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PRINT CLEARLY

Physics 1B - WHITTEN SQ2010

SECOND HOUR EXAM, MAY 21, 2010

11:00 - 11:50 A.M.

Indicate your reasoning clearly and include all calculations on the pages you hand in. If your work is not entirely on a given problem's page, indicate on that page where the work is located.

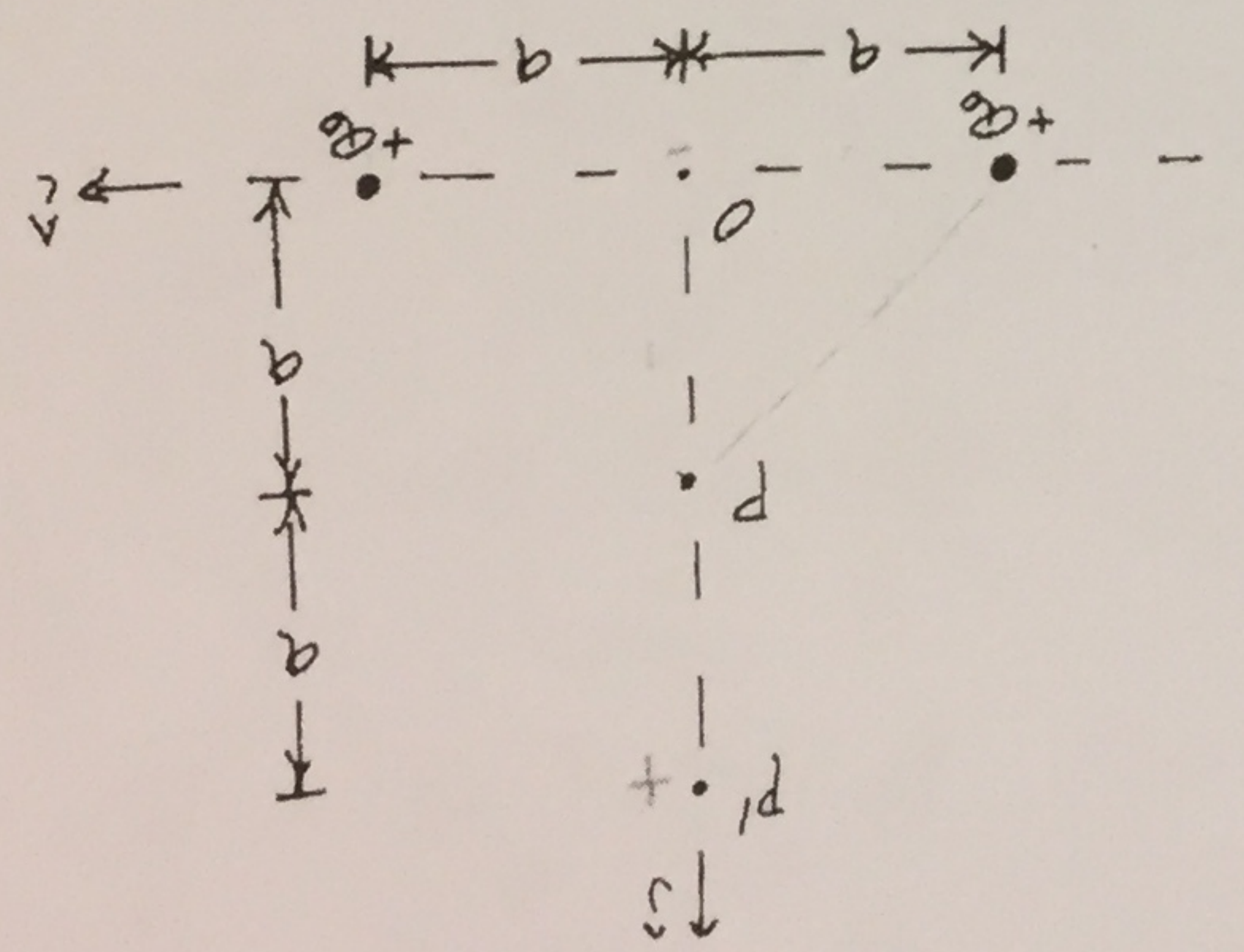
Problem 1. 14

Problem 2. 27

Problem 3. 17

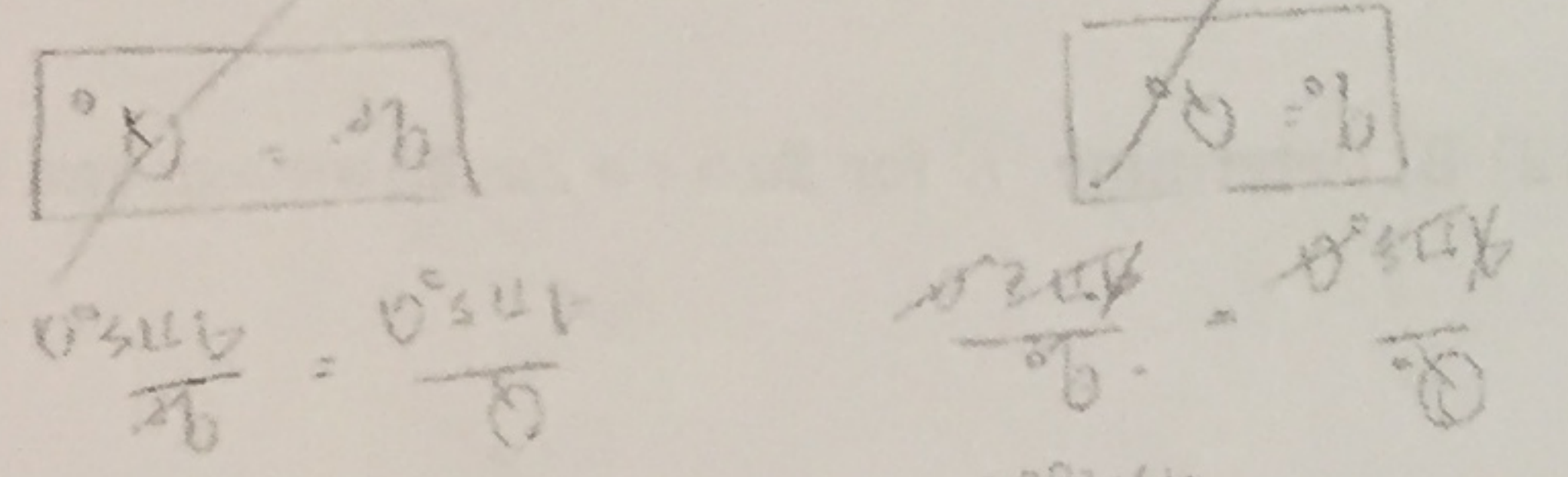
Total Score

58



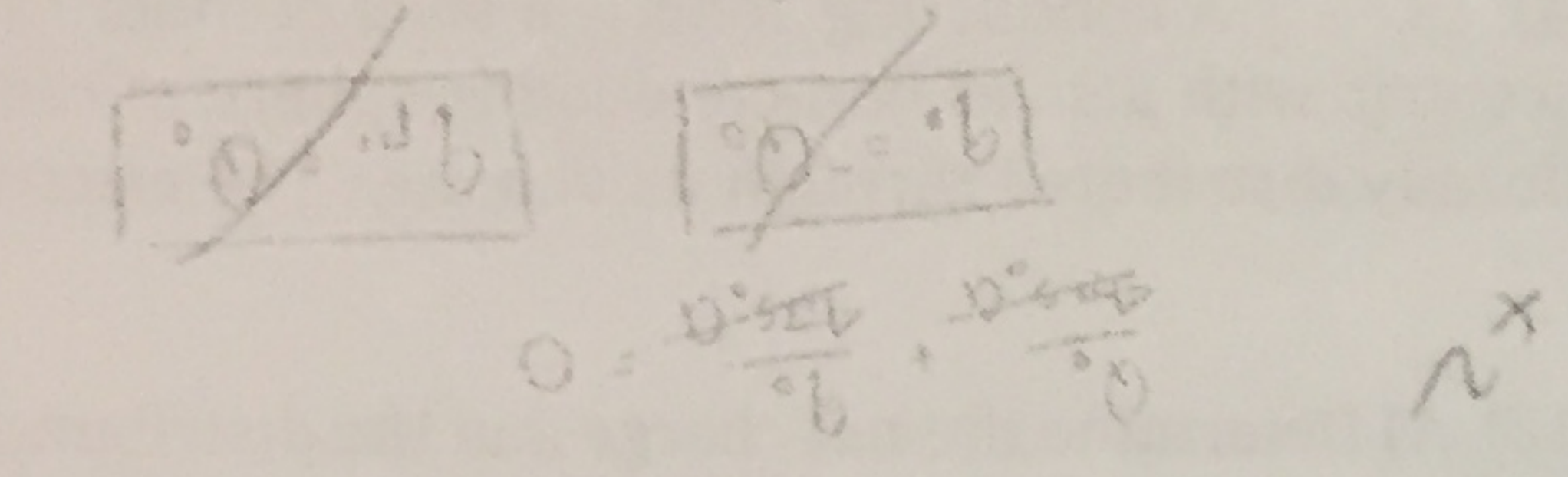
(34) 1.

