

MSE 104, QUIZ No. 1 ver 1 (1hr)
 Winter 2017

NAME: Quen Hava Malyer

Show all work and include units
 for full credit

UCLES

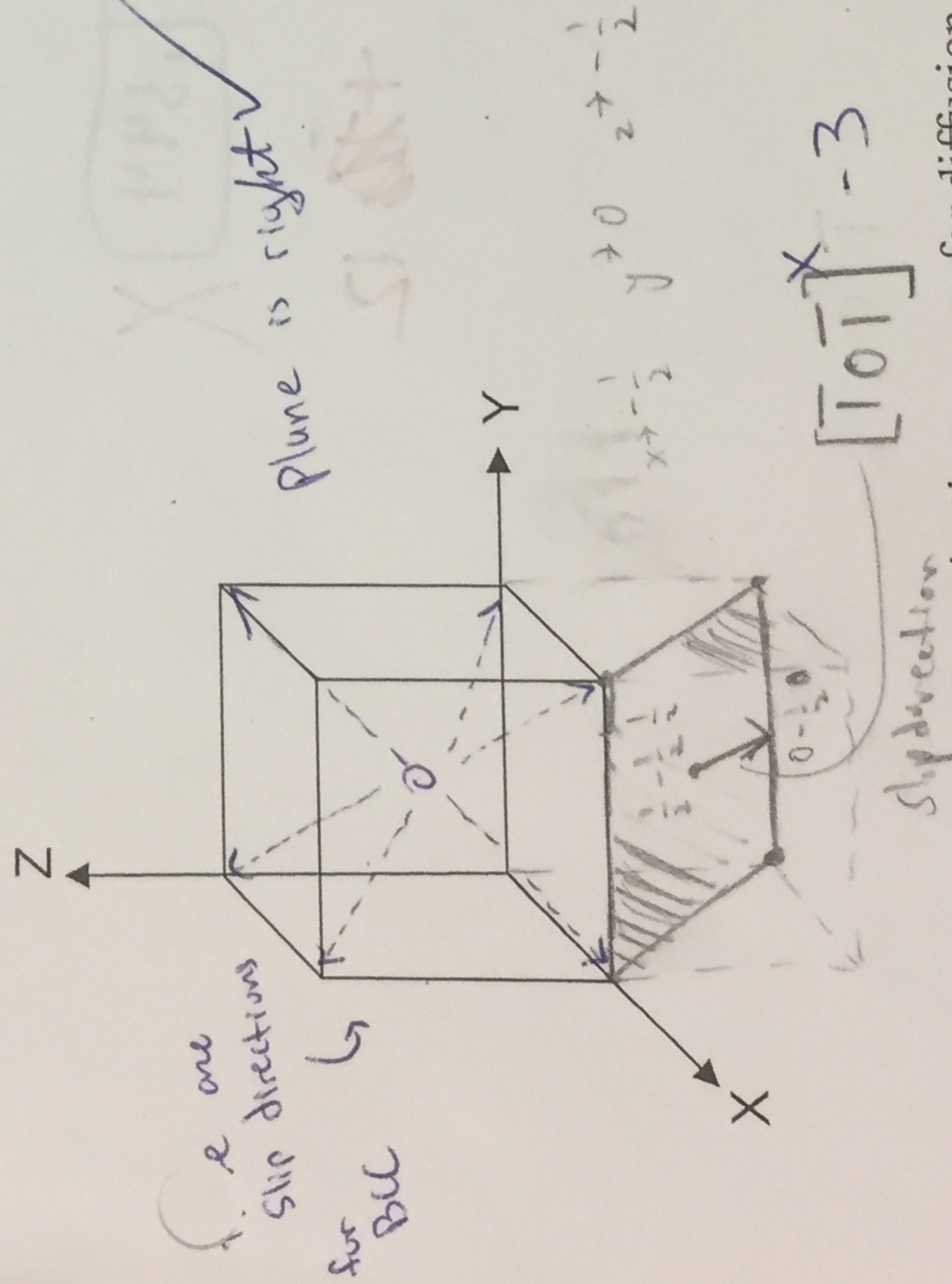
Problem 1 (15 pts) Short answer

1 (15 pts)	10
2 (30 pts)	19
3 (25 pts)	14
4 (30 pts)	30
Total points	73

a. State for each type of bonding whether it is directional or non-directional. (6 pts)

- i. Covalent Directional ✓
- ii. Ionic Directional ✗
- iii. Metallic Non directional ✓

b. Draw the (101) plane, and within that plane, draw one slip direction that would be possible for a BCC metal and state the indices for the direction you have drawn.



