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1	2	3	4	5	6	7	8	9	sum
12	0	2	0	0	6	12	10	9	51

1 (12 minutes). Which integer constants can a single x86 leal instruction can multiply an arbitrary integer N by? The idea is that one puts N into a register, executes the leal instruction, and the bottom 32 bits of $N \times K$ will be put into some other register, where K is a constant. For which values of K can this be done? For each such value, show an leal instruction that implement that value.

2 (12 minutes). On the x86-64, what's the fastest way to reverse each 8-bit byte in a 64-bit unsigned integer? For example, given the input integer 0x0123456789abcdef, we want to compute 0x80c4a2e691d5b3f7; this is because 0x01 is binary 00000001 and reversing it yields binary 10000000 which is 0x80, and similarly the bit-reverse of 0x23 is 0xc4, and so forth until the bit-reverse of 0xef is 0xf7. Write the code in C, and estimate how many machine instructions will be generated (justify your estimate).

3 (12 minutes). On the x86, there is no 'pushl %eip' instruction. Suppose you want to push the instruction pointer onto the stack anyway. What's the best way to do it? If your method takes three instructions A, B, C, the value pushed onto the stack should be the address of D, the next instruction after C.

4 (12 minutes). Explain two different methods that GDB can implement its 'fin' command (which finishes execution of the current function), one method with hardware breakpoints and one without. For each method, say what happens if the current function calls another function via tail recursion.

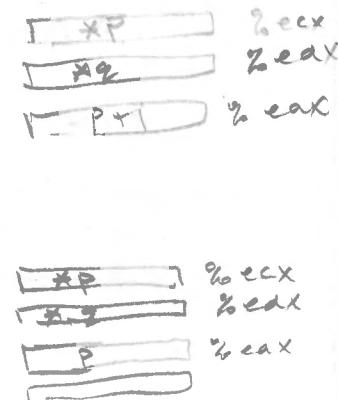
5 (12 minutes). Consider the following C functions and their translations to x86 code.

```
int f (int *p, long *q) {
    ++*p;
    ++*q;
    return *p;
}

int g (int *p, char *q) {
    ++*p;
    ++*q;
    return *p;
}

f:    movl    4(%esp), %ecx
      movl    8(%esp), %edx
      movl    (%ecx), %eax
      addl    $1, %eax
      movl    %eax, (%ecx)
      addl    $1, (%edx)
      ret

g:    movl    4(%esp), %ecx
      movl    8(%esp), %edx
      movl    (%ecx), %eax
      addb    $1, (%edx)
      addl    $1, %eax
      movl    %eax, (%ecx)
      ret
```



There's a compiler bug: one of these functions is translated incorrectly, and the other one is OK. Identify the bug, and explain why the other function is translated correctly even though one might naively think that its translation has a similar bug.

6 (12 minutes). Suppose we have allocated memory locations 0xffff0000 through 0xffffffff for the stack, and we are worried that our x86 program might overflow the stack. We decide to institute the ironclad rule that if a function ever attempts to grow the stack past the allocated bounds, the function immediately stops what it's doing and returns 0, thus shrinking the stack. Explain the problems you see in implementing this rule. Don't worry about the effects of this rule on the user program; worry only about implementing the rule correctly.

7 (12 minutes). Give C source code that corresponds to the following x86-64 assembly language code. Explain briefly and at a high level what useful thing the function does.

```

sub:    movq    %rdi, %rdx      rdi = x
        subq    %rsi, %rdx      rsi = y
        xorq    %rdi, %rsi      rdx = temp
        xorq    %rdi, %rdx
        movq    %rdx, %rax
        andq    %rsi, %rax
        shrq    $63, %rax
        ret
    
```

$\text{rdi} = x$
 $\text{rsi} = y$
 $\text{rdx} = \text{temp}$
 $((x-y)^x) \& (y^x)$

```

bool sub(long x, long y){
    long temp = x - y;
    y ^= x;
    temp ^= x;
    return (temp & y >> 63) & 0x01;
}
    
```

It returns true if $x-y$ will overflow
false otherwise

8 (12 minutes). Match each of the following C source functions to each of the following assembly-language functions. A "match" means that the assembly-language code properly implements the C code. For example, if the C function 'f' is implemented by the assembly-language implementation 'B', write "f=B".

```

int a(int x) { while (x & 1) x>>=1; return x; }
int b(int x) { while (x & 3) x>>=1; return x; }
int c(int x, int y)
{ return x / y - (x % y < 0); }
int d(int x, int y)
{ return x % y + (x % y < 0 ? y : 0); }
int e(unsigned x, unsigned y)
{ return (x + y < x) ^ ((int)y < 0); }
int f(int a, int b, int c) { return a ? b : c; }
int g(int a, int b, int c)
{ return a ? b + c : b & c; }
int h(unsigned x, unsigned y)
{ return x - x / y * y; }
int i(int x, int y) { return x - x / y * y; }
int j(int x) { return ~x; }
int k(int x) { return ~-x; }
int l(int x) { return x+~x; }
    
```