(13) A) With the two point charges $+Q_0$ at the positions indicated a third point charge is placed at either position O or position P' . For these two situations calculate the value of the third charge such that $\vec{E}(P) = 0$



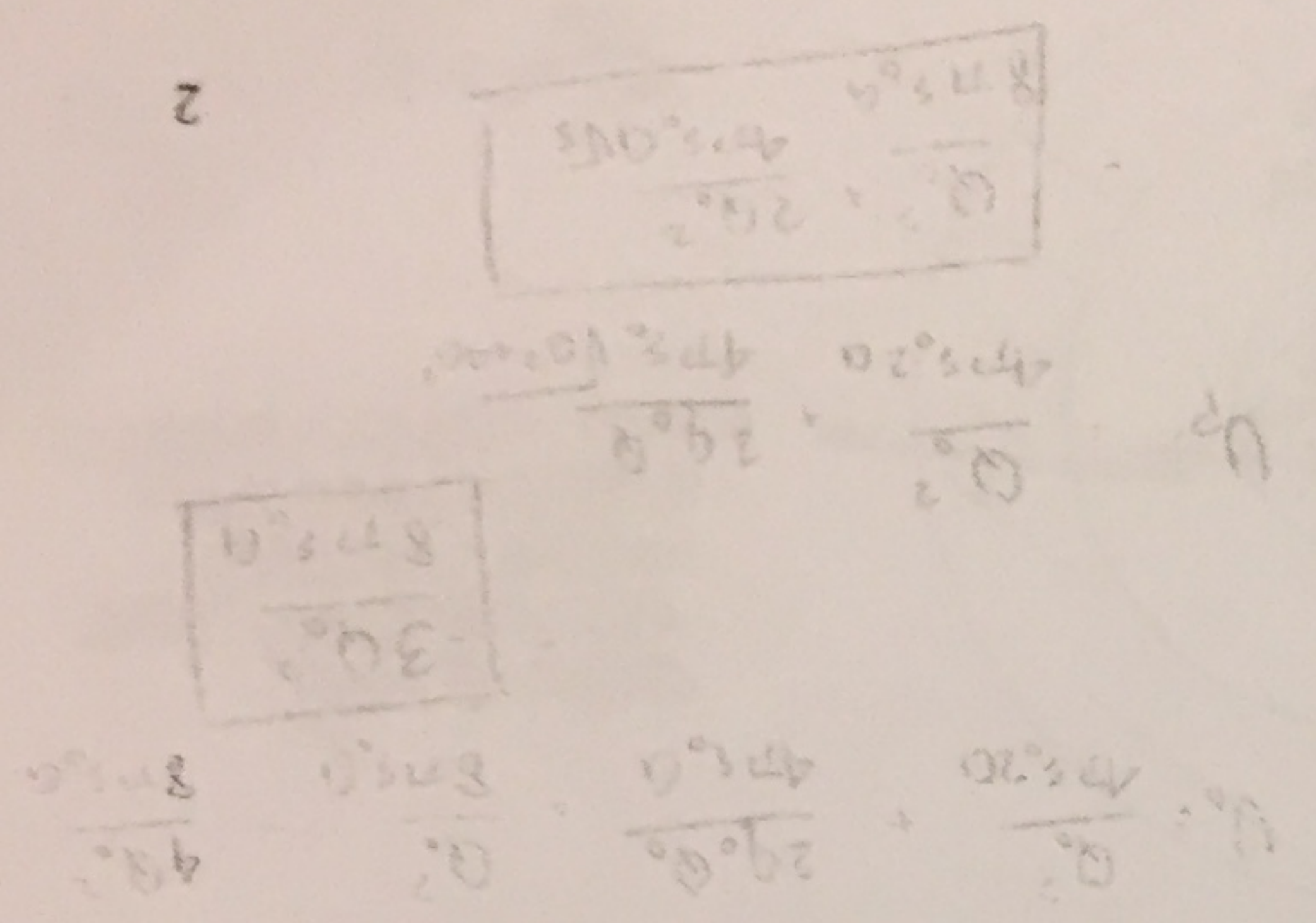
(11) B)