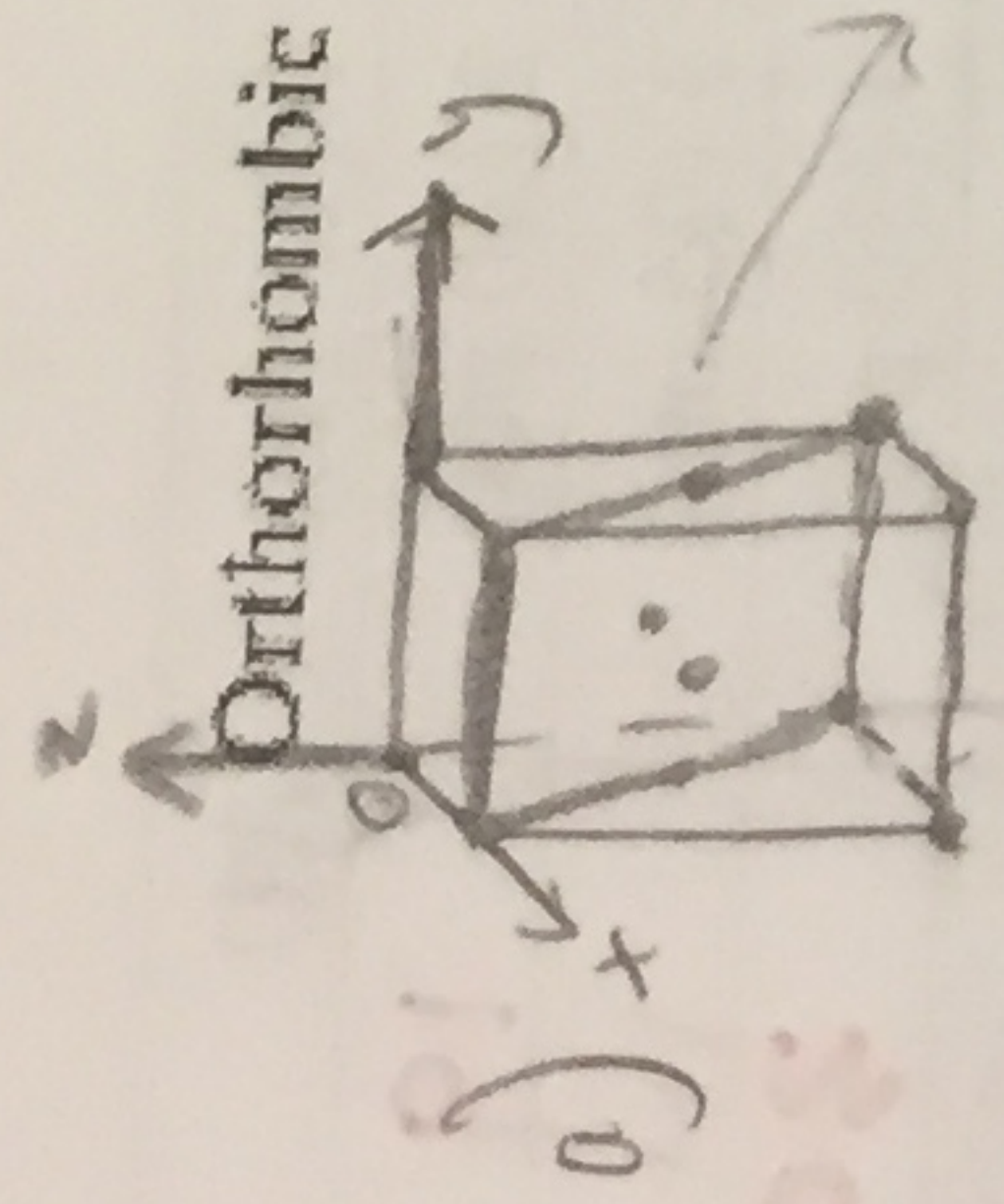
c. Would you expect the activation energy for diffusion to be higher in self-diffusion via vacancies or impurity atom diffusion via interstitials (no explanation necessary)? (3 pts)

self-diffusion via vacancies ✓

Problem 2 (30 pts) Crystal structure

The orthorhombic crystal structure is shown below, and $a = 0.35 \text{ nm}$, $b = 0.38 \text{ nm}$, and $c = 0.30 \text{ nm}$. Assume that a is in the x -direction, b is in the y -direction, and c is in the z -direction. Solve the following problems:

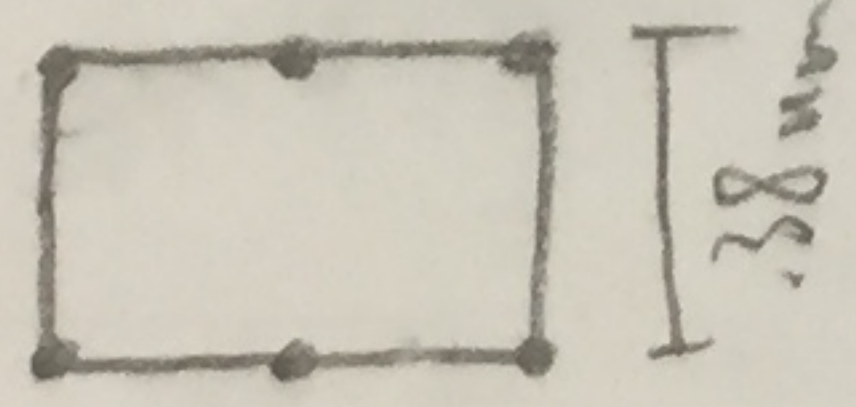
- For a face-centered orthorhombic unit cell, draw the $(1\bar{1}0)$ plane and derive the planar density in number/ nm^2 (number of atoms on plane based on their area divided by total planar area) for that plane.
- What is the atomic packing factor for the face-centered orthorhombic unit cell if the atomic radius is 0.120 nm ?



$a \neq b \neq c$

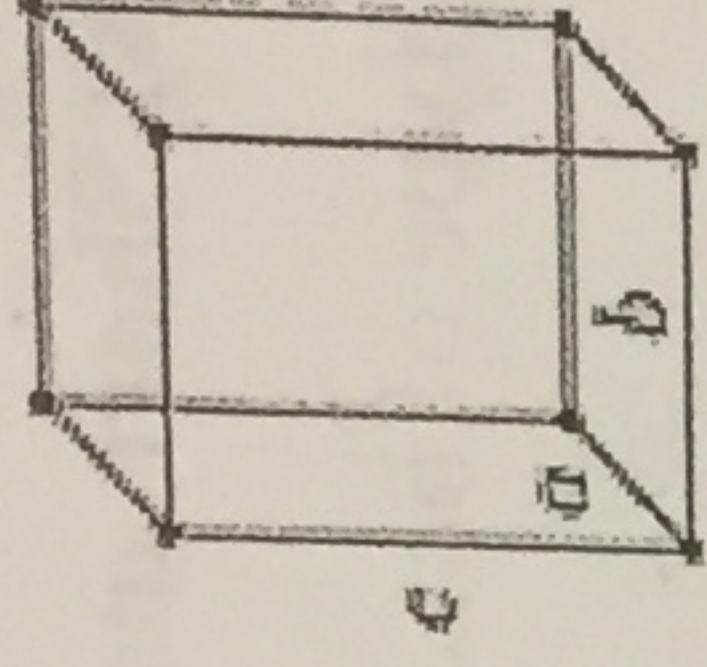
$\alpha = \beta = \gamma = 90^\circ$

(110)



$$\sqrt{0.35^2 + 0.30^2} = 0.461 \text{ nm}$$

~~X~~ +2



$$\frac{\frac{1}{4} \cdot 4 + \frac{1}{2} \cdot 2}{0.38 \text{ nm} \cdot 0.461 \text{ nm}} = 11.4 \frac{\text{number}}{\text{nm}^2}$$