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b = A ✓	e = J ✓	h = H ✓
a = D ✓	d = L ✓	i = E
g = B ✓	c = K	10
f = C ✓		
k = F ✓		
j = I ✓		
l = G ✓		

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A: movl 4(%esp), %eax
 testb \$3, %al
 je .L2

.L3: sarl %eax
 testb \$3, %al
 jne .L3

.L2:
 ret

B: movl 8(%esp), %eax
 movl 12(%esp), %edx
 movl %eax, %ecx
 orl %edx, %ecx
 andl %eax, %edx
 movl 4(%esp), %eax
 testl %eax, %eax
 movl %ecx, %eax
 cmovc %edx, %eax
 ret

C: movl 4(%esp), %eax
 testl %eax, %eax
 movl 12(%esp), %eax
 cmovne 8(%esp), %eax
 ret

D: movl 4(%esp), %eax
 testb \$1, %al

.L17: je .L16
 sarl %eax

.L16:
 testb \$1, %al
 jne .L17
 ret

E: movl 4(%esp), %eax
 cltd
 idivl 8(%esp)
 shr1 \$31, %edx
 subl %edx, %eax
 ret

F: movl 4(%esp), %eax
 subl \$1, %eax
 ret

$$\sim x + 1 = -x$$

$$\sim x = -x - 1$$

G: movl \$-1, %eax
 ret

H: movl 4(%esp), %eax
 xorl %edx, %edx
 divl 8(%esp)
 movl %edx, %eax
 ret

X %eax
00000000 %

I: movl 4(%esp), %eax
 addl \$1, %eax
 ret

J: movl 8(%esp), %edx
 movl %edx, %eax
 addl 4(%esp), %eax
 setc %al
 shr1 \$31, %edx
 xorl %eax, %edx
 movzbl %dl, %eax
 ret

K: movl 4(%esp), %eax
 cltd
 idivl 8(%esp)
 movl %edx, %eax
 ret

L: movl 4(%esp), %eax
 movl 8(%esp), %ecx
 cltd
 idivl %ecx
 movl \$0, %eax
 testl %edx, %edx
 cmovns %eax, %ecx
 leal (%edx,%ecx), %eax
 ret

X %eax
Y %ecx

9 (12 minutes). Consider the following program:

```
1 unsigned ack (unsigned m, unsigned n) {  
2     if (m == 0)  
3         return n + 1;  
4     if (n == 0)  
5         return ack (m - 1, 1);  
6     return ack (m - 1,  
7                  ack (m,  
8                      n - 1));  
9 }
```

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and the following assembly-language implementation as reported by objdump:

```
1 ack:  
2     pushl %ebx - callee save  
3     subl $8, %esp  
4 fm %ebx movl 16(%esp), %ebx line 1 +4  
5 fm %eax movl 20(%esp), %eax line 1  
6 fm %eax testl %ebx, %ebx line 2  
7     +2 je .L2 z,3 this is the if statement  
8     subl $1, %ebx 5 & 6 both have m-1  
9     +2 jmp .L4 transition from line 2 → 4  
10    .L7:  
11     testl %ebx, %ebx → line 2  
12     movl $1, %eax  
13     leal -1(%ebx), %edx  
14     ✓ je .L2 jump from line 2 → 3  
15    .L6:  
16     fm movl %edx, %ebx line 5 & 6 both have  
17    .L4:  
18     testl %eax, %eax line 4 ✓  
19 fm %edx leal 1(%ebx), %edx  
20     je .L7 jump line 5 → 2 ✓  
21     subl $8, %esp - decrement stack  
22     subl $1, %eax line 8  
23     pushl %eax ] caller save  
24     pushl %edx  
25     call ack line 7 ✓  
26     addl $16, %esp allocate stack frame  
27     testl %ebx, %ebx line 2 ✓  
28 fm %edx leal -1(%ebx), %edx line 5 & 6 both  
29     jne .L6 jump 2 → 5 or have m-1  
30    .L2:  
31     addl $8, %esp - decrement stack  
32     addl $1, %eax - line 3  
33     popl %ebx - callee restore  
34     ret line 3
```

For each instruction in the implementation, identify the corresponding source-code line number. If an instruction corresponds to two or more source-code line numbers, write them all down and explain.