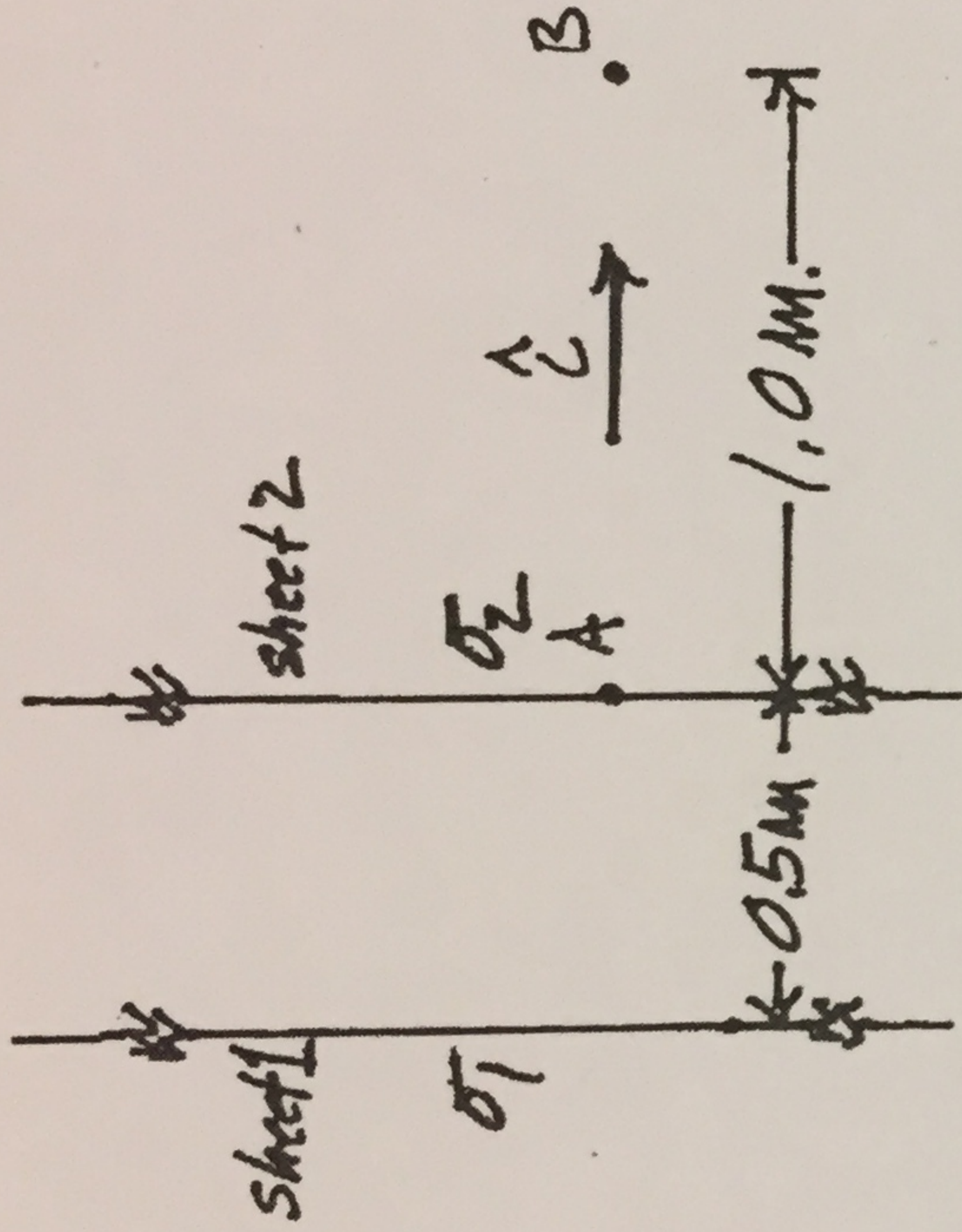
Again a third charge is placed either at position O or at position P' . However, for these two situations now calculate the value of the third point charge such that $V(P) = 0$ (Use the convention $V(\infty) = 0$).