~~X~~ +5

b) # atoms per cell = $\frac{1}{8} \cdot 8 + \frac{1}{2} \cdot 4 = 3$ ~~4~~

$$\text{APF} = \frac{V_{\text{atoms}}}{V_c} = \frac{3 \cdot \frac{4}{3} \pi \cdot (0.120 \text{ nm})^3}{0.35 \text{ nm} \cdot 0.38 \text{ nm} \cdot 0.30 \text{ nm}} = 1.544$$

~~X~~ +12

Problem 3 (25 pts) Crystal structure and Defects

A hypothetical pure FCC metal has an atomic radius of 0.140 nm. Assume the energy for vacancy formation is 0.85 eV/atom. (Hint: In the vacancy number density equation, N_0 is the number density of atoms in a perfect crystal and it can be calculated based on crystal structure). What is the number density of vacancies (in units of m^{-3}) at 1200K?

$$N_v = N_0 e^{-\frac{Q_v}{kT}}$$

$$N_v = 8.88 \times 10^{28} \text{ m}^{-3} \cdot e^{-\frac{0.85 \text{ eV/atom}}{8.62 \times 10^{-5} \text{ eV/atom} \cdot \text{K} \cdot 1200 \text{ K}}}$$

$$= 2.40 \times 10^{25} \text{ m}^{-3}$$

$$\# \text{ atoms/cell in FCC: } \frac{1}{8} \cdot 8 \cdot \frac{1}{2} \cdot 6 = 3$$

$$V_{\text{cell}} = a^3$$

$$= (0.323 \times 10^{-9} \text{ m})^3$$

$$= 3.38 \times 10^{-29} \text{ m}^3$$

$$N_0 = \frac{3 \text{ atoms}}{3.38 \times 10^{-29} \text{ m}^3} = 8.88 \times 10^{28} \text{ m}^{-3}$$

$$a = \frac{4R}{\sqrt{3}} = 0.323 \text{ nm}$$

Problem 4 (30 pts)

30

In the preparation of a semiconducting device, gallium (Ga) atoms are to be diffused into pure silicon (Si) at 1200°C for 2 hours. If the required concentration of Ga at a position 1.5 μm below the surface is 5×10^{23} atoms/m³, compute the required surface concentration assuming that the surface concentration remains constant and the diffusion pre-exponential and activation energy values are 3.74×10^{-5} m²/s and 327.2 KJ/mol, respectively.

$$T = 1200^\circ\text{C} = 1473 \text{ K}, \quad t = 2 \text{ h} = 7200 \text{ s}, \quad x = 1.5 \times 10^{-6} \text{ m}, \quad C_s = 5 \times 10^{23} \text{ atoms/m}^3$$

(pure silicon) $C_0 = 0$

$$D = \frac{3.74 \times 10^{-5} \text{ m}^2/\text{s}}{\exp\left(\frac{-327.2 \text{ kJ/mol}}{8.314 \times 10^{-3} \text{ kJ/mol}\cdot\text{K} \cdot 1473 \text{ K}}\right)}$$

$$D = 3.74 \times 10^{-5} \text{ m}^2/\text{s} = 9.32 \times 10^{-17} \text{ m}^2/\text{s}$$

$$\frac{x}{2\sqrt{Dt}} = \frac{1.5 \times 10^{-6} \text{ m}}{2\sqrt{9.32 \times 10^{-17} \text{ m}^2/\text{s} \cdot 7200 \text{ s}}} = 0.915$$

$$\text{erf}(0.915) = 0.7970 + (0.8209 - 0.7970) \left(\frac{0.015}{0.05}\right)$$

$$= 0.804$$

$$\frac{C_x - C_0}{C_s - C_0} = 1 - \text{erf}\left(\frac{x}{2\sqrt{Dt}}\right)$$

$$C_s = C_0 + \frac{C_x - C_0}{1 - \text{erf}\left(\frac{x}{2\sqrt{Dt}}\right)}$$

$$C_s = \frac{C_x}{1 - \text{erf}\left(\frac{x}{2\sqrt{Dt}}\right)}$$

$$C_s = \frac{5 \times 10^{23} \text{ atoms/m}^3}{1 - 0.804}$$

$$C_s = 2.56 \times 10^{24} \text{ atoms/m}^3$$