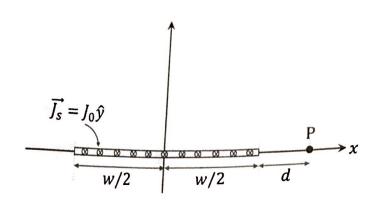
(c) C = 2+0+ = A \(\frac{1}{2}\) \(\frac{1}{2}\)

(a) since 
$$C_1 = \frac{A \sum r \sum r}{d_1} = \frac{Q}{V_1}$$

$$C_2 = \frac{A \sum r}{d_2} = \frac{Q}{V_2}$$

$$\frac{V_1 \cdot V_2}{Q} = \frac{d_2}{A \sum r} + \frac{d_1}{A \sum r \sum r} = \frac{V_0}{Q} = \frac{d_2 \sum r \cdot d_1}{A \sum r}$$

$$C_1 \cdot V_2 \cdot V_2 \cdot V_2 \cdot V_3 \cdot V_4 \cdot V_4 \cdot V_5 \cdot V_6 \cdot V_6 \cdot V_6 \cdot V_7 \cdot V_7$$



An infinitely long thin conducting sheet of width w positioned along the x direction and lying in the x-y plane as shown in the figure. It carries a surface current density of  $\vec{J}_s = J_0 \hat{y}$ . Find the magnetic field  $\vec{H}$  at point P.

He x-y plane as shown in the figure. It carries a surface current density of 
$$J_3$$
 agnetic field  $\overrightarrow{H}$  at point  $P$ .

Ampere's  $Jaw$ :

$$\overrightarrow{Ampere} = Jaw:$$

$$\overrightarrow{Ampere} = Jo.dr.$$

$$\overrightarrow{Ampere} = Jo.dr.$$