(10) C)

For part A) calculate the electrostatic potential energy for the two situations.





(34) 2. Consider two infinite sheets a distance 0.5 meters apart with respective constant surface charge densities σ_1 and σ_2 . $\sigma_1 = +4 \times 10^{-9}$ Coulombs/m² and $\vec{E} = 75 \hat{i}$ volts/meter between the sheets.

(in mks units $1/\epsilon_0 = 1.13 \times 10^{11}$)

(20) A.) Calculate σ_2 (Coulombs/m²).

$$E = 75 \text{ V/m}$$

$$E = \frac{\sigma}{2\epsilon_0} = \frac{\sigma_1 - \sigma_2}{2\epsilon_0} = 75$$

$$\sigma_2 = 2\epsilon_0 75 - \sigma_1 = \boxed{2.067 \times 10^{-9} \text{ C/m}^2}$$

+20

(7) B.) Calculate \vec{E} (vector, volts/m) to the right of sheet 2 and to left of sheet 1..

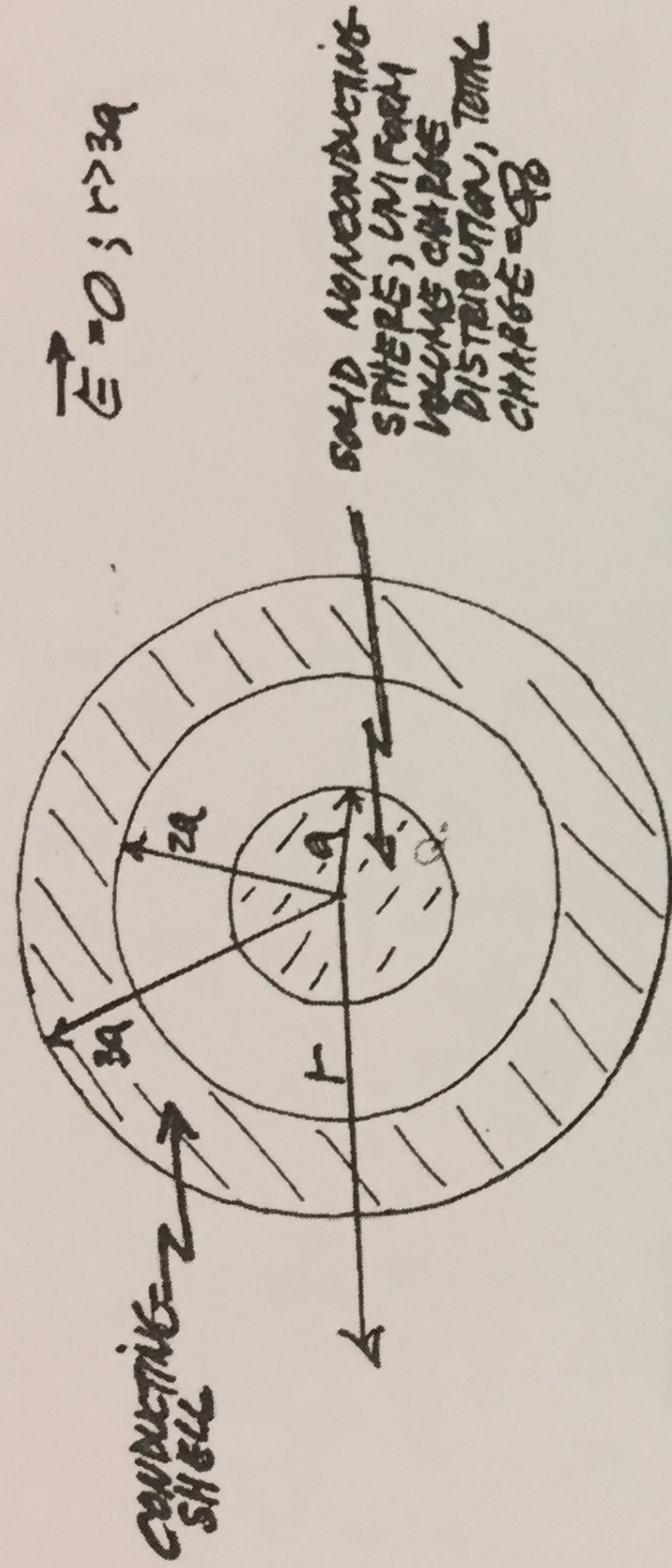
$$E_{\text{right of sheet 2}} = \frac{\sigma_2 + \sigma_1}{2\epsilon_0} = \boxed{377 \text{ V/m}}$$

$$\boxed{-377 \text{ V/m}}$$

1011

(7) C.) Calculate the potential difference $V(A) - V(B)$ in volts.

~~9 27~~



(34) 3. A conducting spherical shell of inner radius $2a$ and outer radius $3a$ is concentric with a solid non-conducting sphere of radius a having a total charge Q_0 uniformly distributed through its volume. The electric field for $r > 3a$ is given by $\vec{E} = 0$.

(12) A) Determine the net charge and the distribution of charge on the conducting shell.

net charge: $-Q_0$
 $-Q_0$ is on the inner rim and $+2Q_0$ is on the outer rim

(12) B) Determine \vec{E} for $3a > r > 2a$; $2a > r > a$; and $a > r \geq 0$.

$3a > r > 2a: \vec{E} = 0$
 $2a > r > a: \vec{E} = \frac{Q_0}{4\pi\epsilon_0 r^2}$
 $a > r \geq 0: \vec{E} = \frac{Q_0}{4\pi\epsilon_0} \frac{r}{a^3}$

(10) C) Using the convention $V(r = \infty) = 0$ determine $V(r)$ everywhere and show that $V(r=0) = \frac{Q_0}{4\pi\epsilon_0 a}$

$r > 3a: V = \int_{\infty}^r E dx = \int_{\infty}^r 0 dx = 0$
 $2a > r > a: V = \int_{\infty}^{2a} E dx + \int_{2a}^r E dx = 0 + \int_{2a}^r \frac{Q_0}{4\pi\epsilon_0 x^2} dx = 0 + \left[\frac{Q_0}{4\pi\epsilon_0} \left(\frac{1}{x} \right) \right]_{2a}^r = \frac{Q_0}{4\pi\epsilon_0} \left(\frac{1}{r} - \frac{1}{2a} \right)$
 $a > r \geq 0: V = \int_{\infty}^{3a} E dx + \int_{3a}^{2a} E dx + \int_{2a}^r E dx = \int_{\infty}^{3a} \frac{Q_0}{4\pi\epsilon_0 x^2} dx + \int_{3a}^{2a} 0 dx + \int_{2a}^r \frac{Q_0}{4\pi\epsilon_0 x^2} dx = \frac{Q_0}{4\pi\epsilon_0} \left(\frac{1}{3a} - \frac{1}{\infty} \right) + 0 + \left[\frac{Q_0}{4\pi\epsilon_0} \left(\frac{1}{x} \right) \right]_{2a}^r = \frac{Q_0}{4\pi\epsilon_0} \left(\frac{1}{3a} + \frac{1}{2a} - \frac{1}{r} \right) = \frac{Q_0}{4\pi\epsilon_0} \left(\frac{5}{6a} - \frac{1}{r} \right)$